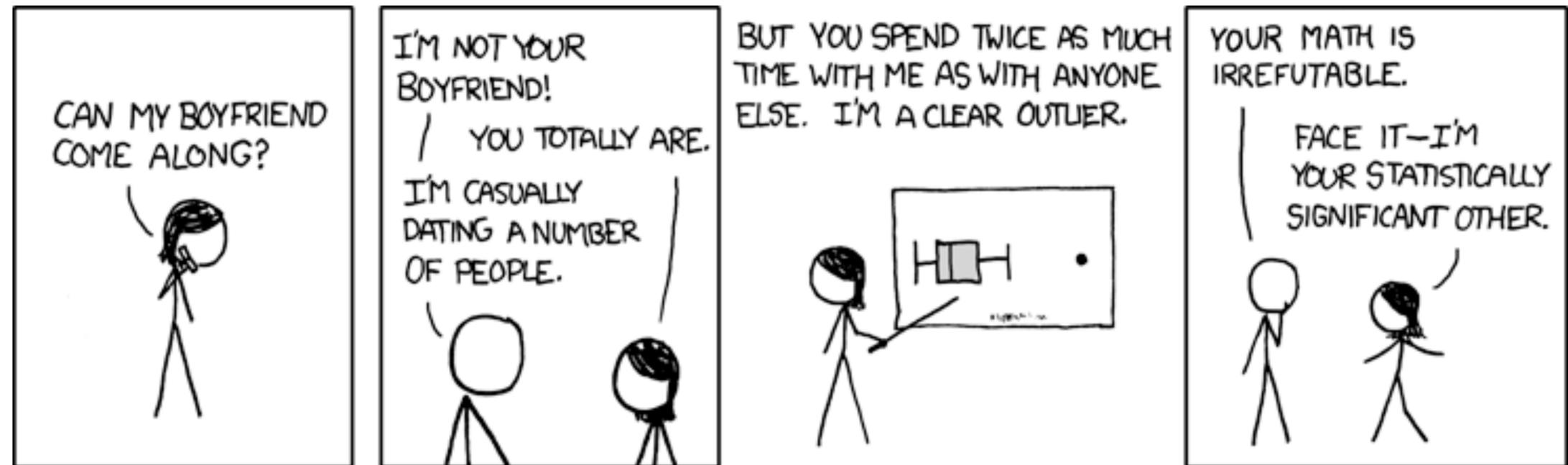


# CS-5630 / CS-6630 Visualization for Data Science

## Filtering & Aggregation

Alexander Lex  
[alex@sci.utah.edu](mailto:alex@sci.utah.edu)



# Reducing Items and Attributes

## ➔ Filter

→ Items



→ Attributes



## ➔ Aggregate

→ Items



→ Attributes



# Filter

elements are eliminated

What drives filters?

Any possible function that partitions a dataset into two sets

Bigger/smaller than x

Fold-change

Noisy/insignificant



# Dynamic Queries / Filters

coupling between encoding and interaction so that user can immediately see the results of an action

Queries: start with 0, add in elements

Filters: start with all, remove elements

*Approach depends on dataset size*

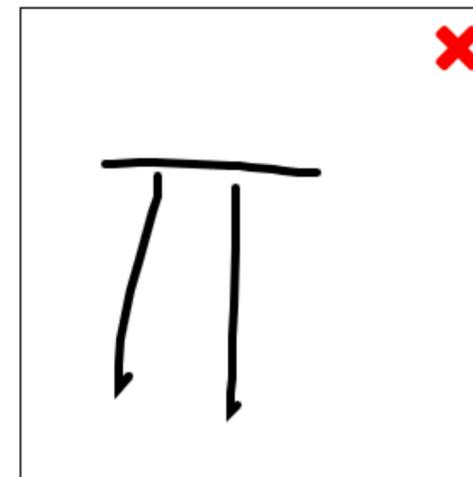
# Sketch-based Queries

Idea: we have a mental model of a pattern.

Let user sketch it!

Detexify

classify symbols



## Want a Mac app?

Lucky you. The Mac app is finally stable enough. See how it works on [Vimeo](#). Download the latest version [here](#).

*Restriction:* In addition to the LaTeX command the unlicensed version will copy a reminder to purchase a license to the clipboard when you select a symbol.

$\Pi$

Score: 0.05819911585627072  
`\Pi`  
mathmode

$\prod$

Score: 0.05906024733857653  
`\prod`  
mathmode

$\Uppsi$

Score: 0.06257830365544022  
`\usepackage{ upgreek }`  
`\Uppi`  
mathmode

$\lceil$

Score: 0.06859782837342329  
`\usepackage{ stmaryrd }`  
`\llceil`  
mathmode

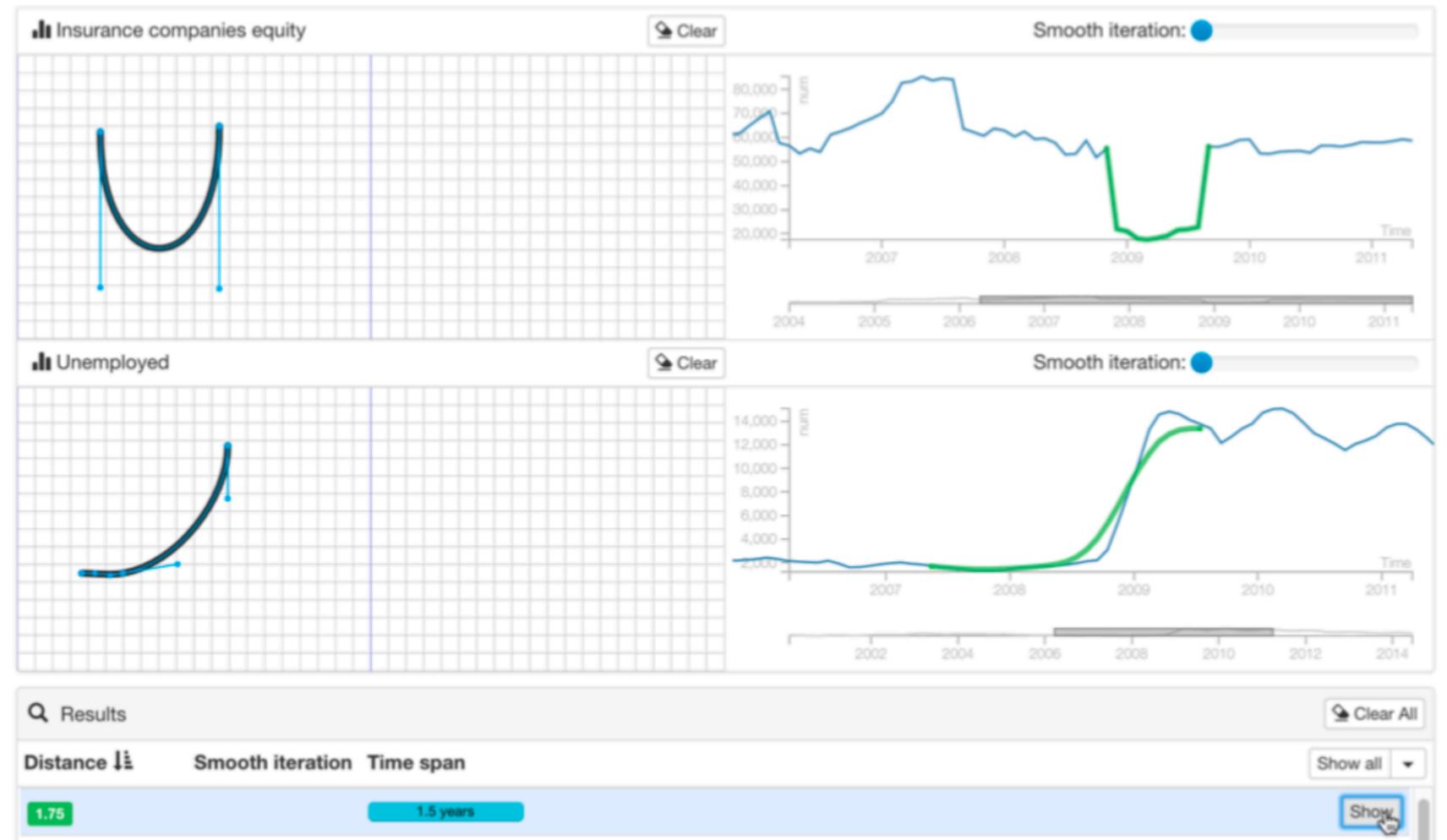
$\pi$

Score: 0.07635285017928727  
`\pi`  
mathmode

The symbol is not in the list? [Show more](#)

# Sketch-based Queries

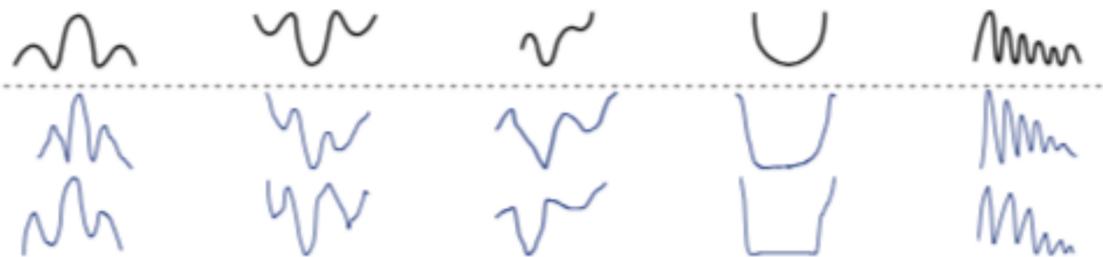
## Time Series



### Queries

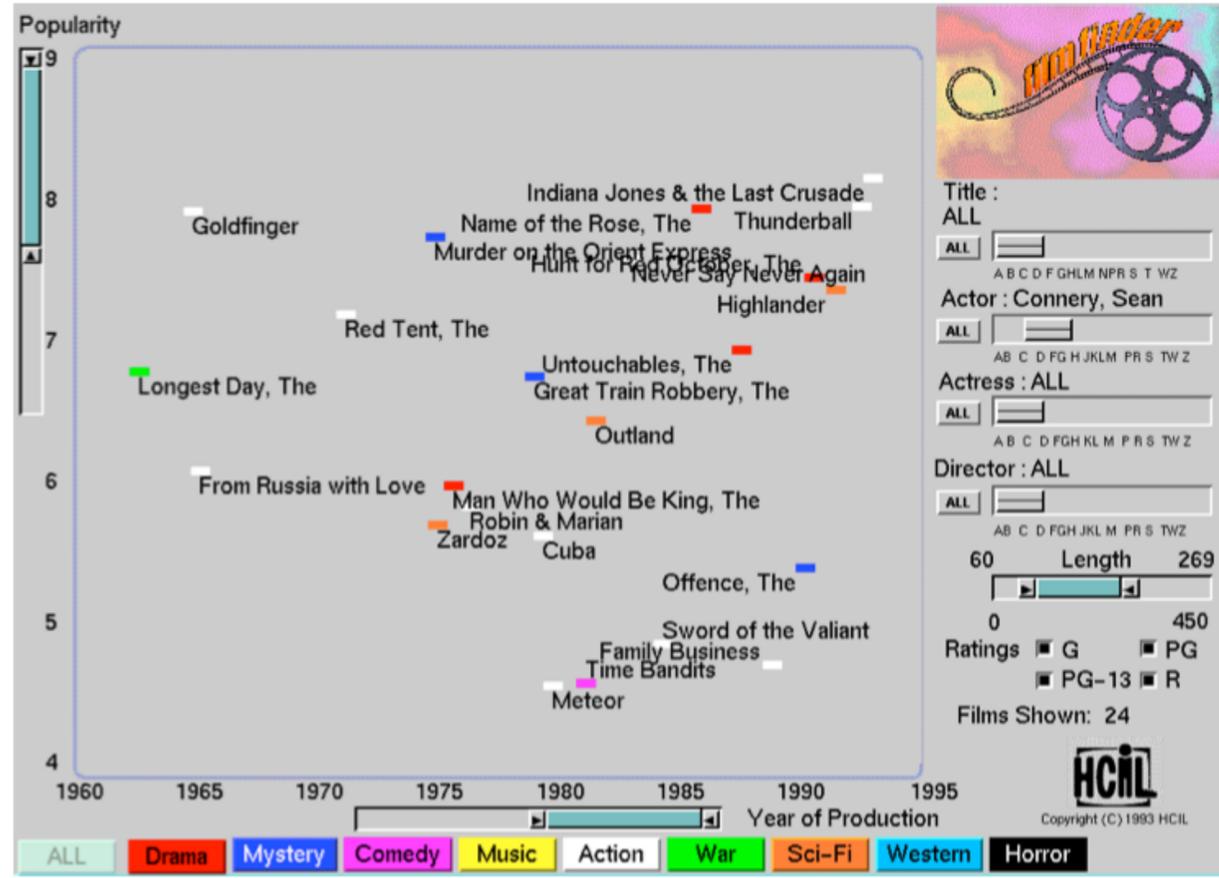
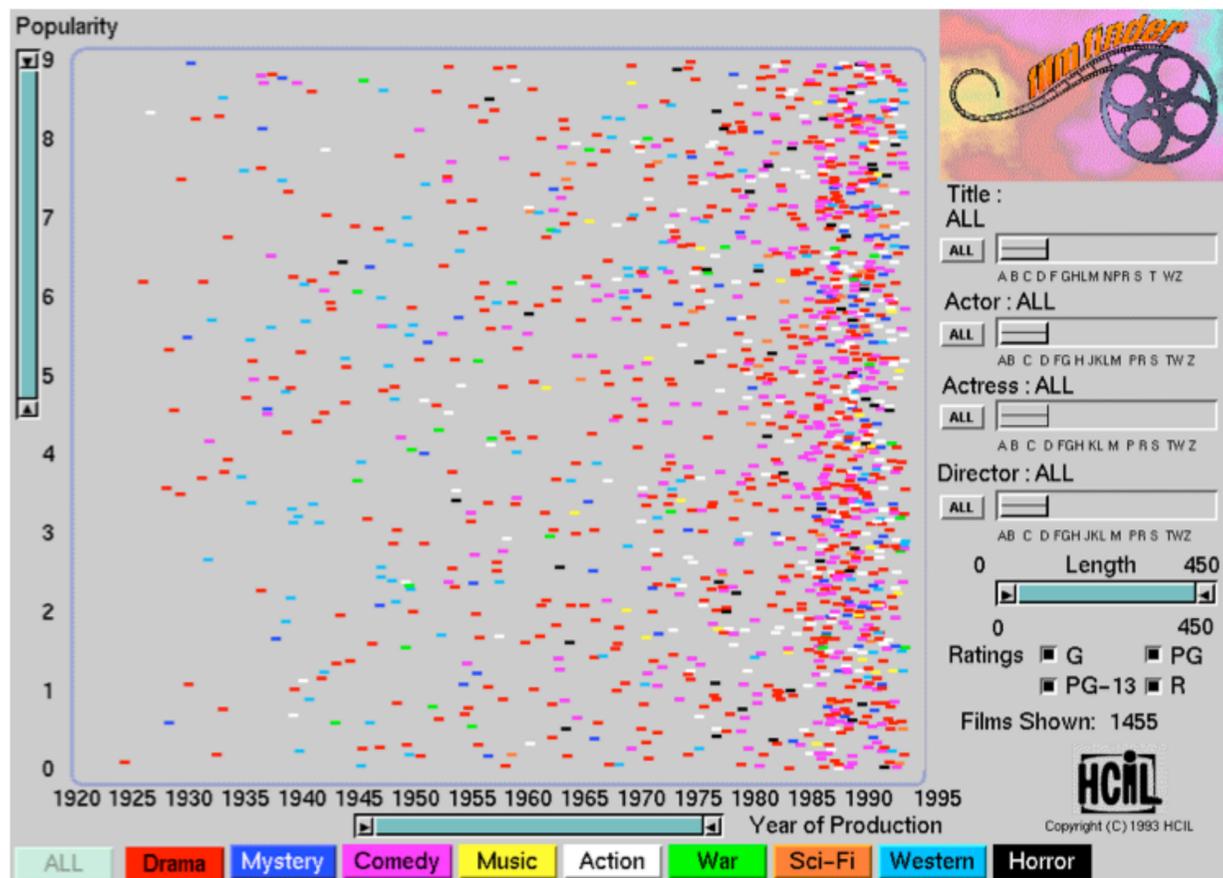
### Sketch Samples

Typical sketches preserve key perceptual features but have local distortions.



<https://www.youtube.com/watch?v=4YQTuUuIFbl>

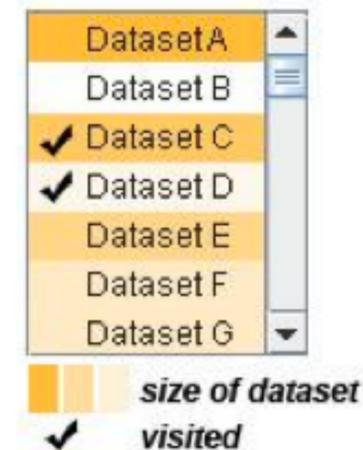
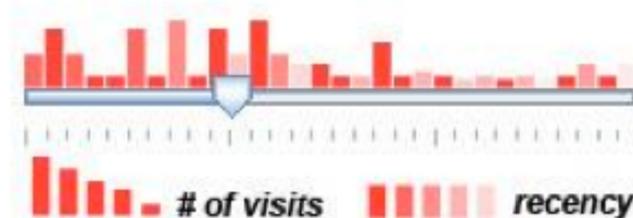
# ITEM FILTERING



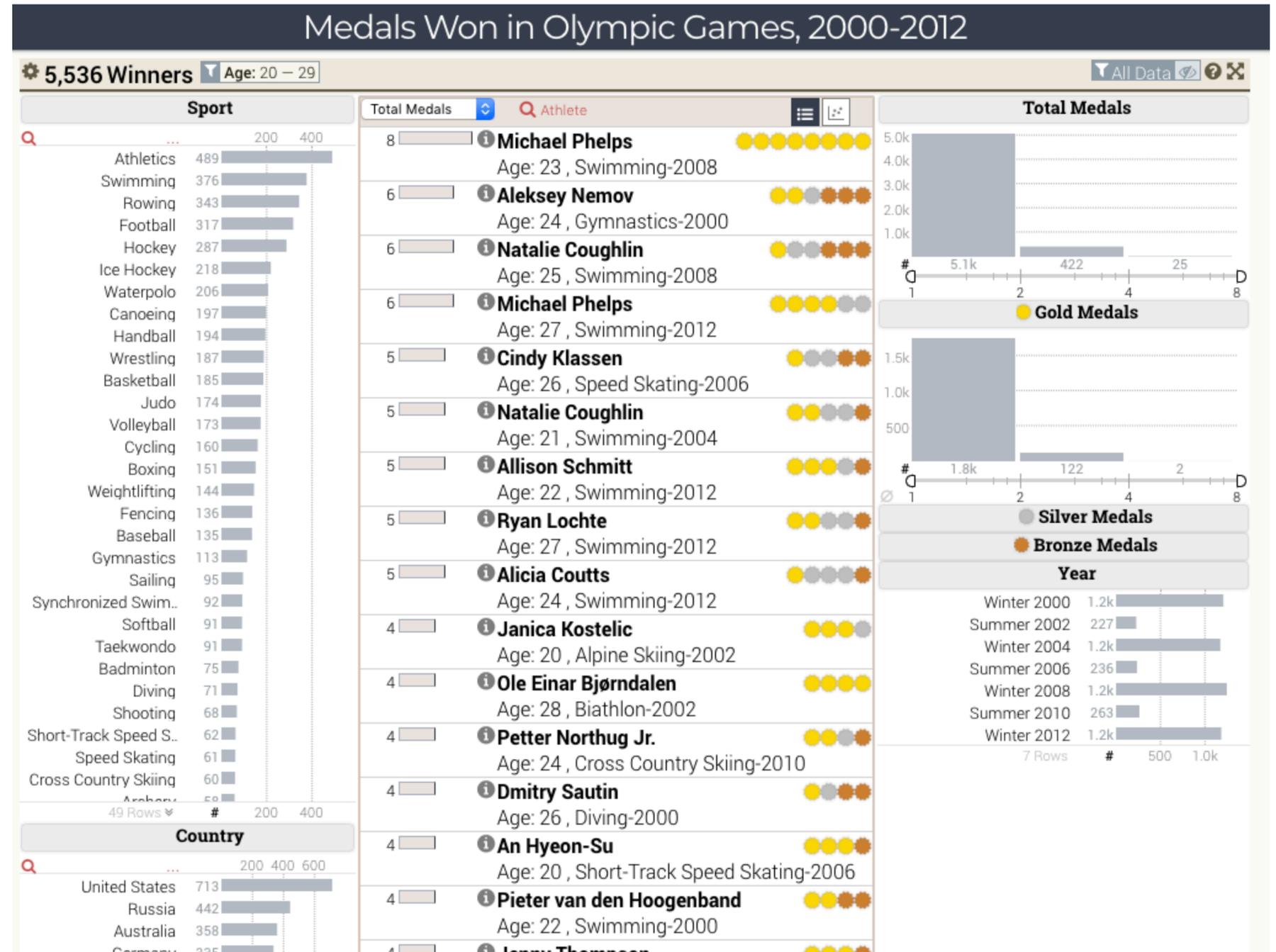
# Scented Widgets

**information scent:** user's (imperfect) perception of data

**GOAL:** lower the cost of information foraging through better cues



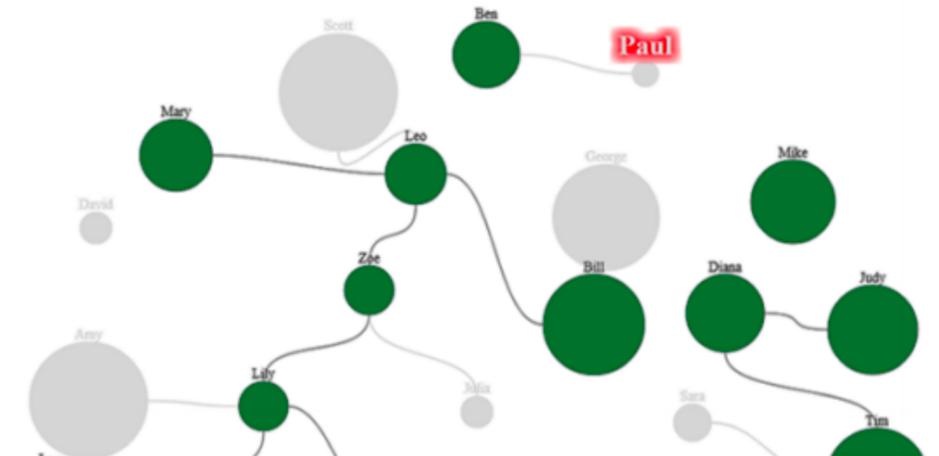
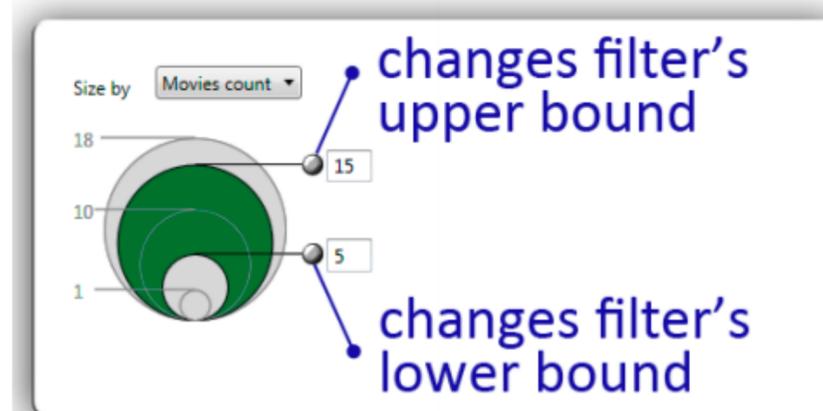
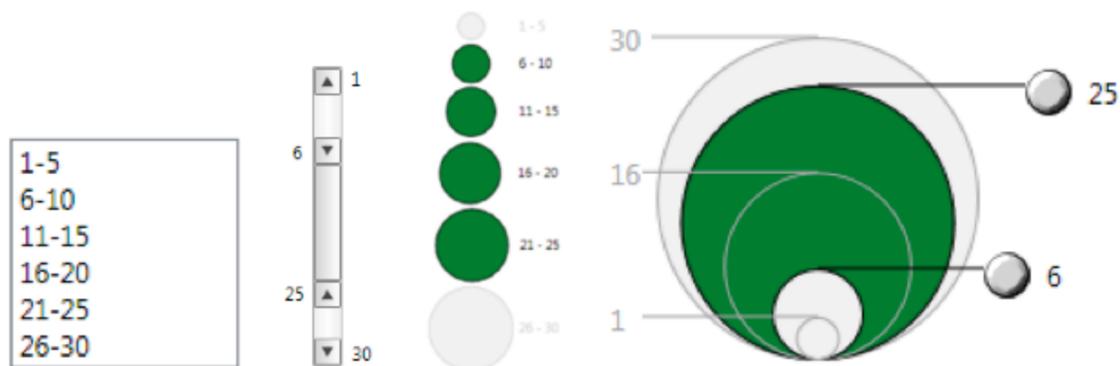
# Item Filtering with Scented Widgets



# Interactive Legends

Controls combining the visual representation of static legends with interaction mechanisms of widgets

Define and control visual display together

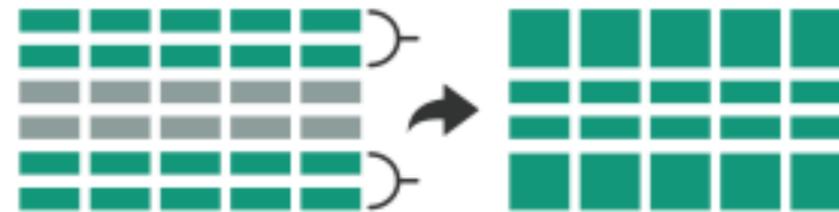


# Aggregation

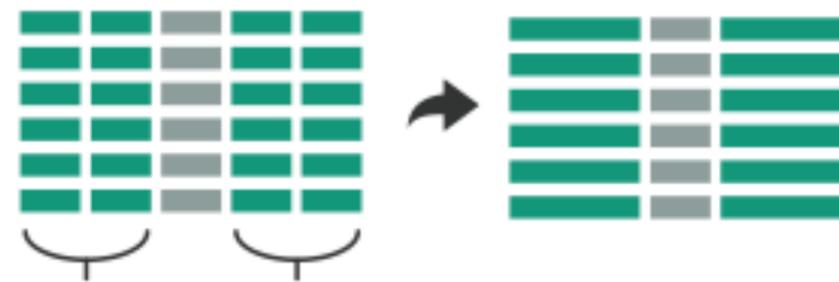
# Aggregate

a group of elements is represented by a (typically smaller) number of derived elements

→ Items

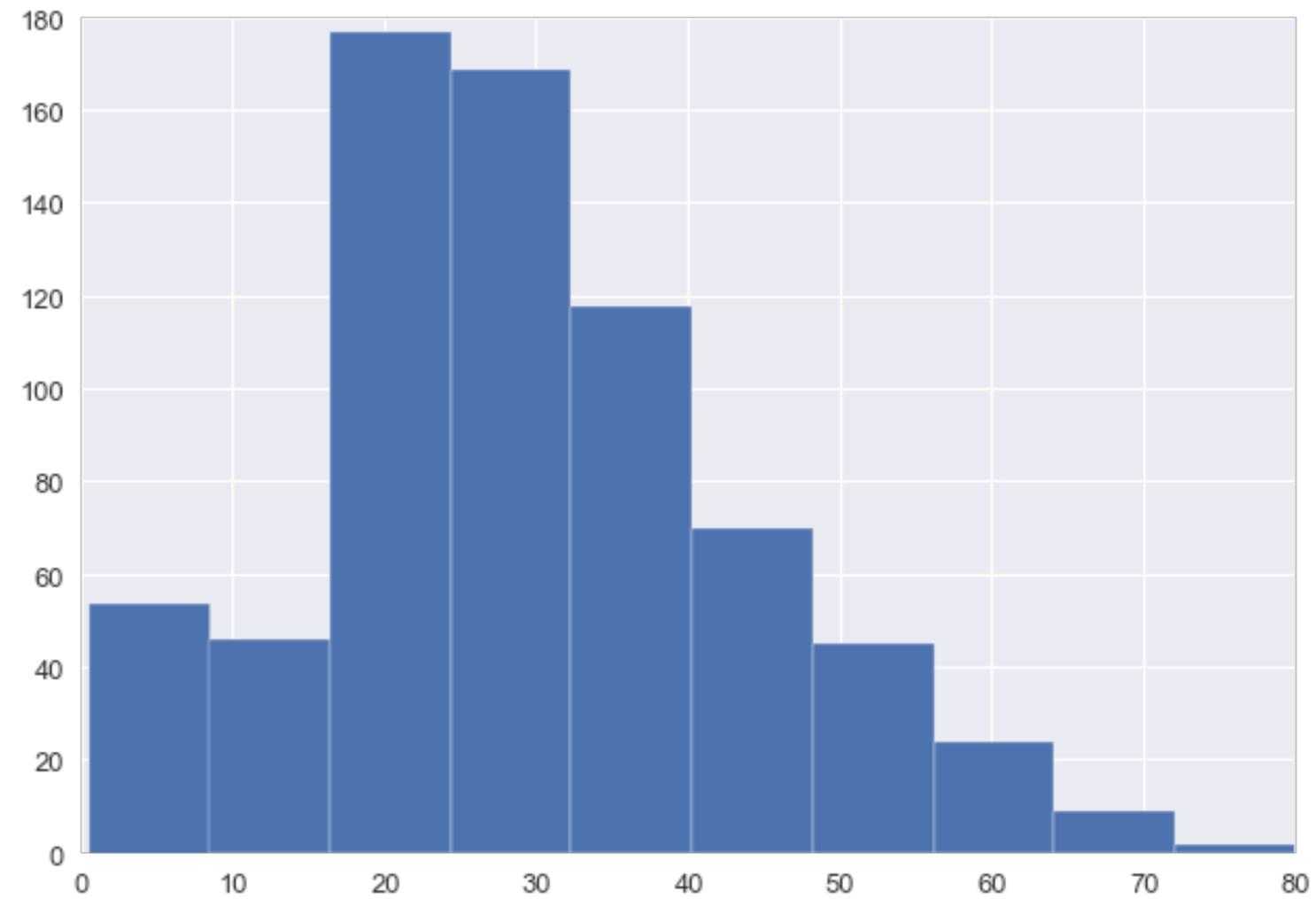


→ Attributes

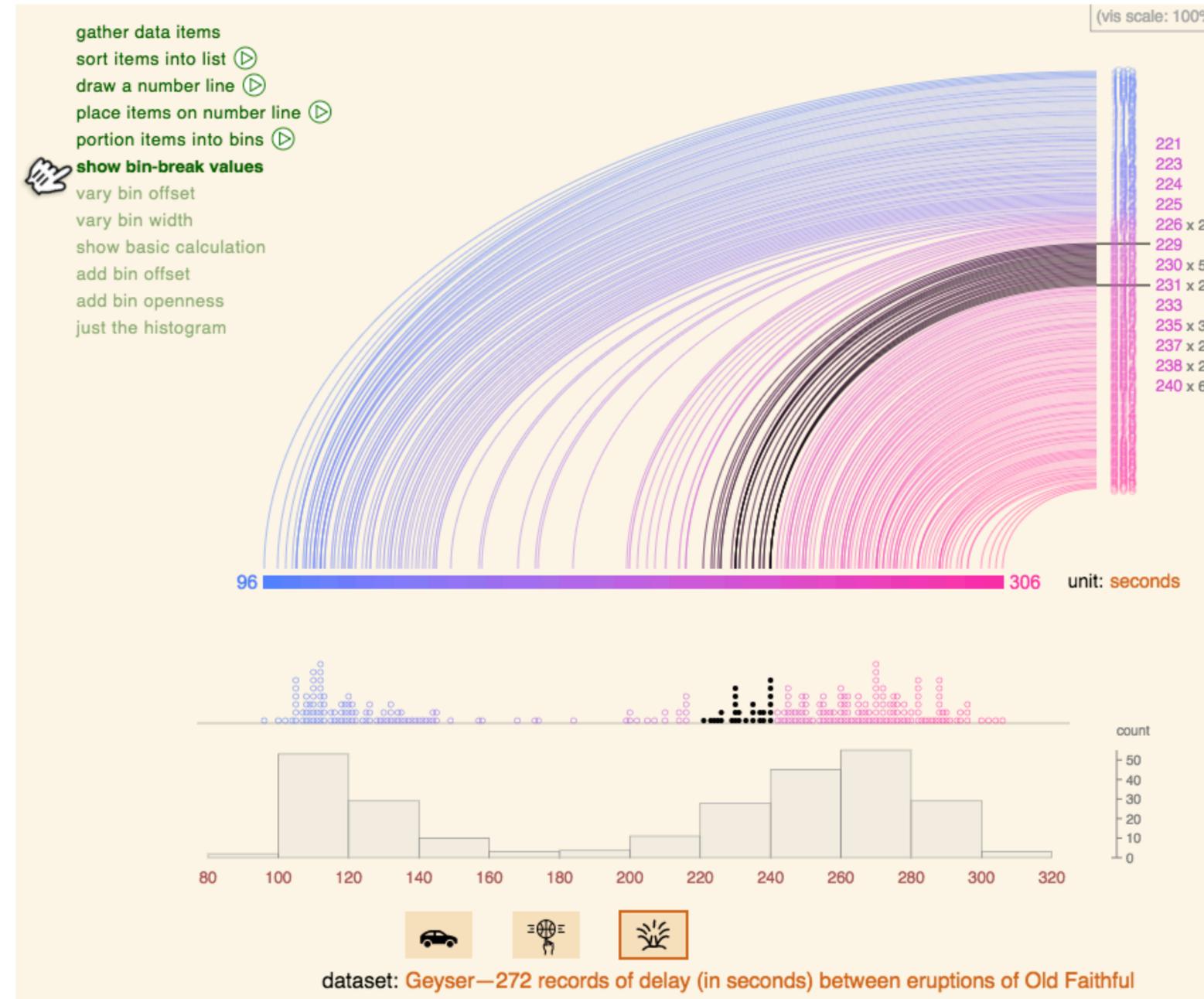


Why Aggregate?

# What's a histogram?



# Histograms Explained



<http://tinlizzie.org/histograms/>

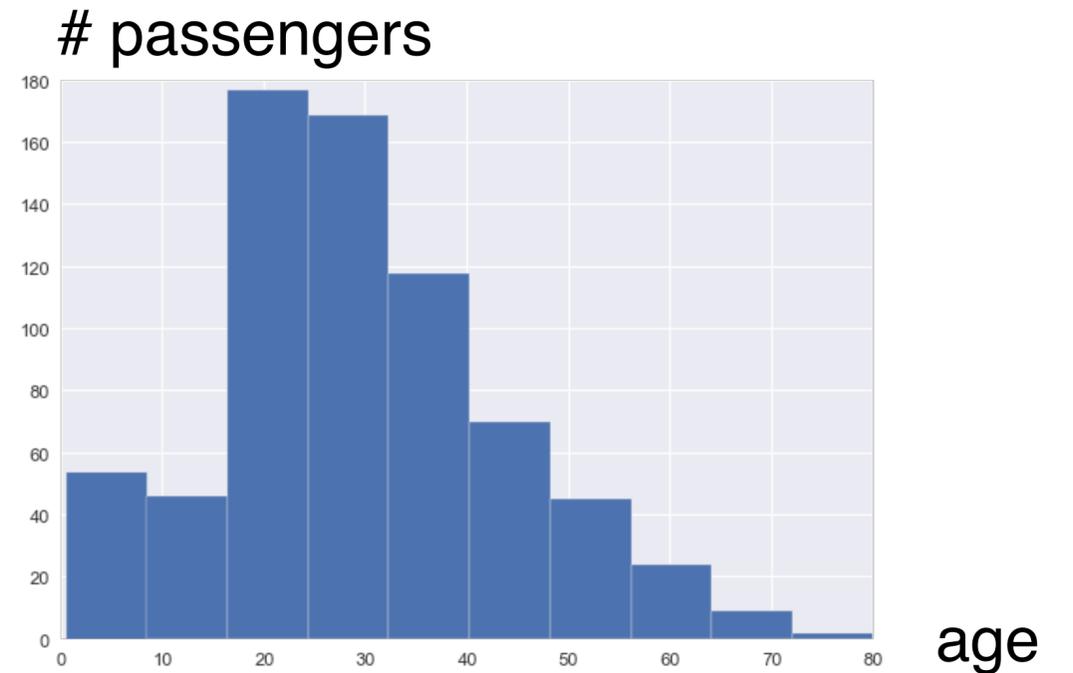
# Histogram

Good #bins hard to predict  
make interactive!

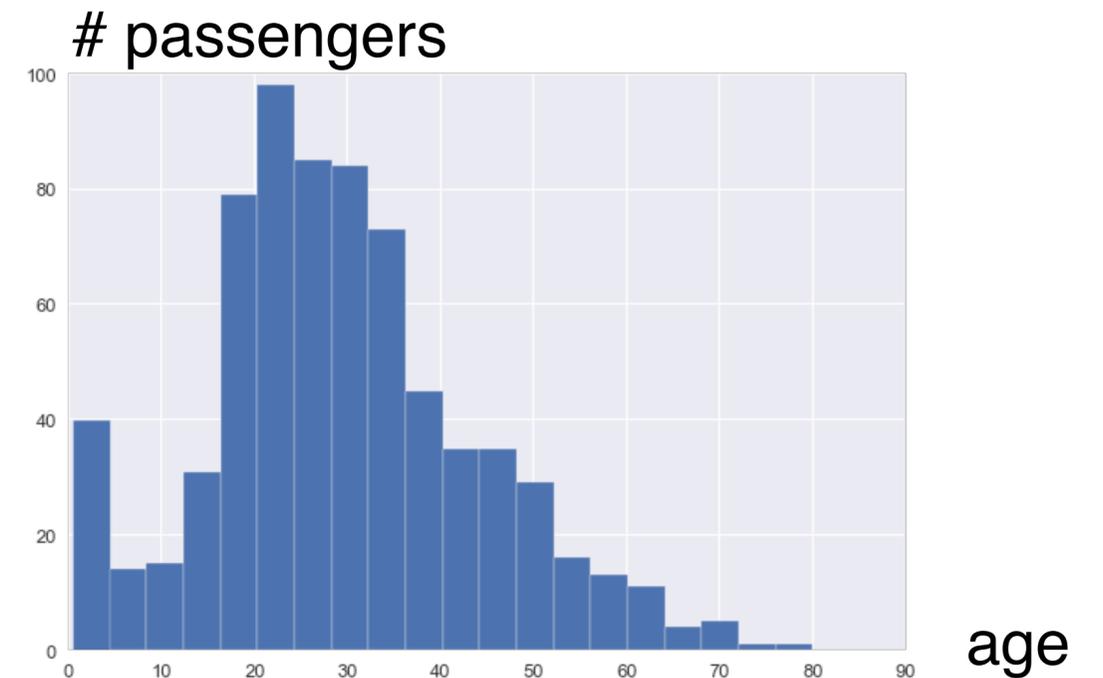
rules of thumb:

$$\#bins = \sqrt{n}$$

$$\#bins = \log_2(n) + 1$$

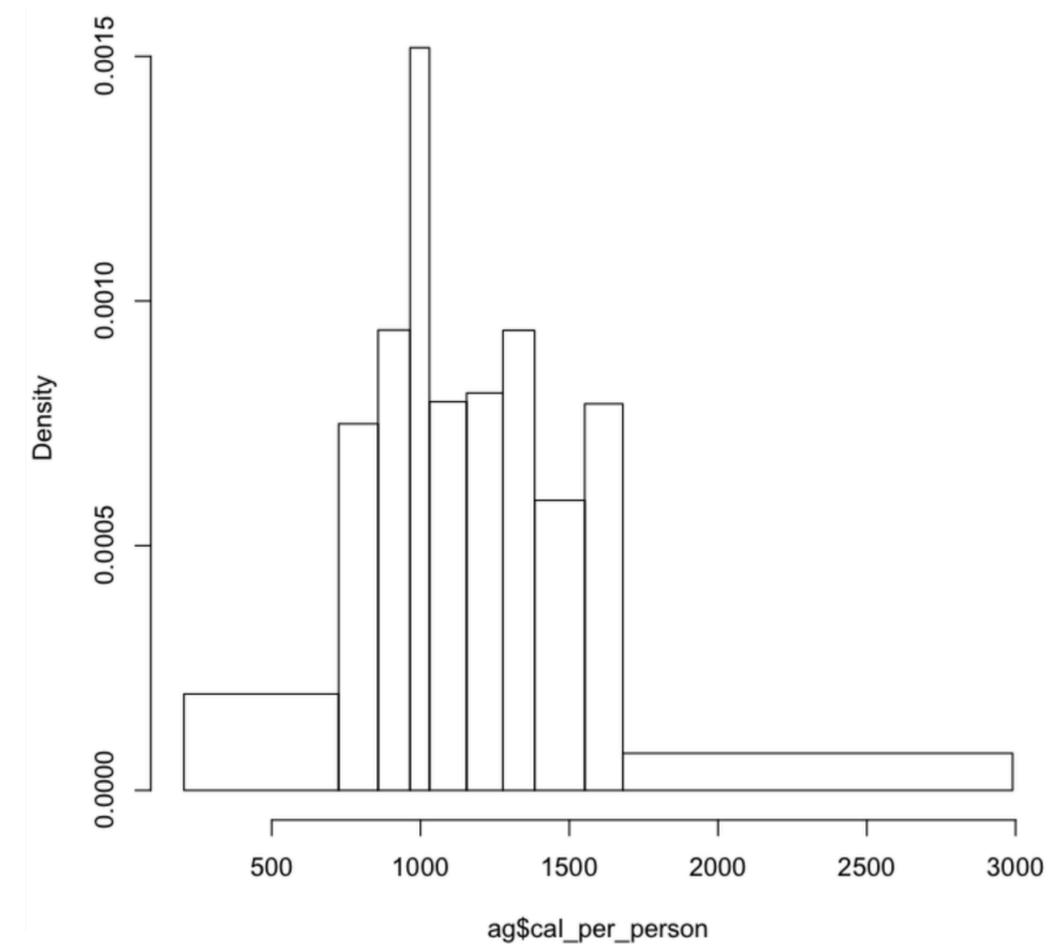
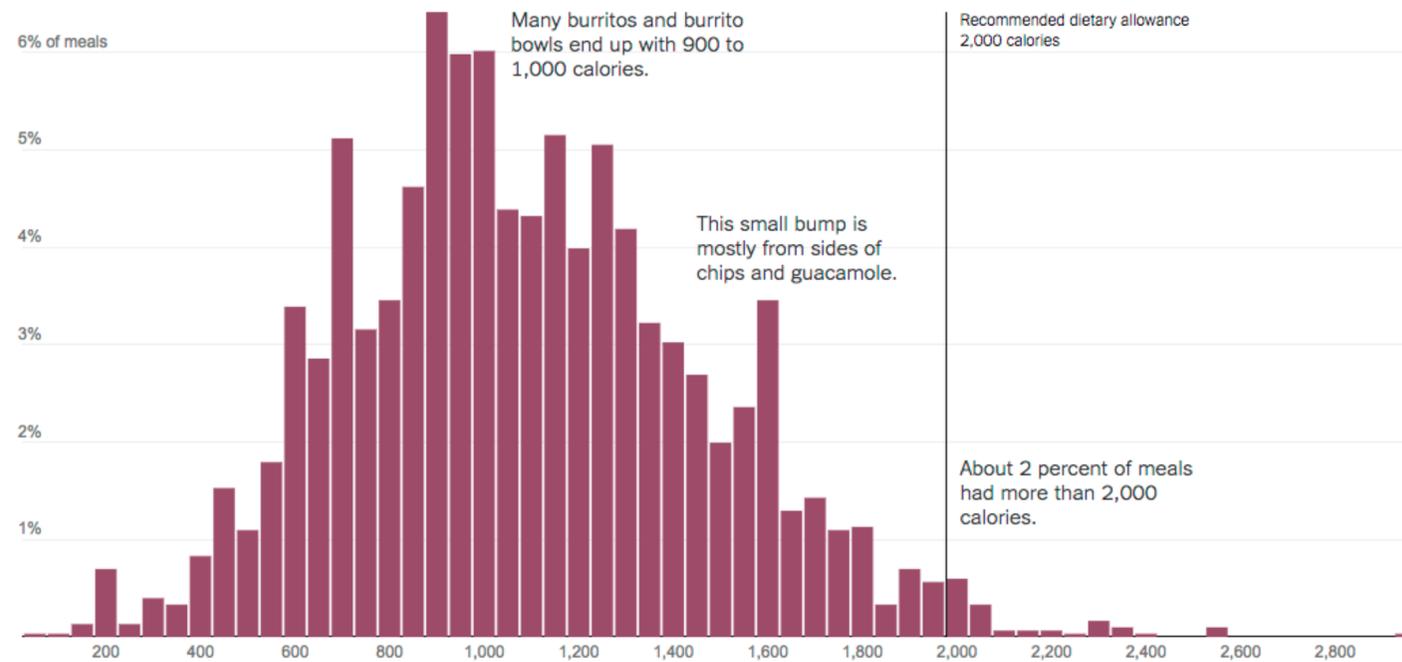


10 Bins



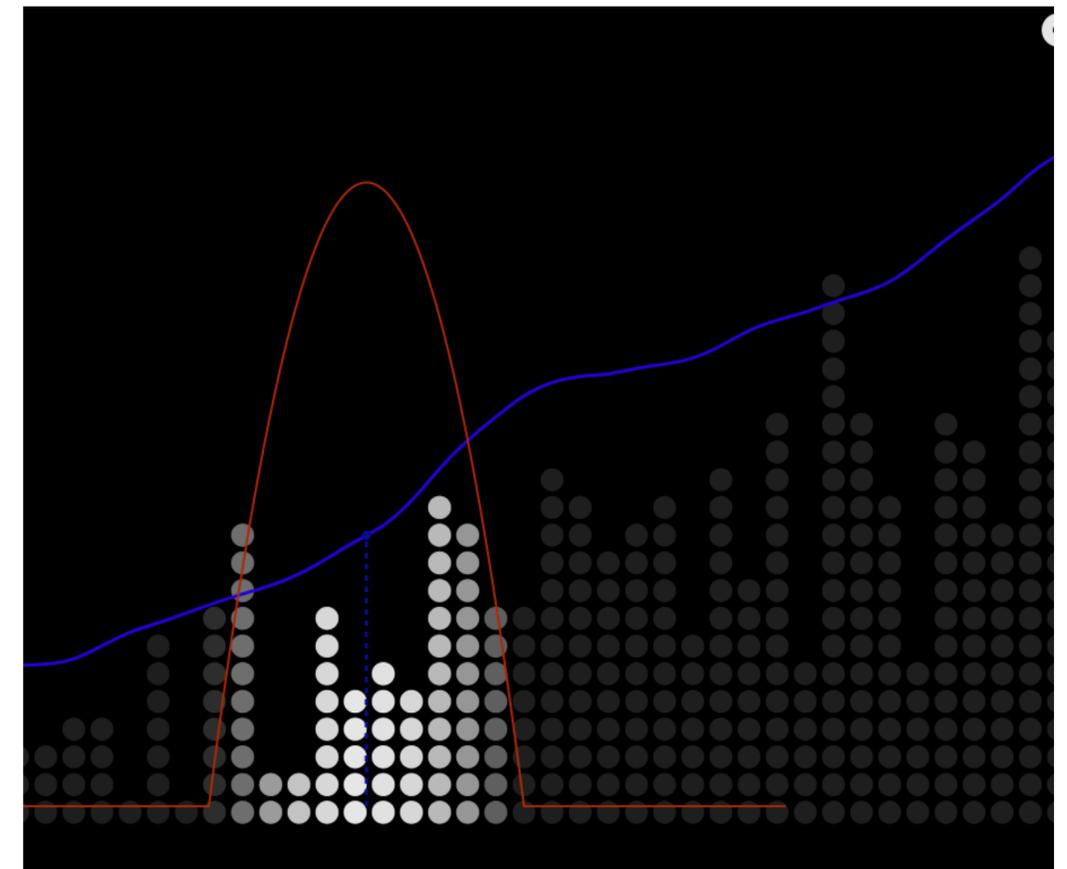
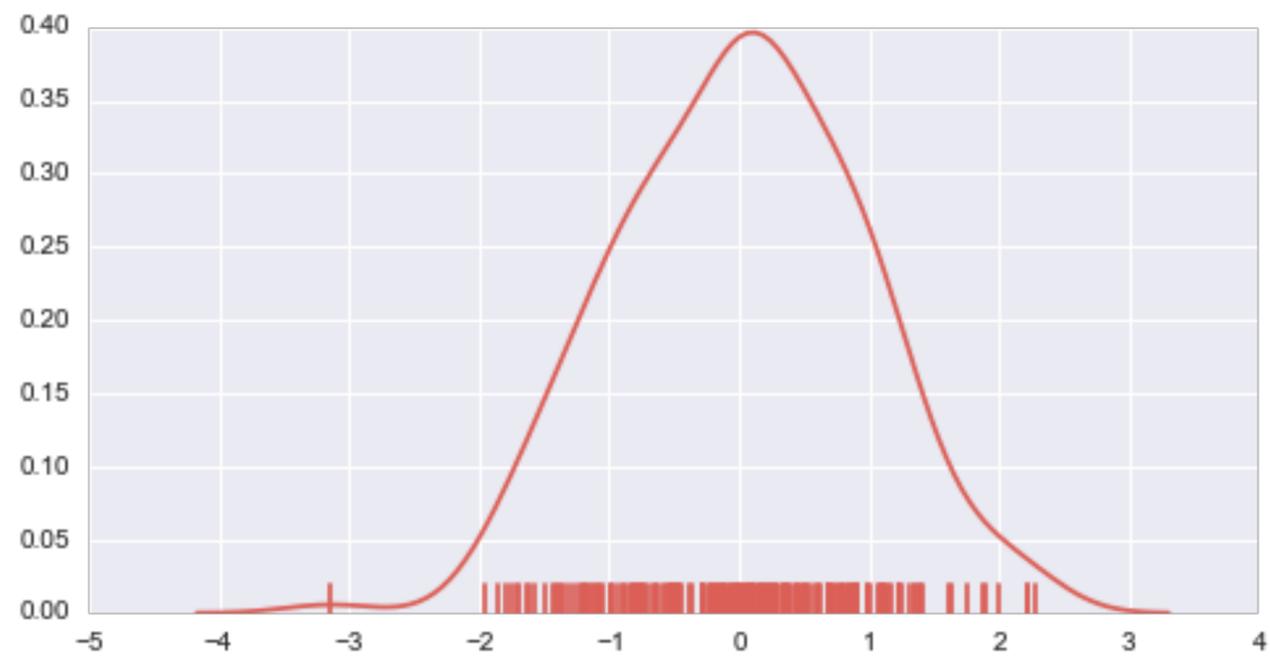
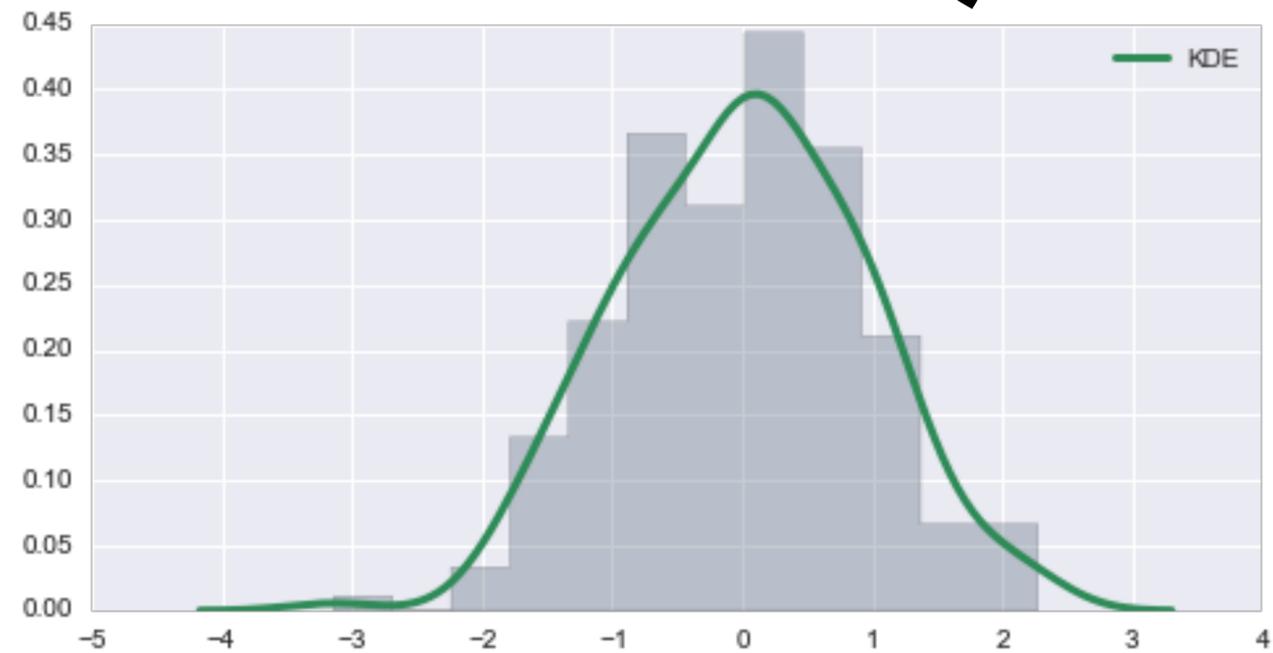
20 Bins

# Unequal Bin Width



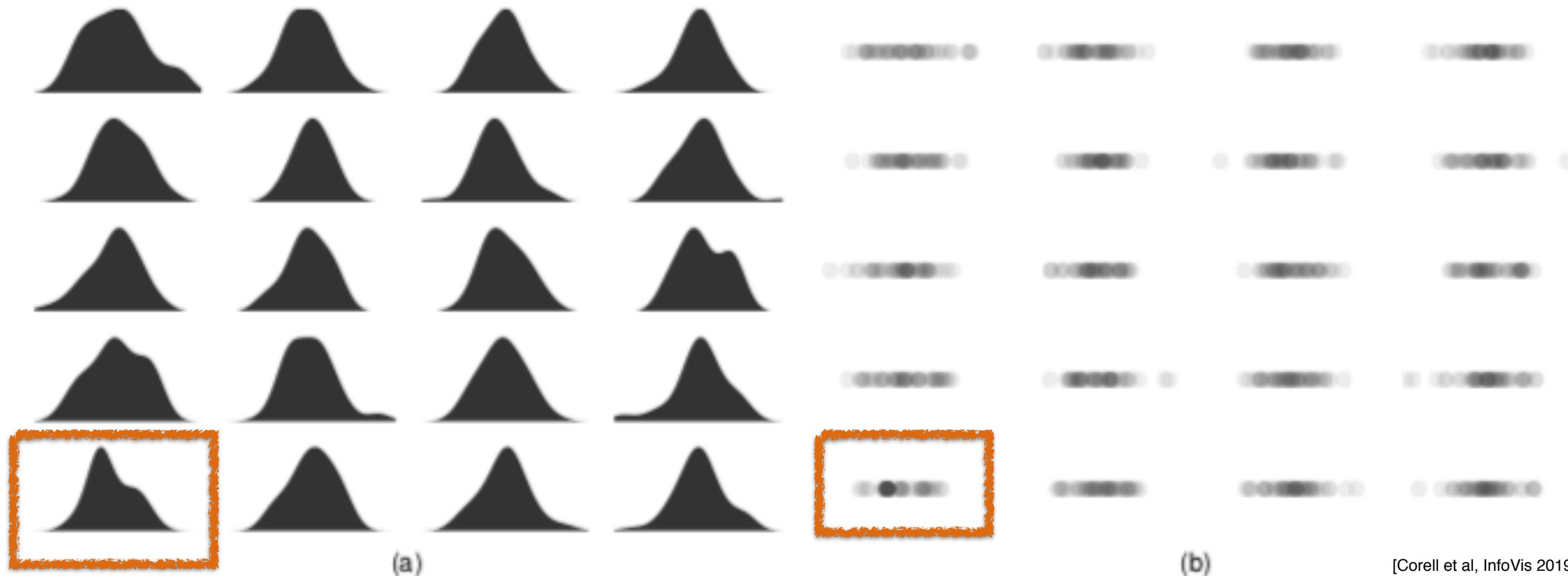
Can be useful if data is much sparser in some areas than others  
Show density as area, not height.

# Density Plots (Kernel Density Estimation)



# One of these things is not like the other...

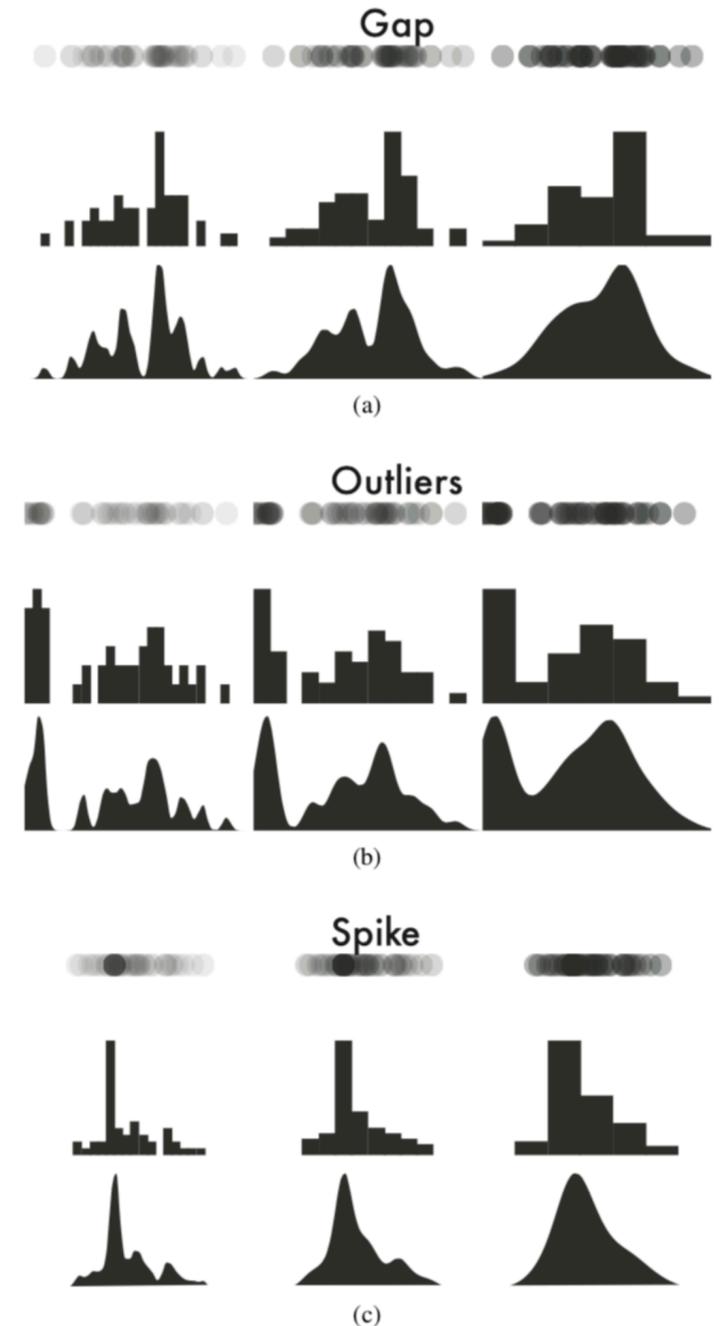
19 charts are random samples from a gaussian.  
1 chart has 20% of samples with identical value



# Detecting Data Flaws

Tricky with aggregate  
visualization

Bin size / kernel type /  
bandwidth / visualization  
choice all affect different  
situations



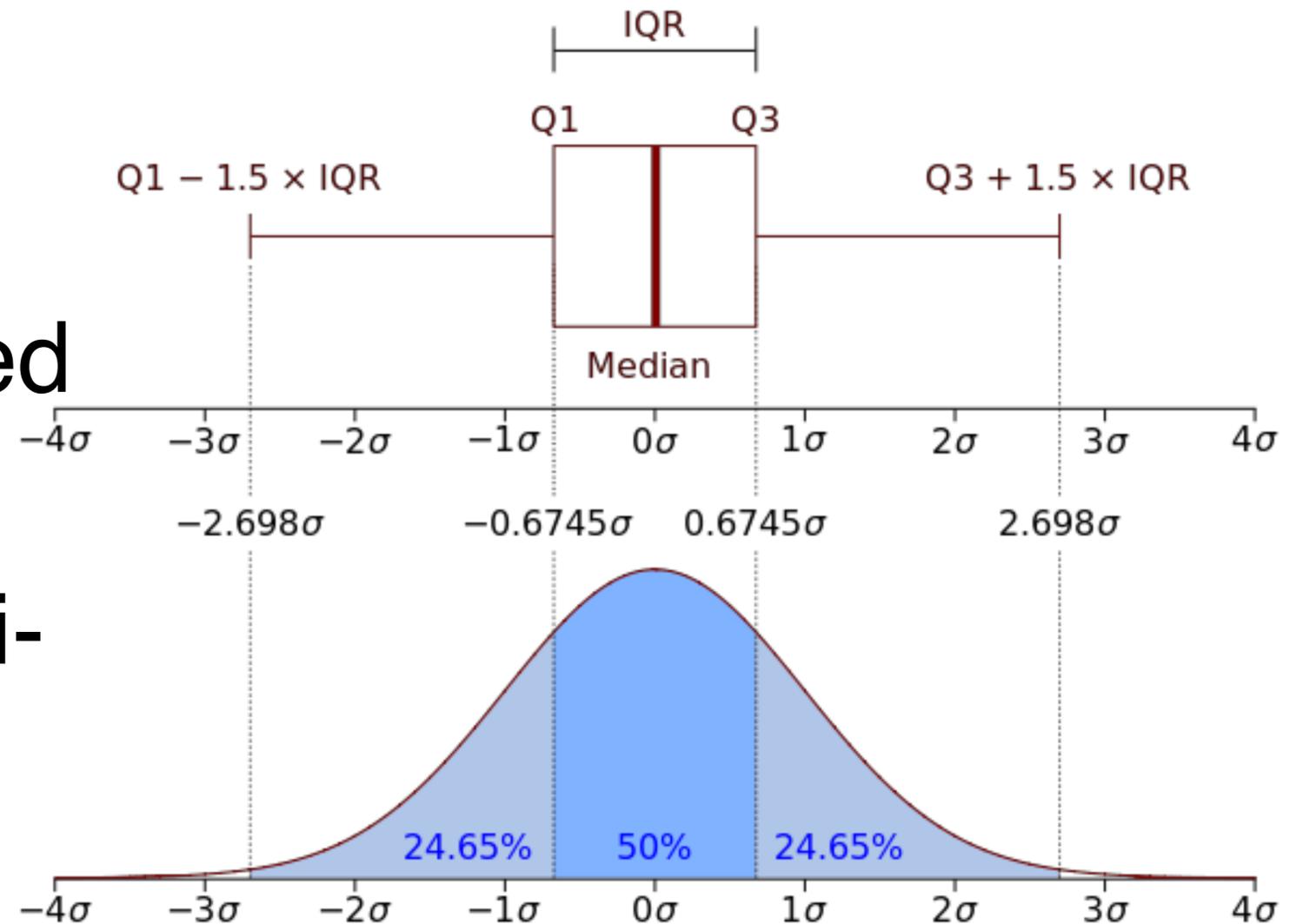
# Box Plots

aka Box-and-Whisker Plot

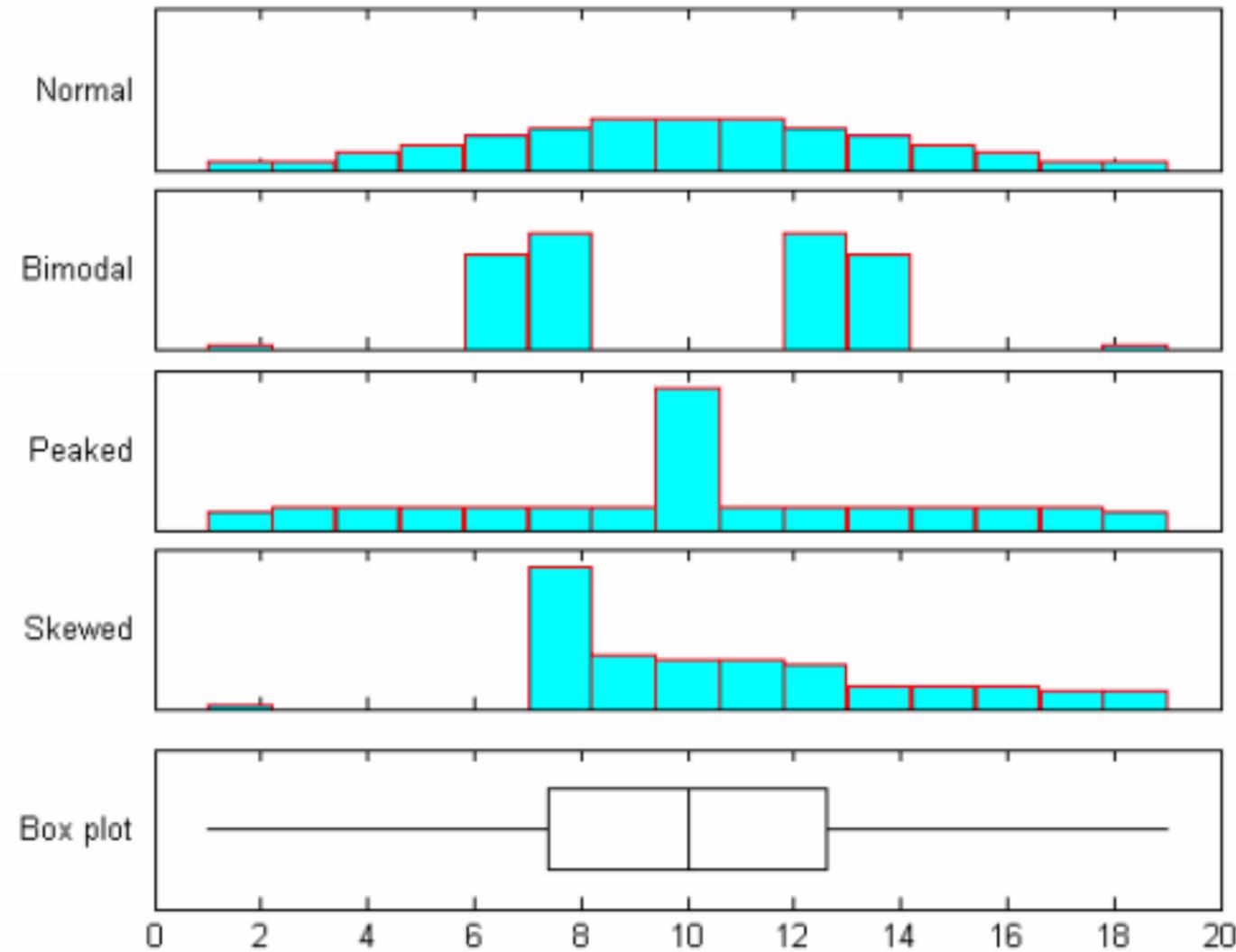
Show outliers as points!

Bad for non-normal distributed data

Especially bad for bi- or multi-modal distributions



# One Boxplot, Four Distributions



*Figure 1: Histograms and box plot: four samples each of size 100*

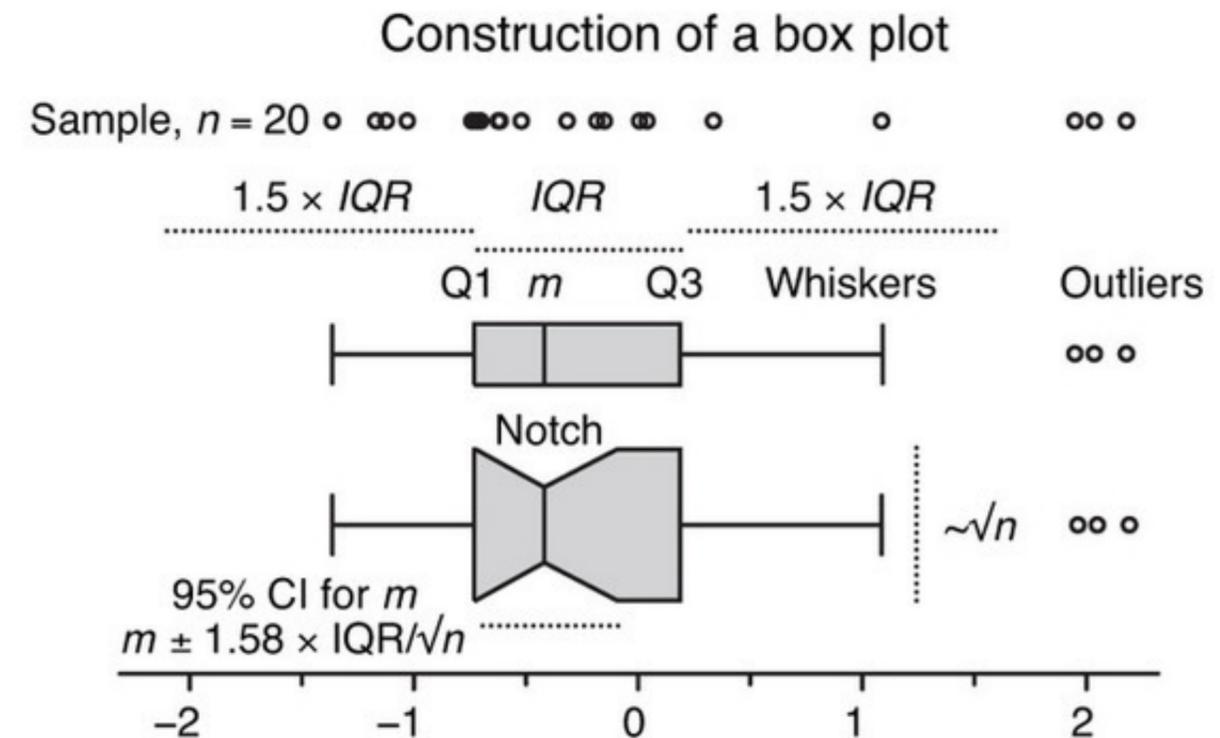
# Notched Box Plots

Notch shows

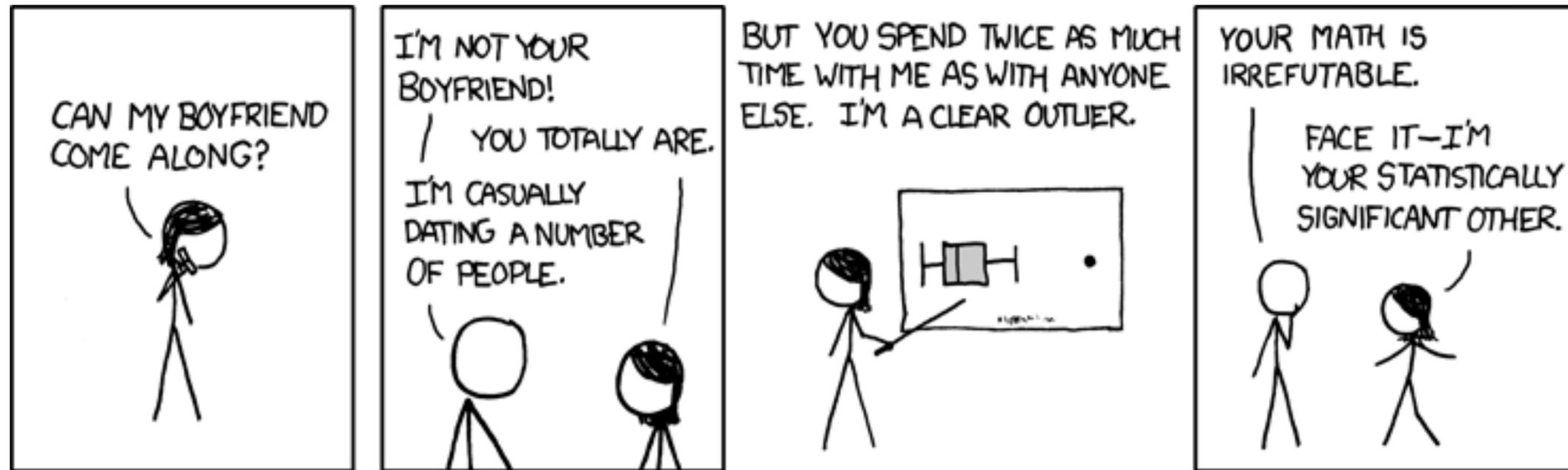
$m \pm 1.58 \times IQR/\sqrt{n}$

-> 95% Confidence Intervall

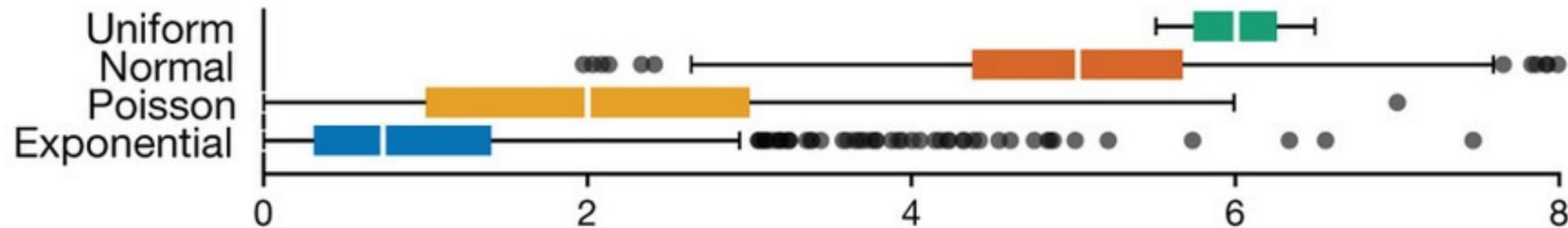
A guide to statistical significance.



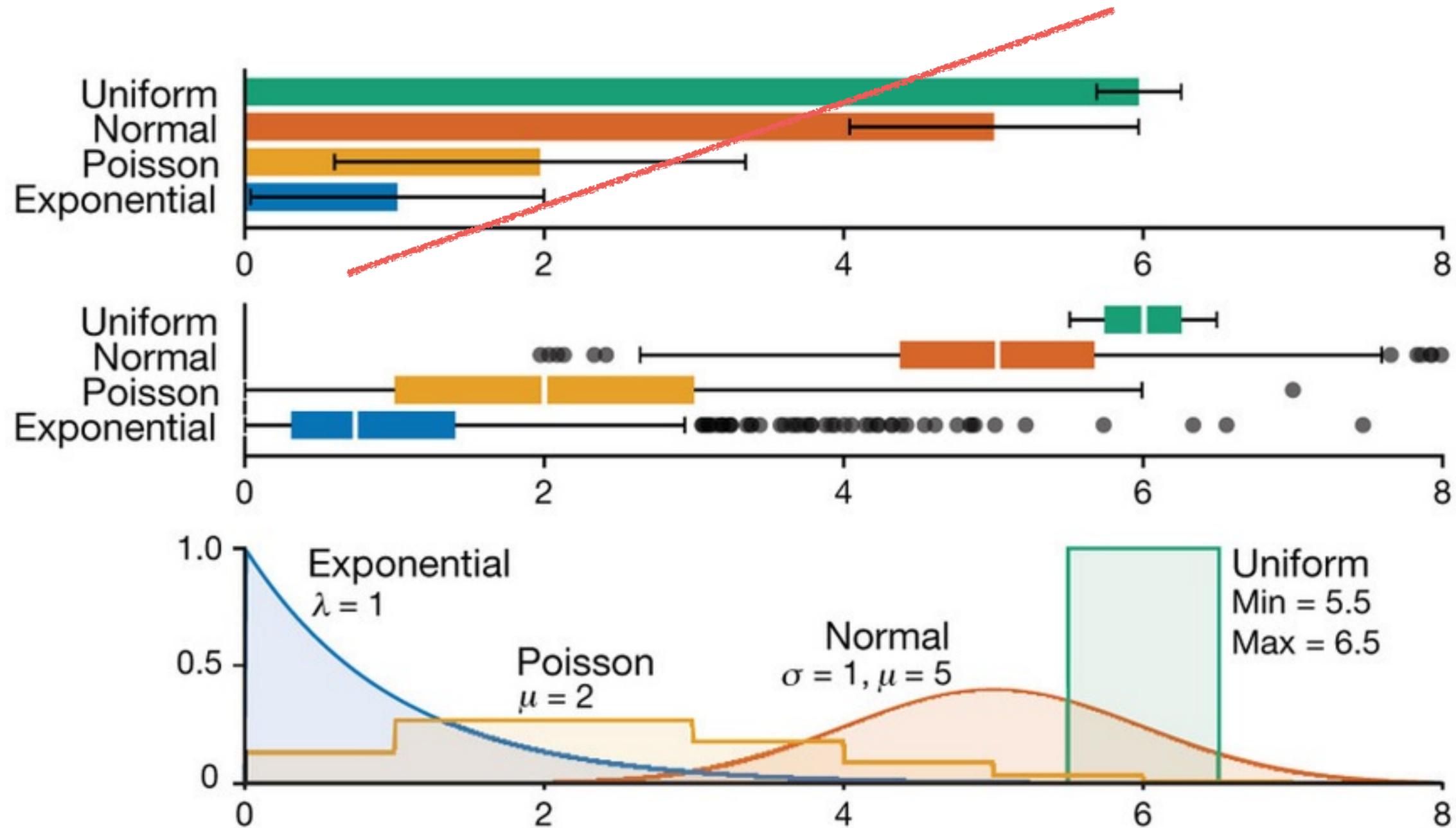
# Box(and Whisker) Plots



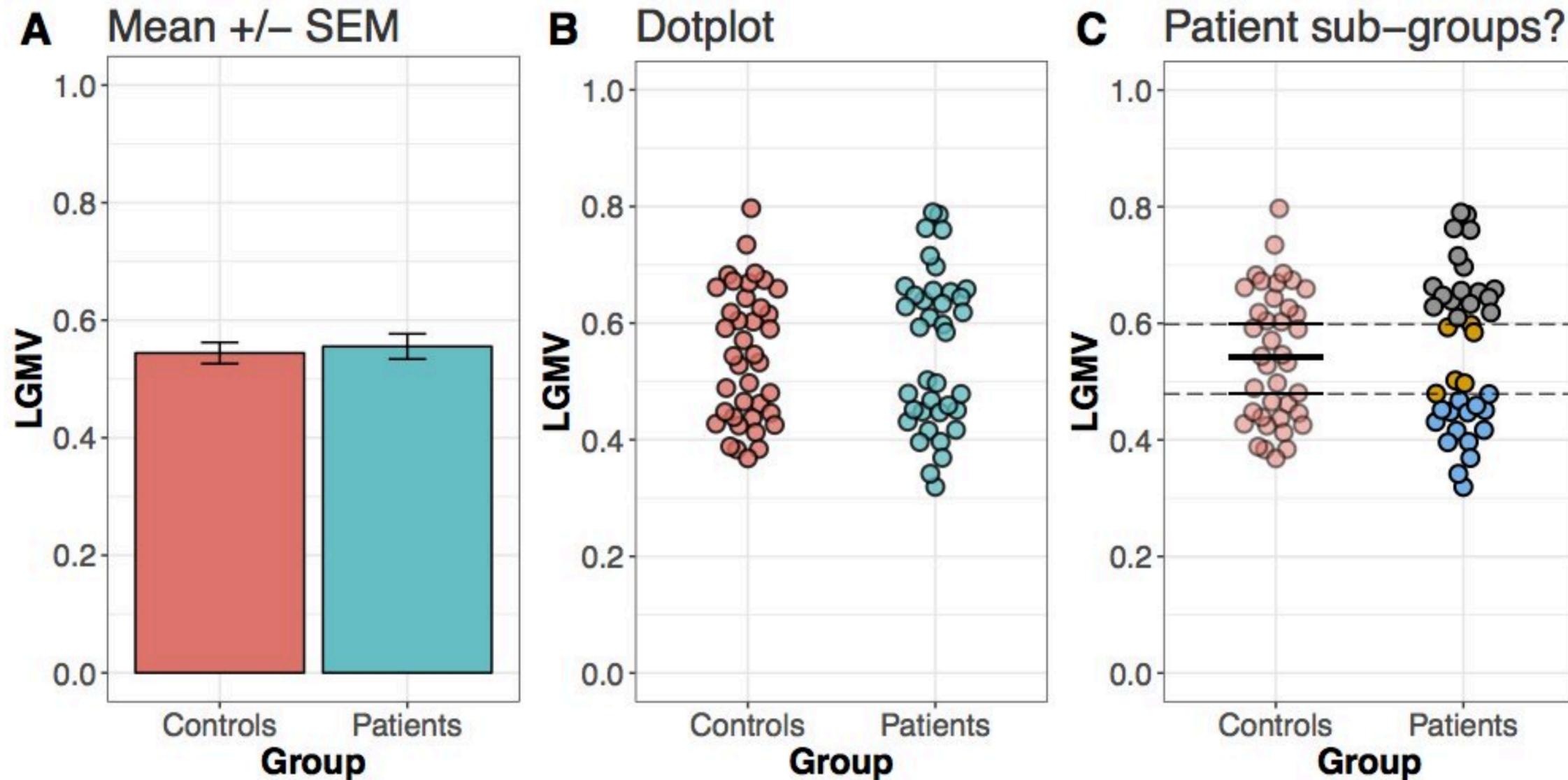
<http://xkcd.com/539/>



# Comparison

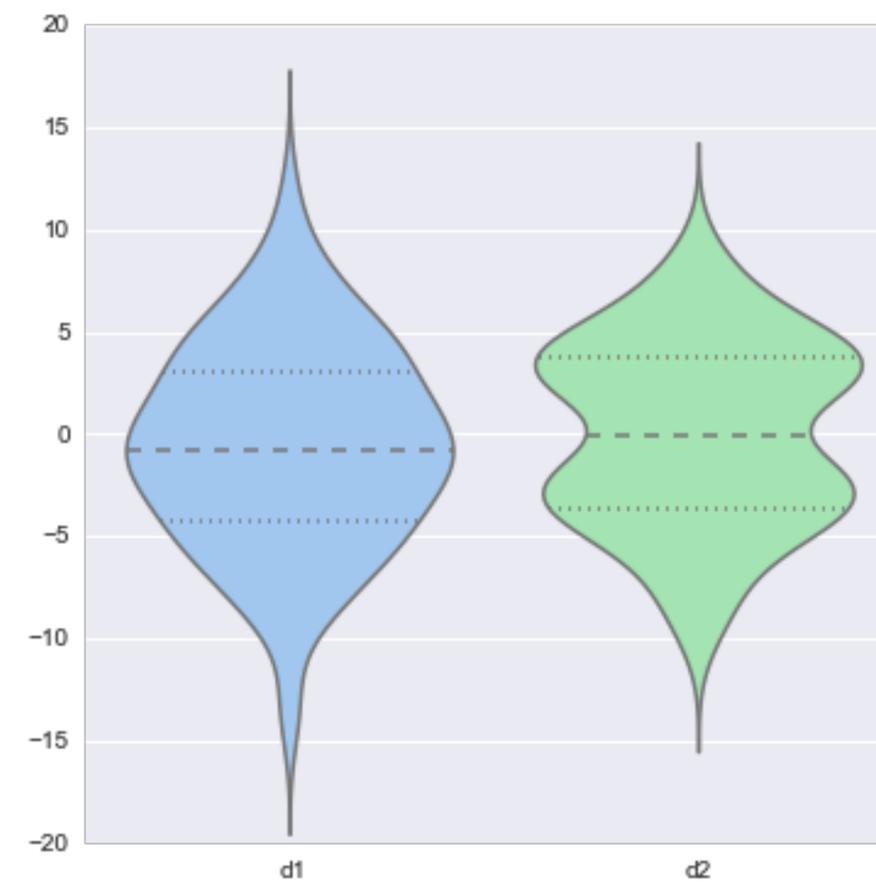
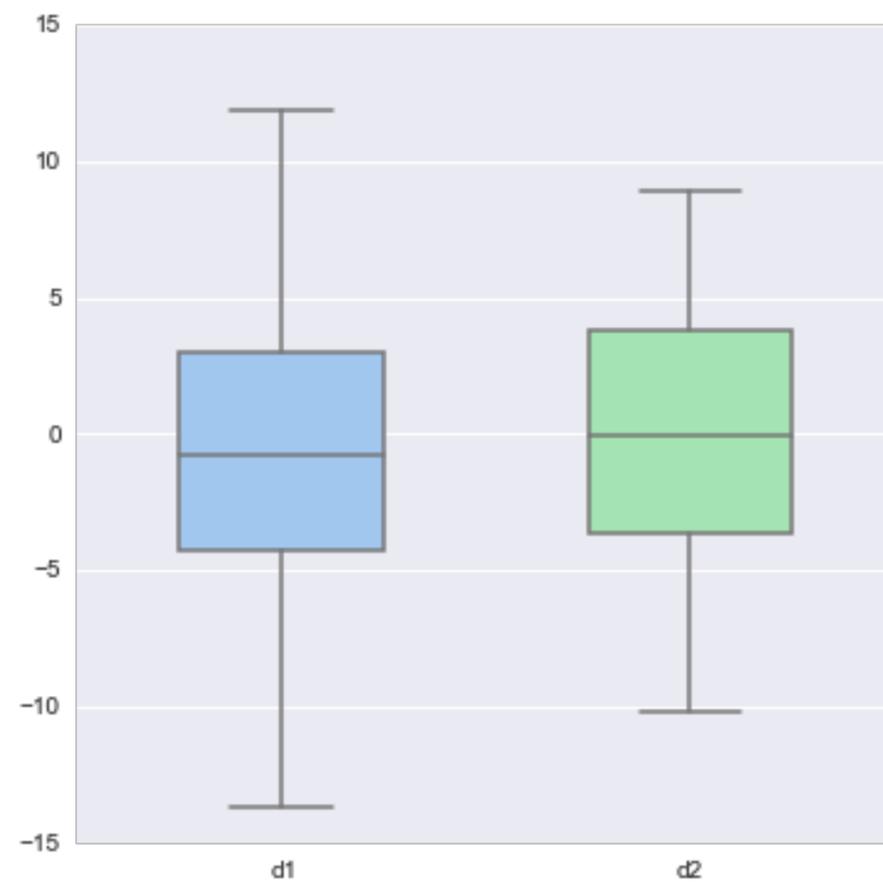


# Bar Charts vs Dot Plots



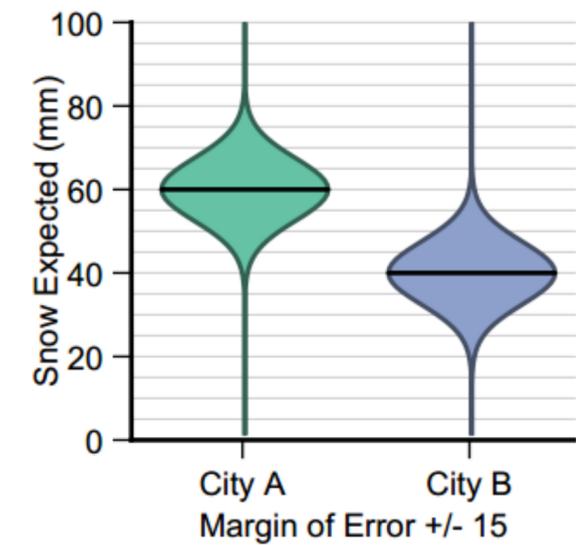
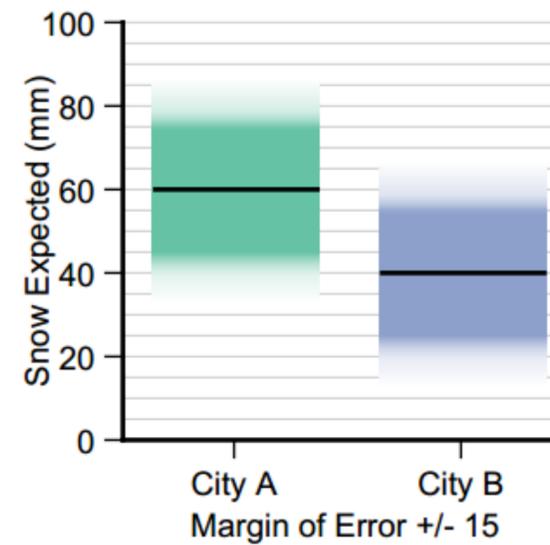
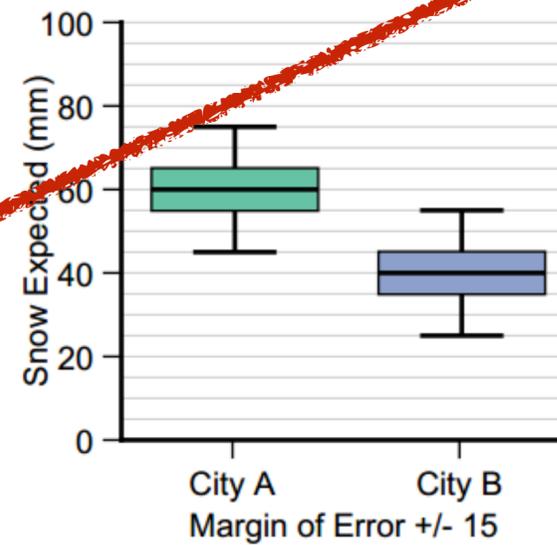
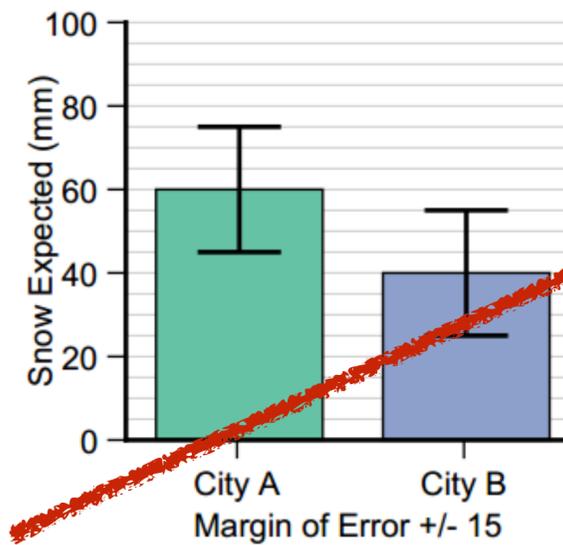
# Violin Plot

= Box Plot + Probability Density Function



# Showing Expected Values & Uncertainty

NOT a distribution!

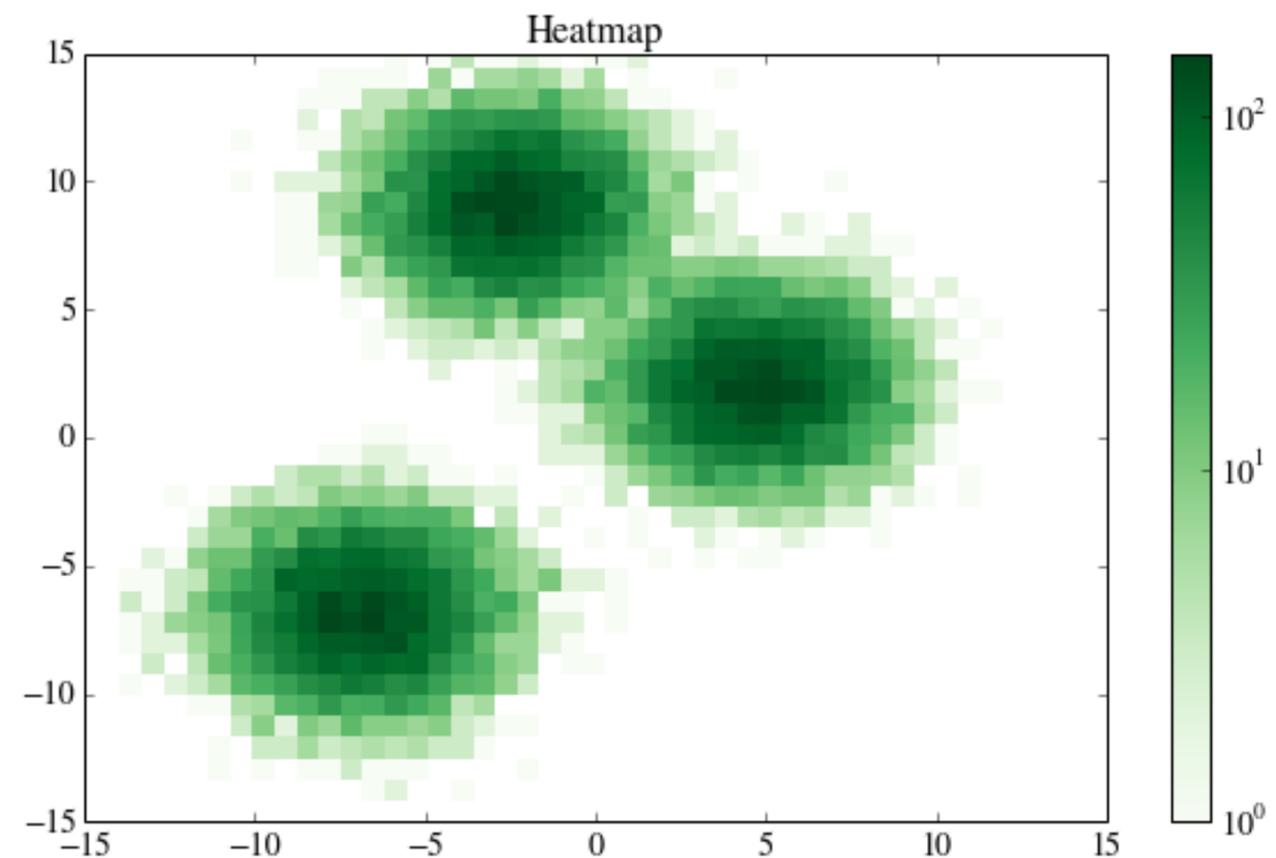
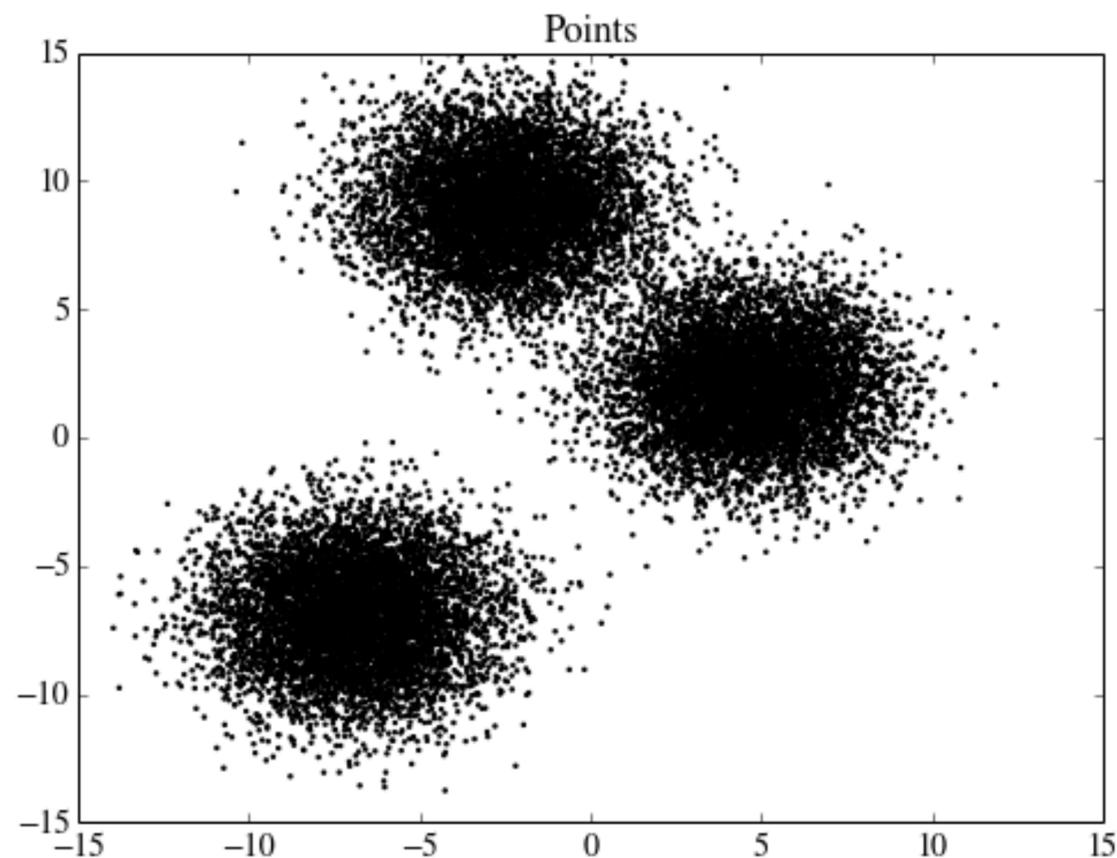


Error Bars Considered Harmful:  
Exploring Alternate Encodings for Mean and Error  
Michael Correll, and Michael Gleicher

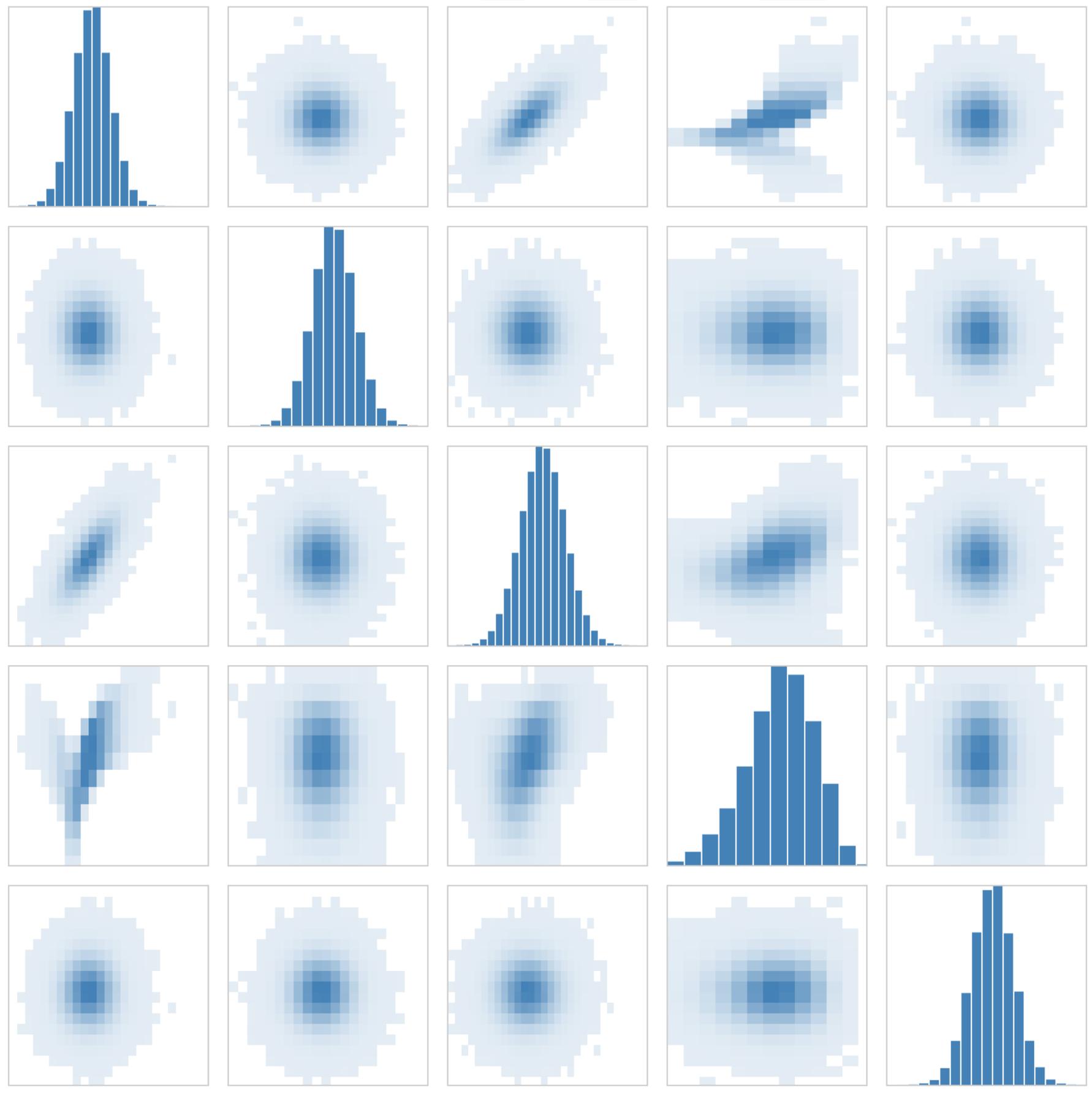
# Heat Maps

binning of scatterplots

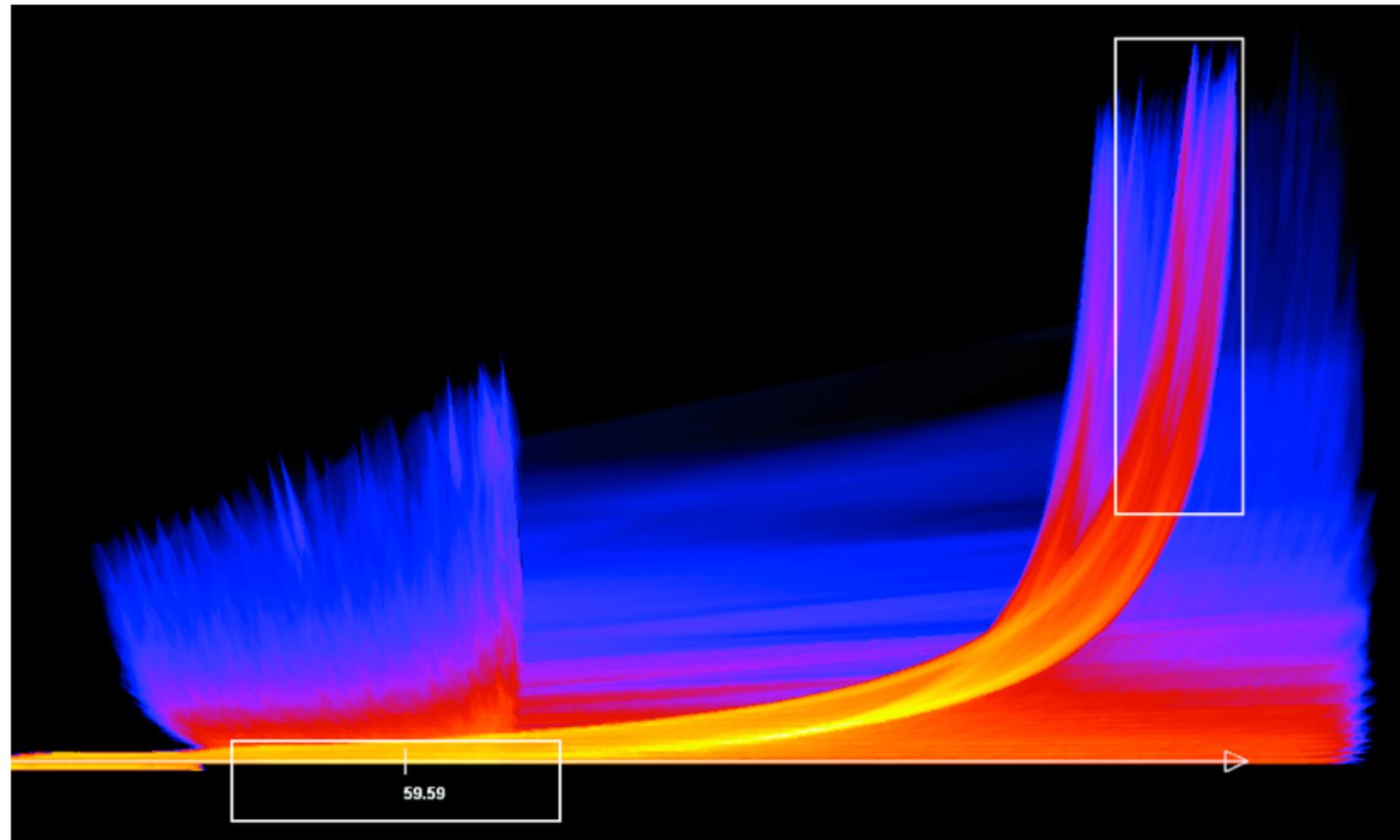
instead of drawing every point, calculate grid and intensities



Interactive Binned Scatterplot Matrix    Dimensions: 5    Bins: 20    Data Points: 100k



# Continuous Scatterplot

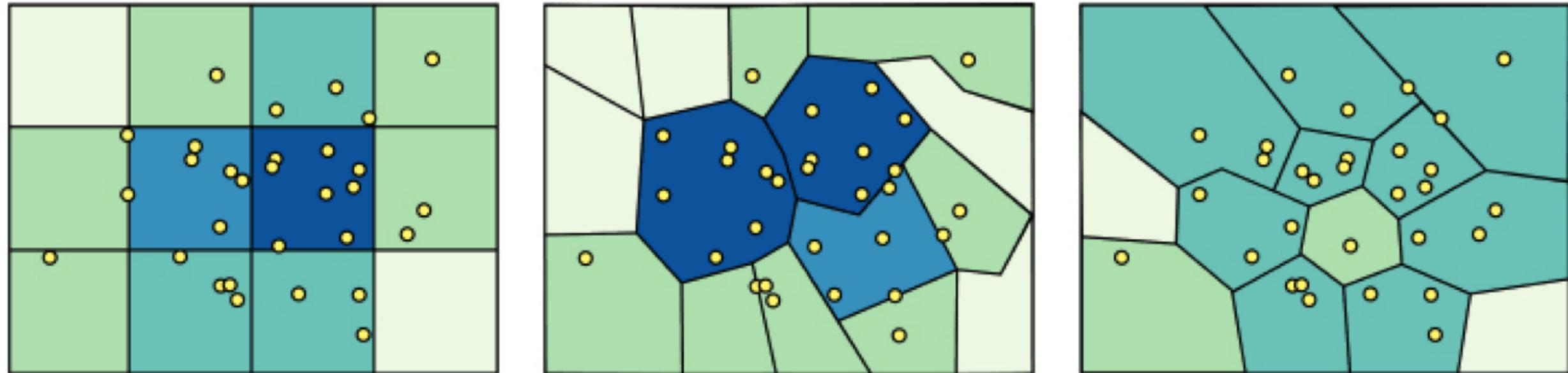


# Spatial Aggregation

# Spatial Aggregation

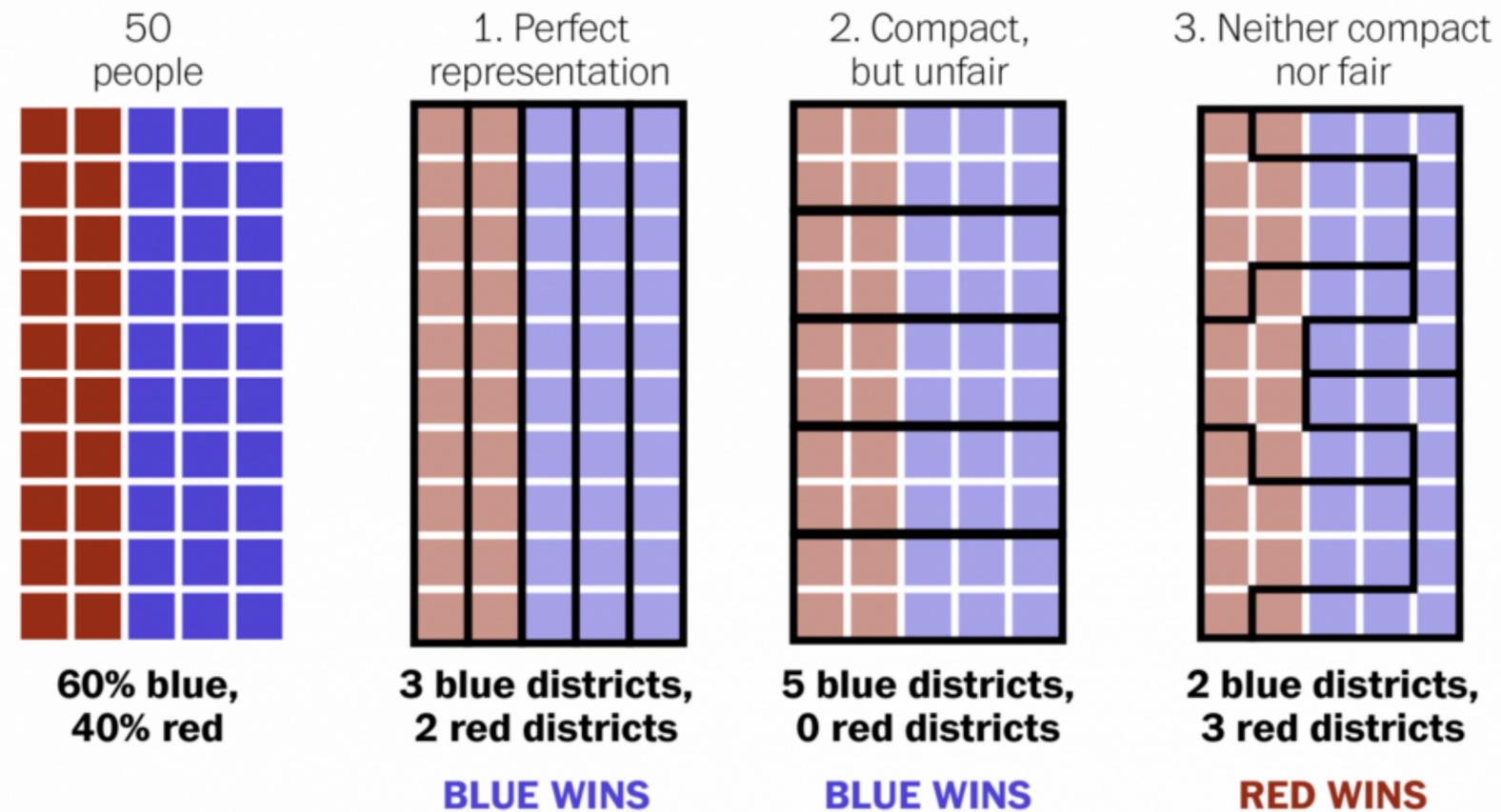
## modifiable areal unit problem

in cartography, changing the boundaries of the regions used to analyze data can yield dramatically different results



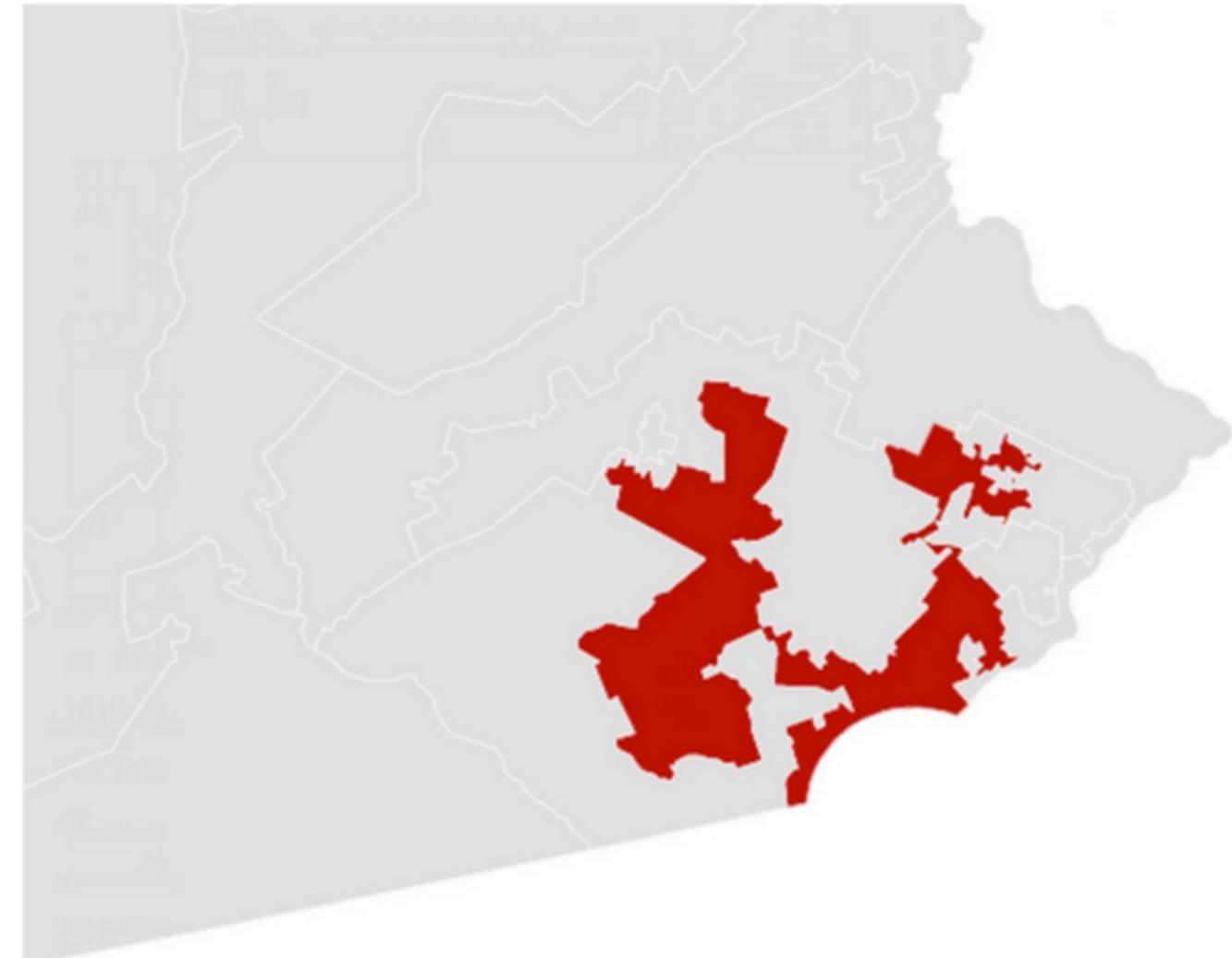
# Gerrymandering, explained

Three different ways to divide 50 people into five districts



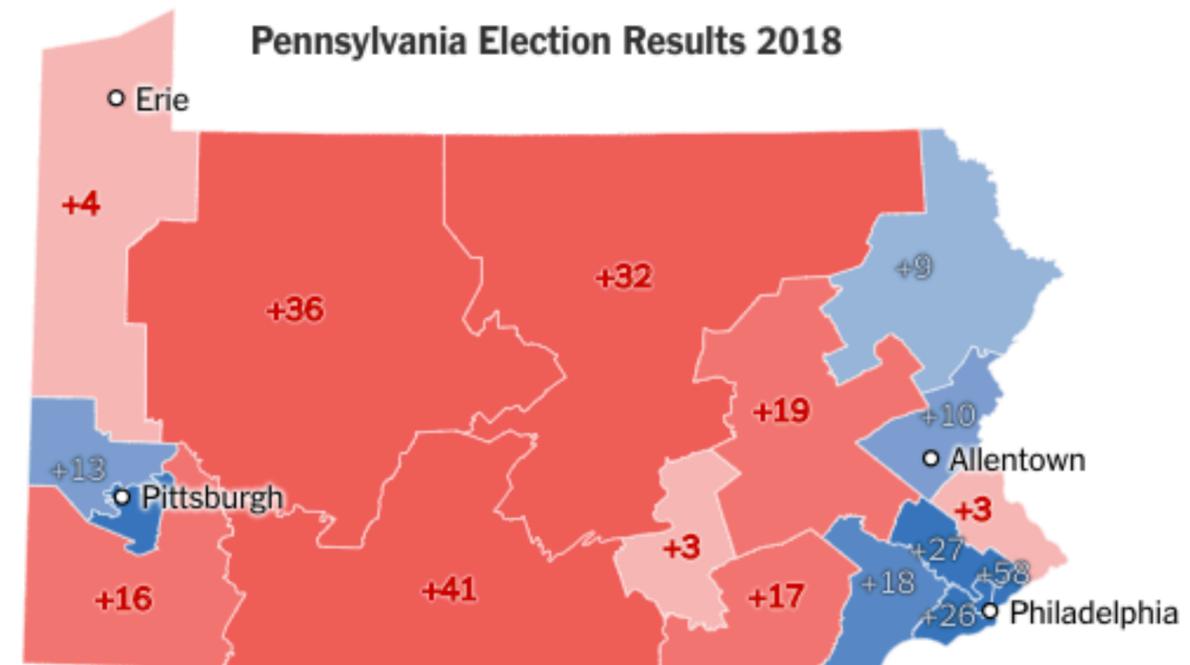
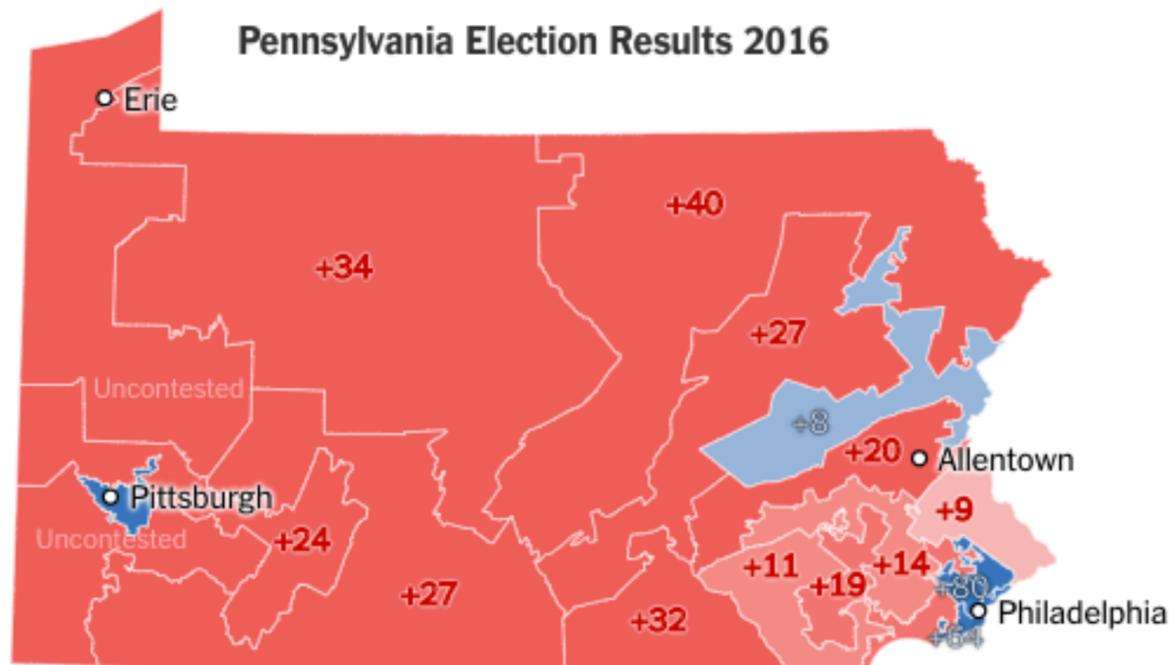
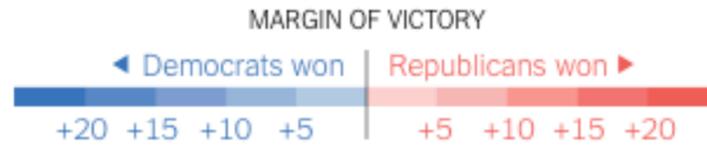
WASHINGTONPOST.COM/**WONKBLOG**

Adapted from Stephen Nass

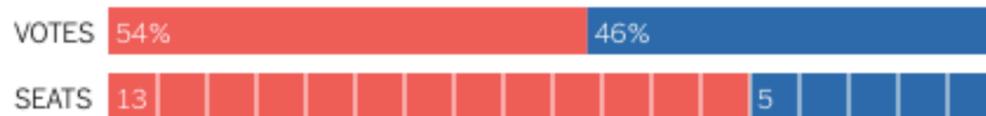


A real district in Pennsylvania  
Democrats won 51% of the vote  
but only 5 out of 18 house seats

# Updated Map after Court Decision

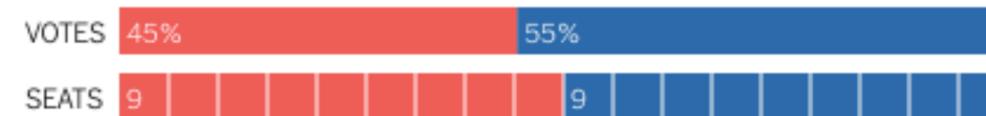


Republicans got 54% of U.S. House votes statewide ...



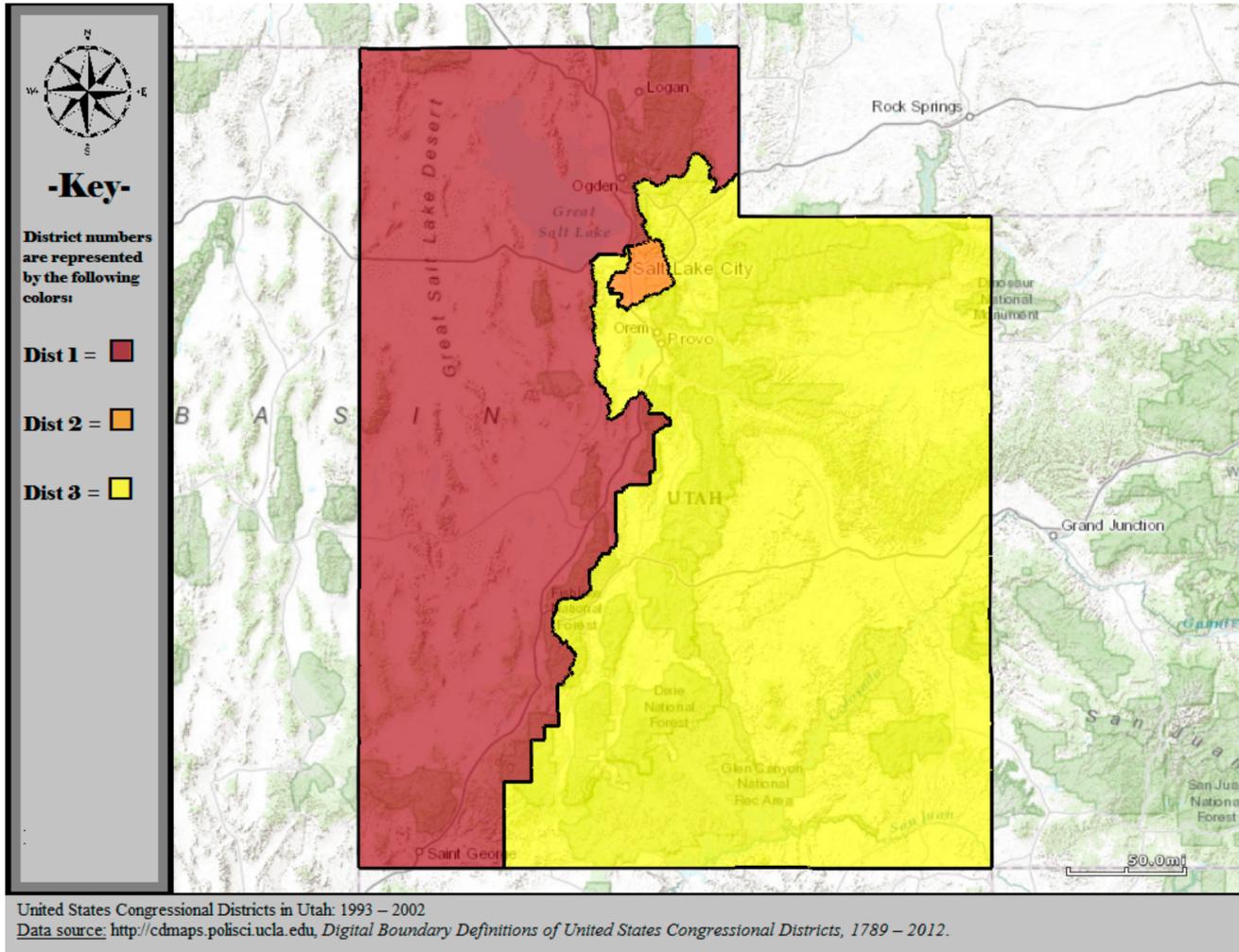
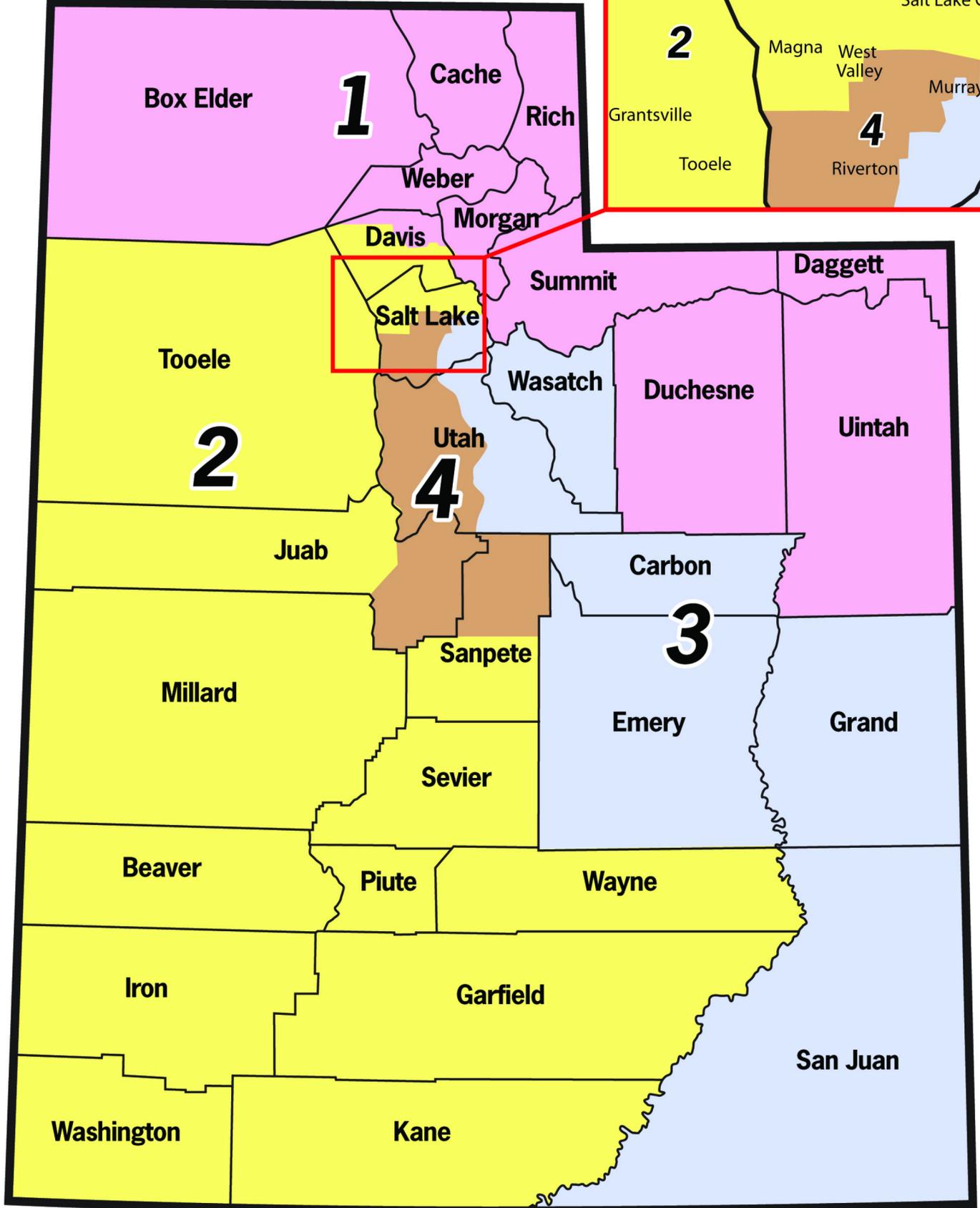
... but won 13 of 18 seats.

Republicans got 45% of U.S. House votes statewide ...



... and won 9 of 18 seats.

# Congressional Districts

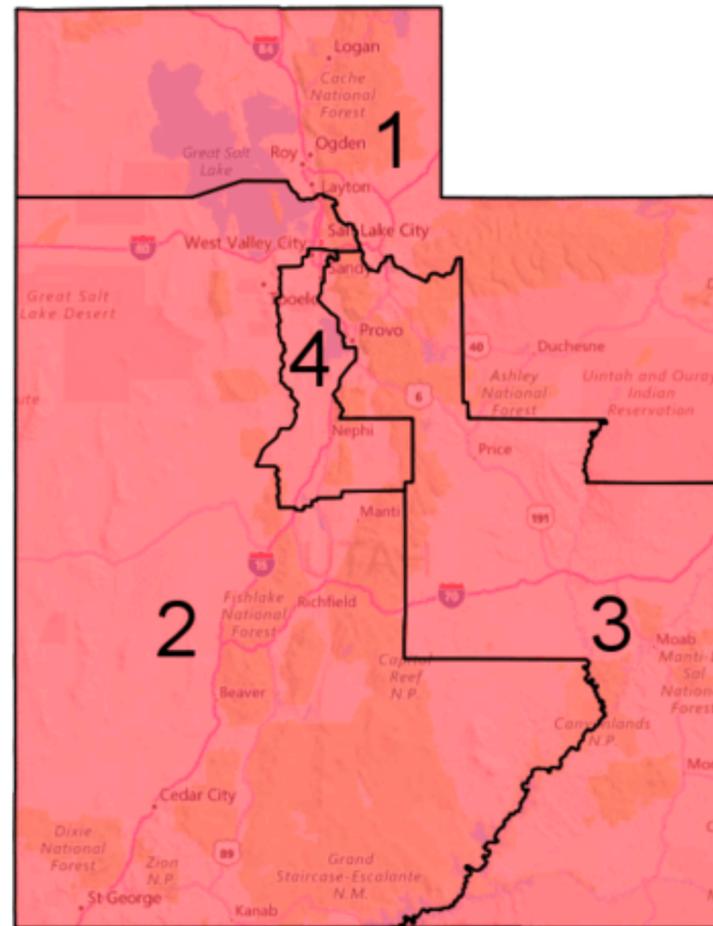


Valid till 2002

<http://www.sltrib.com/opinion/1794525-155/lake-salt-republican-county-http-utah>

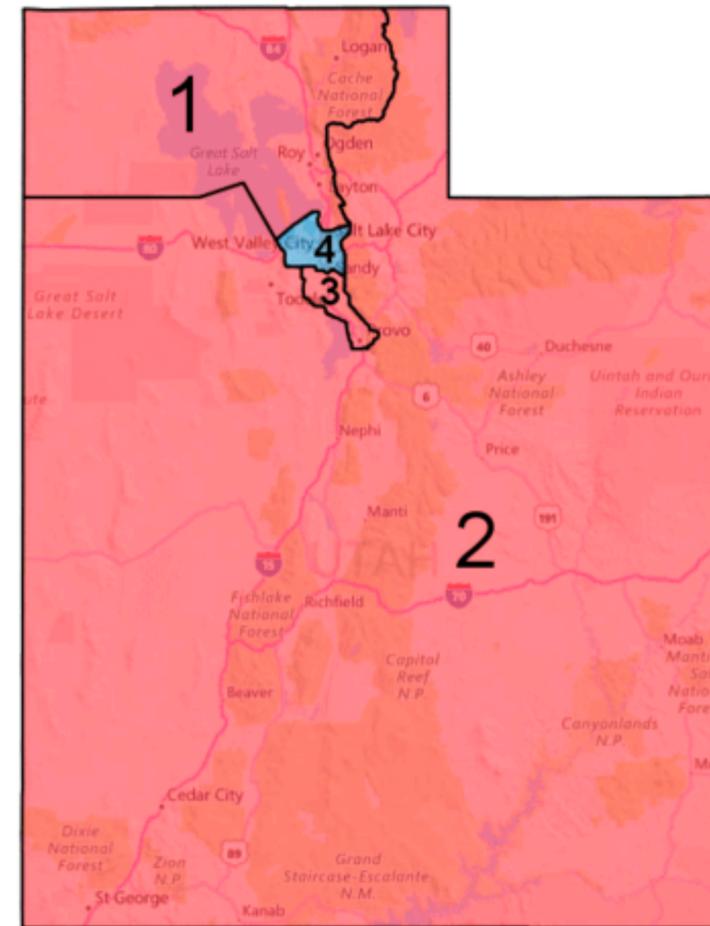
# 2016 Congressional Elections

## Utah's Republican Congressional Map



2016 Outcome  
Republican (4)

## Hypothetical Nonpartisan Map



Predicted Outcome  
Democratic (1)  
Republican (3)

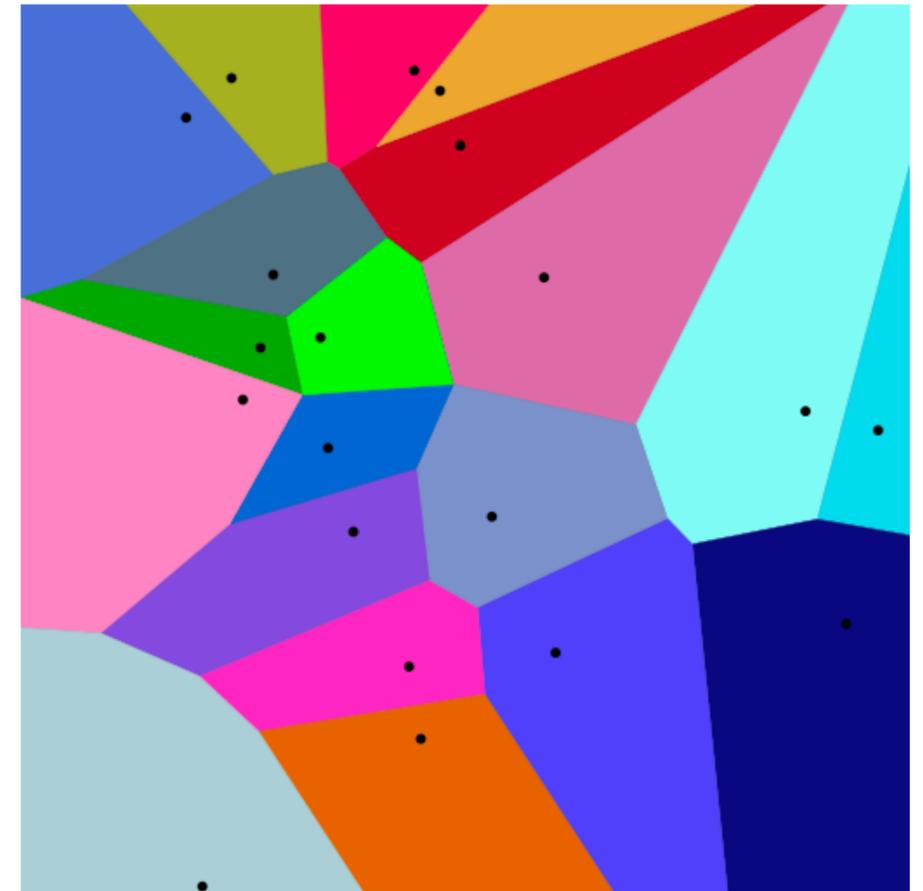


# Voronoi Diagrams

Given a set of locations, for which area is a location  $n$  closest?

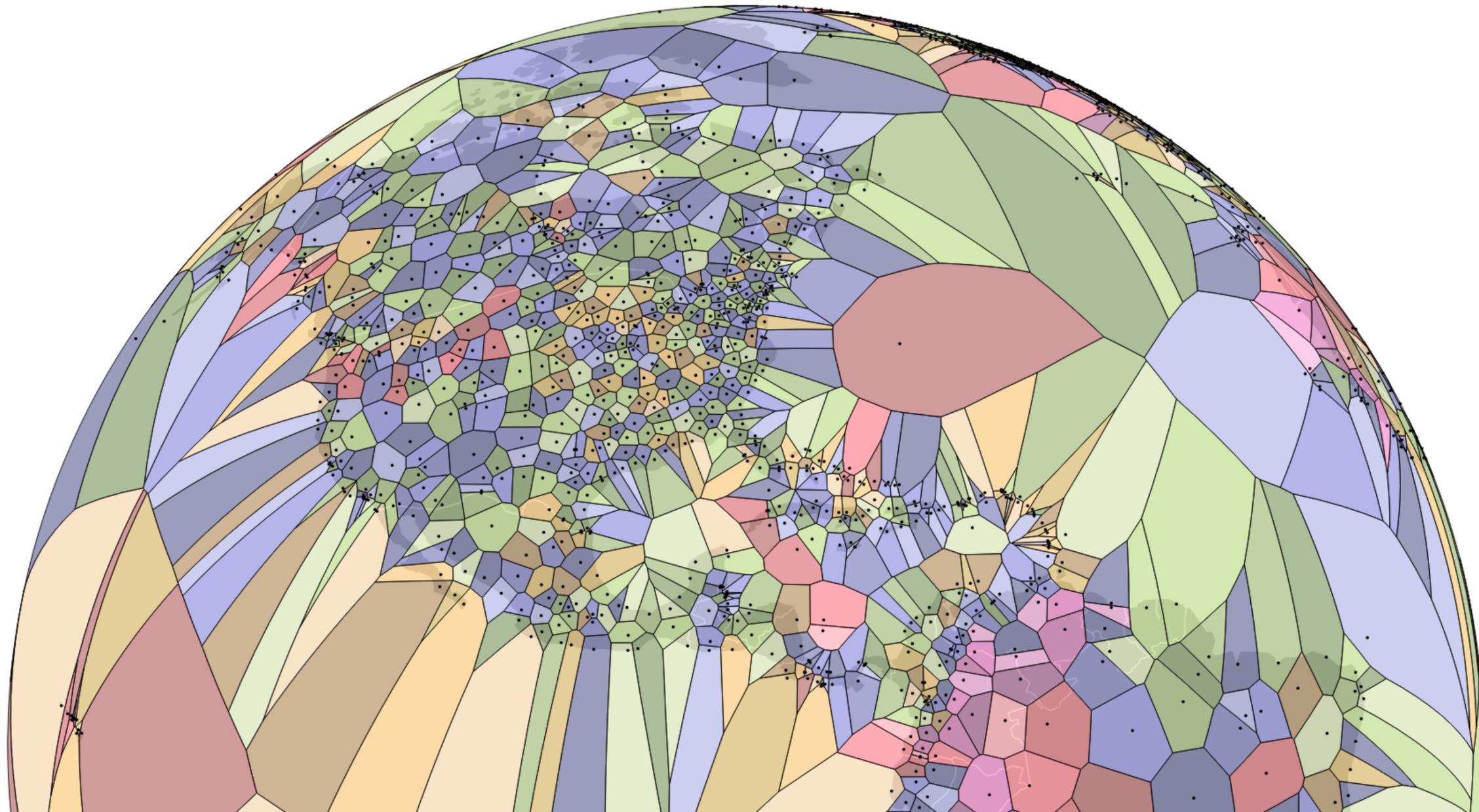
D3 Voronoi Layout:

<https://github.com/d3/d3-voronoi>



# Voronoi Examples

World Airports Voronoi

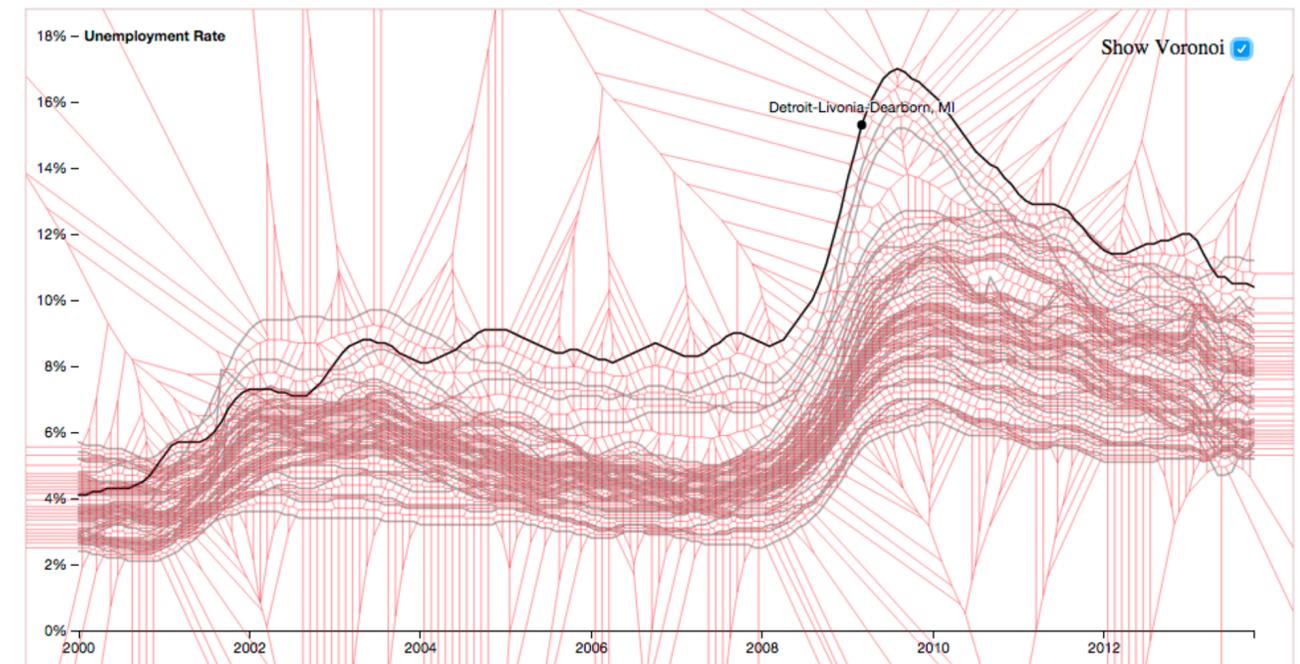
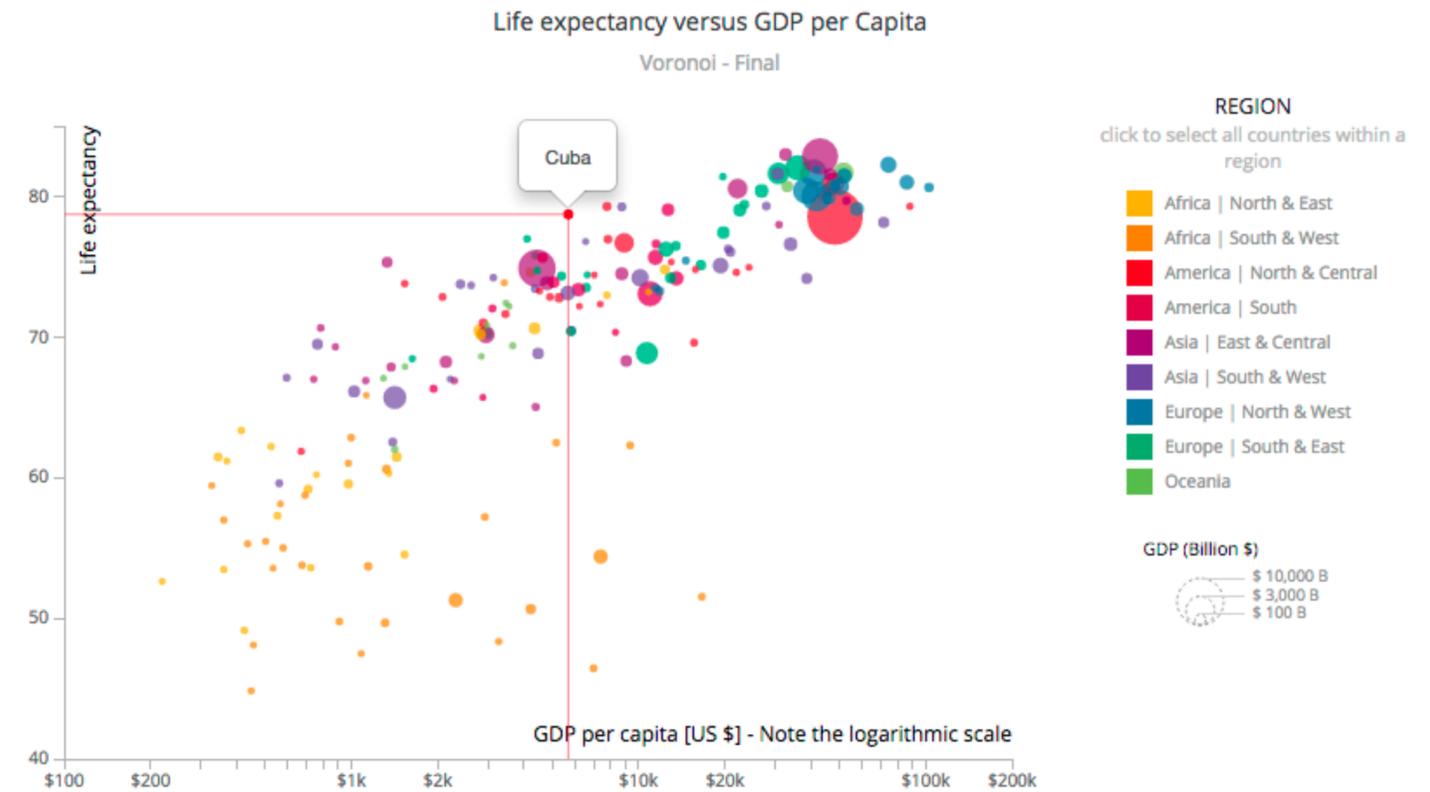


# Voronoi for Interaction

Useful for interaction:  
Increase size of target area to  
click/hover

Instead of clicking on point,  
hover in its region

<https://github.com/d3/d3-voronoi/>

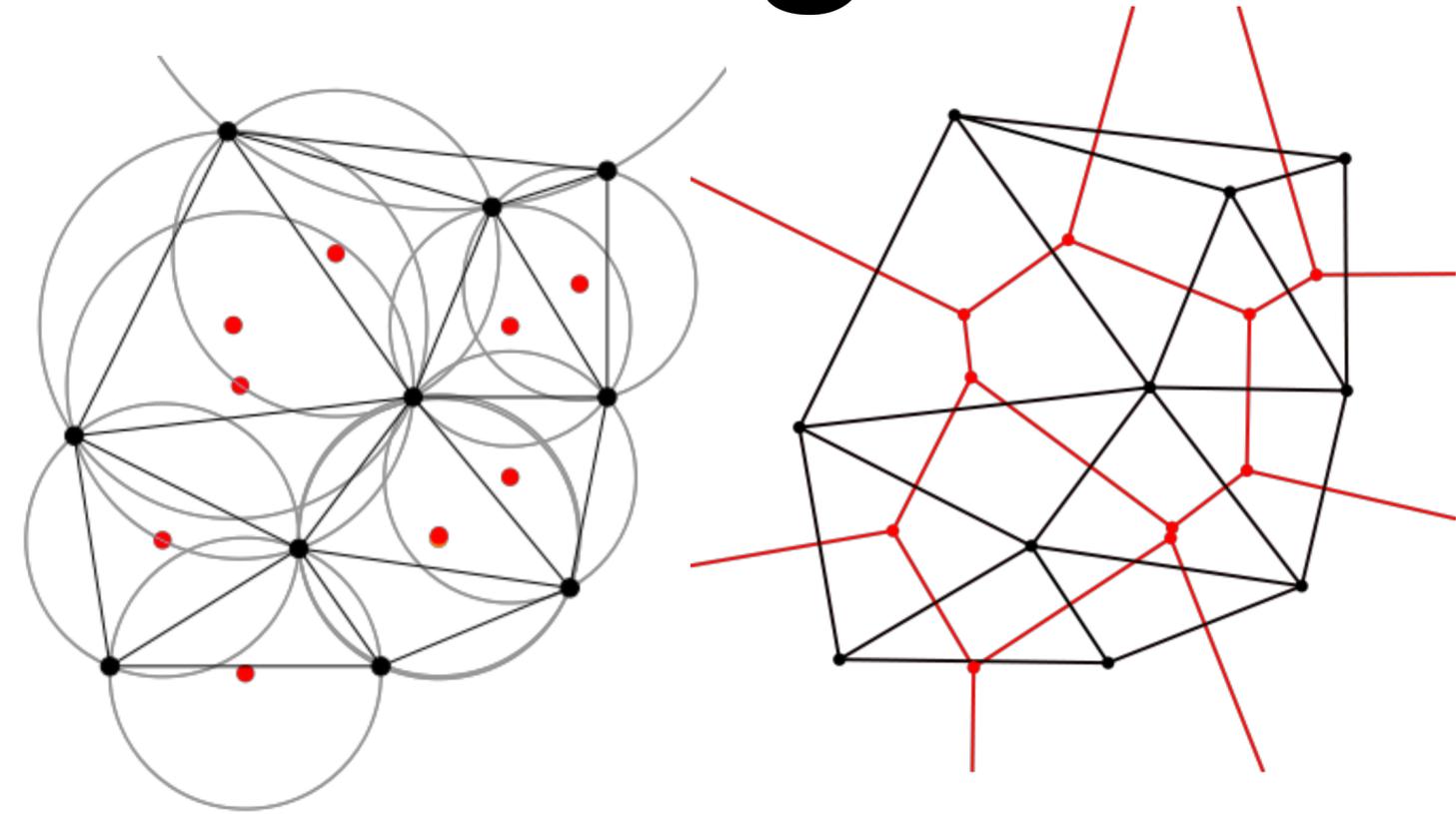


# Constructing a Voronoi Diagram

Calculate a Delaunay triangulation

Triangulation where no vertices are in a circle described by the vertices of a triangle

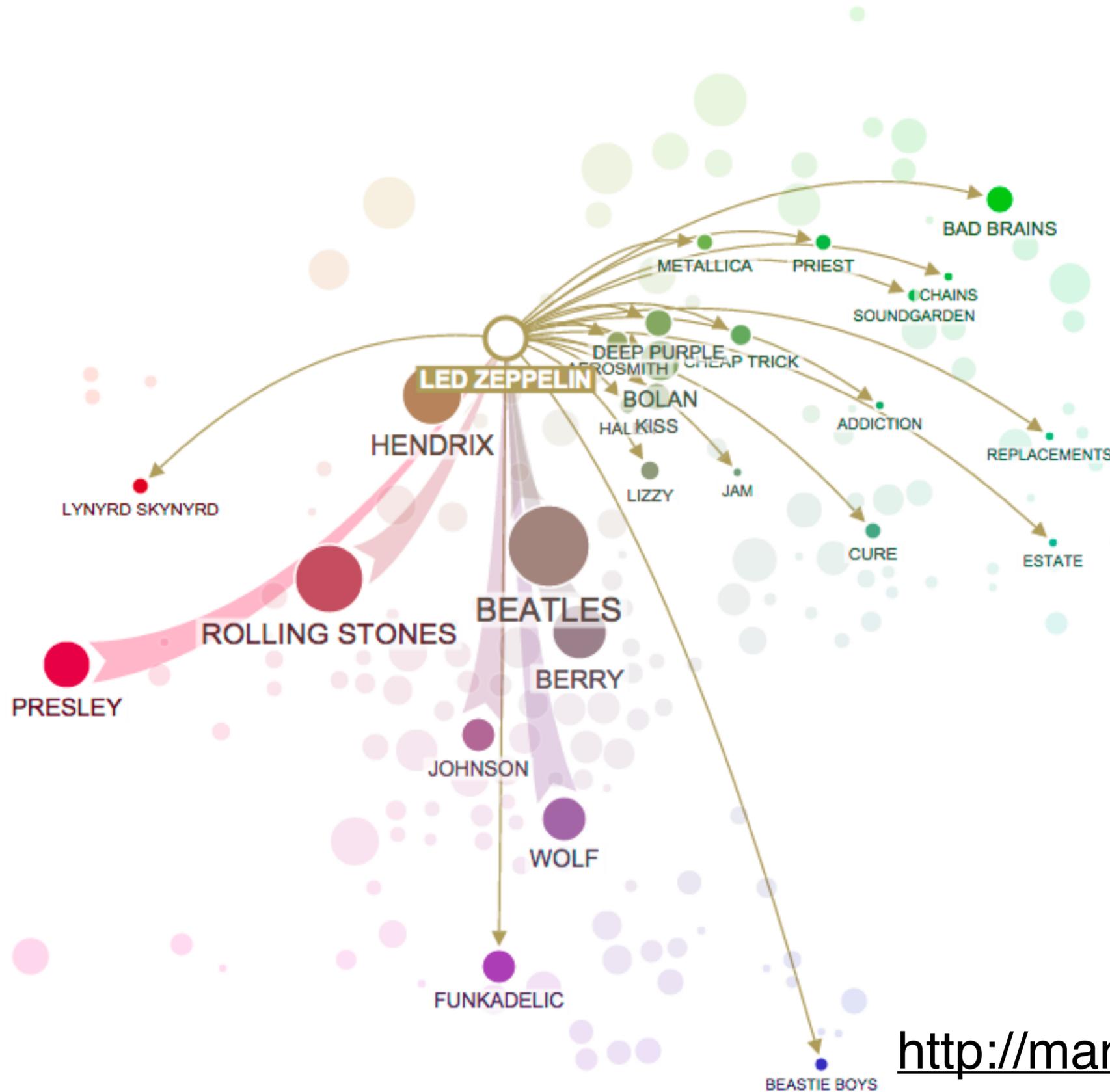
Voronoi edges are perpendicular to triangle edges.



[https://en.wikipedia.org/wiki/Delaunay\\_triangulation](https://en.wikipedia.org/wiki/Delaunay_triangulation)

<http://paulbourke.net/papers/triangulate/>

# Design Critique



<https://goo.gl/IDRXDI>

<http://mariandoerk.de/edgemaps/demo/>

# Clustering

# Clustering

Classification of items into “similar” bins

Based on similarity measures

Euclidean distance, Pearson correlation, ...

Partitional Algorithms

divide data into set of bins

# bins either manually set (e.g., k-means) or automatically determined (e.g., affinity propagation)

Hierarchical Algorithms

Produce “similarity tree” – dendrogram

Bi-Clustering

Clusters dimensions & records

Fuzzy clustering

allows occurrence of elements in multiples clusters

# Clustering Applications

Clusters can be used to

- order (pixel based techniques)

- brush (geometric techniques)

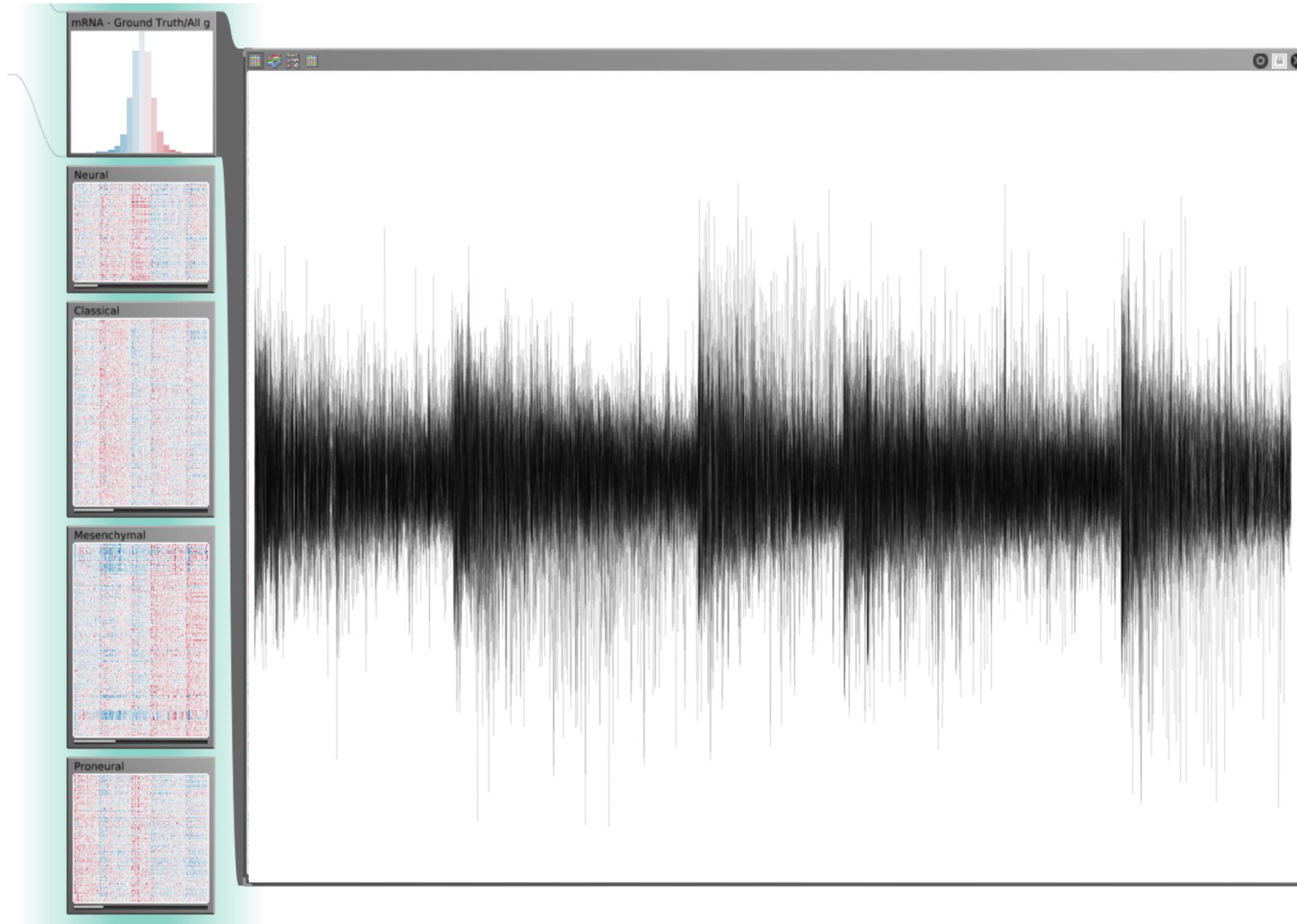
- aggregate

## Aggregation

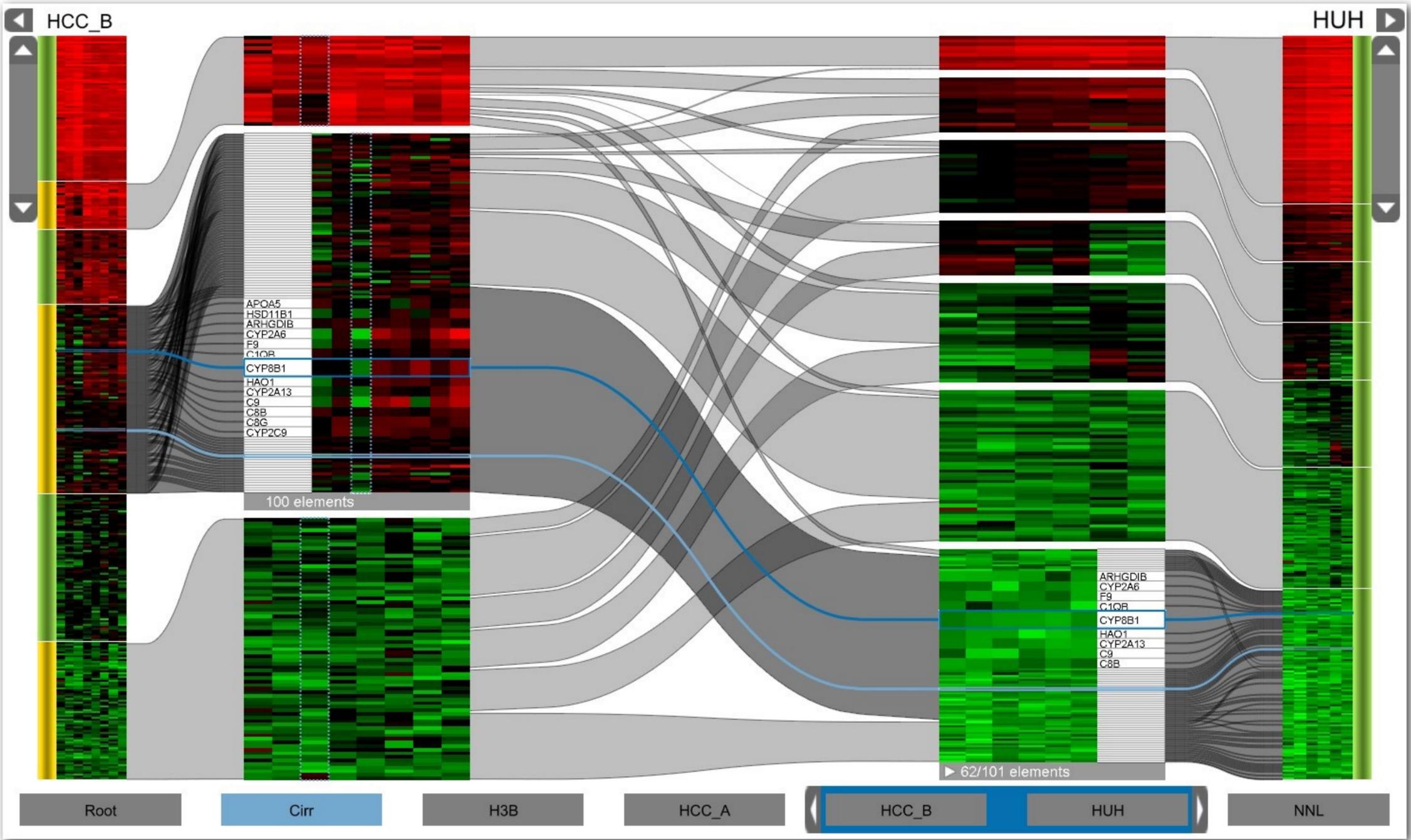
- cluster more homogeneous than whole dataset

- statistical measures, distributions, etc. more meaningful

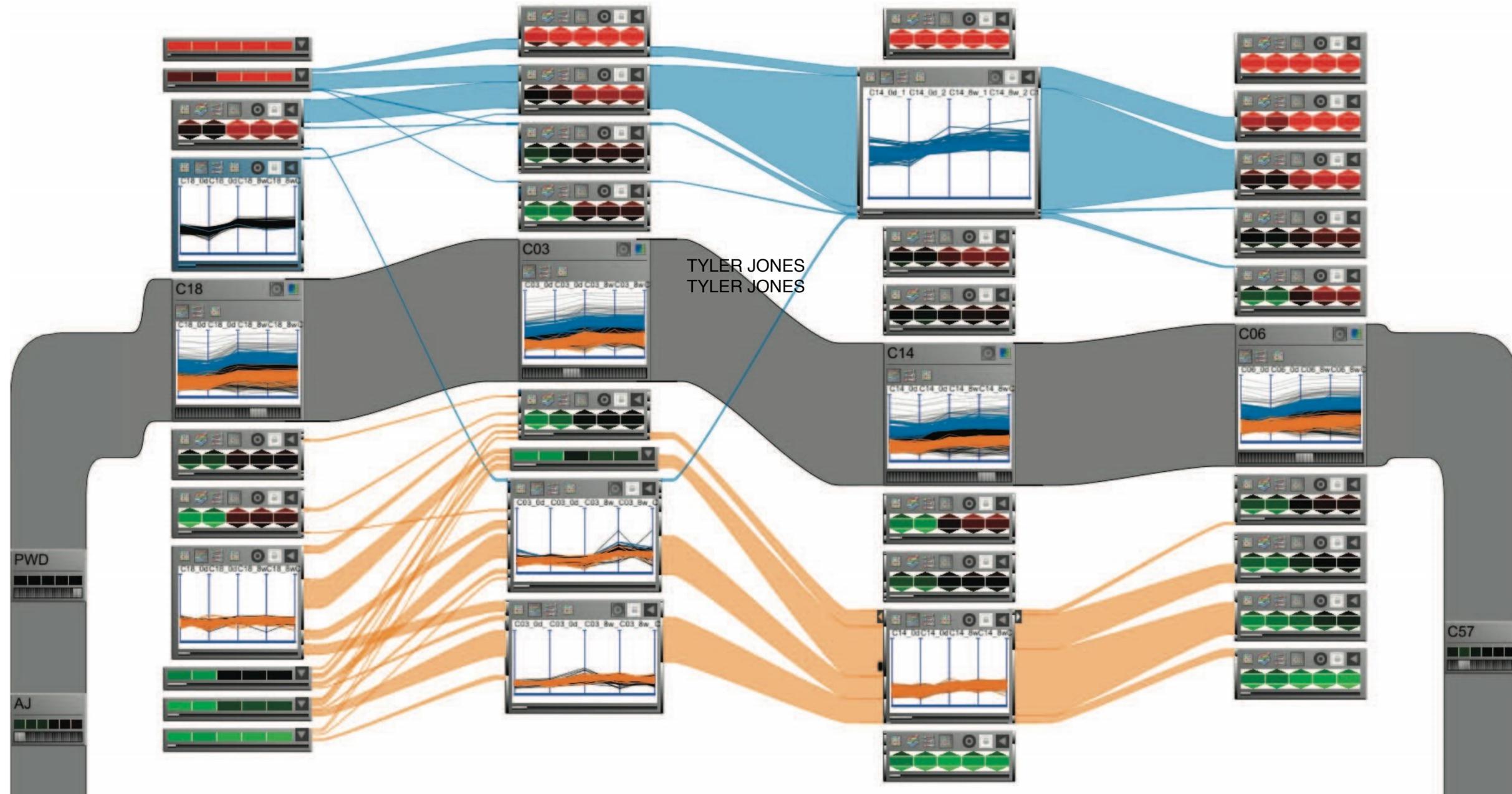
# Clustered Heat Map



# Cluster Comparison



# Aggregation



# Example: K-Means

Goal: Minimize aggregate intra-cluster distance (*inertia*)

$$\underset{C}{\operatorname{argmin}} \sum_{i=1}^k \sum_{x \in C_i} \|x - \mu_i\|^2$$

total squared distance from point to center of its cluster

for euclidian distance: this is the variance

measure of how internally coherent clusters are

# Lloyd's Algorithm

Input: set of records  $x_1 \dots x_n$ , and  $k$  (nr clusters)

Pick  $k$  starting points as centroids  $c_1 \dots c_k$

While not converged:

1. for each point  $x_i$  find closest centroid  $c_j$ 
  - for every  $c_j$  calculate distance  $D(x_i, c_j)$
  - assign  $x_i$  to cluster  $j$  defined by smallest distance
2. for each cluster  $j$ , compute a new centroid  $c_j$   
by calculating the average of all  $x_i$  assigned to cluster  $j$

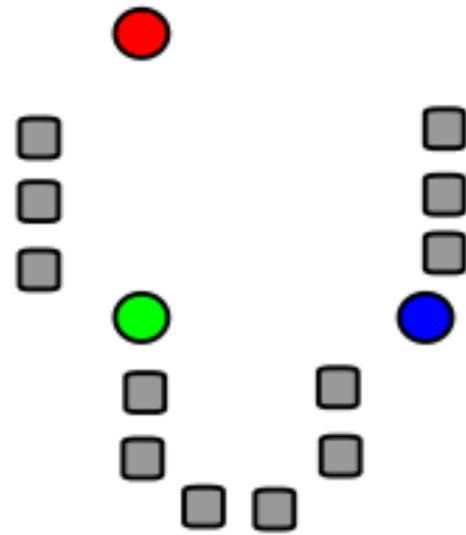
Repeat until convergence, e.g.,

no point has changed cluster

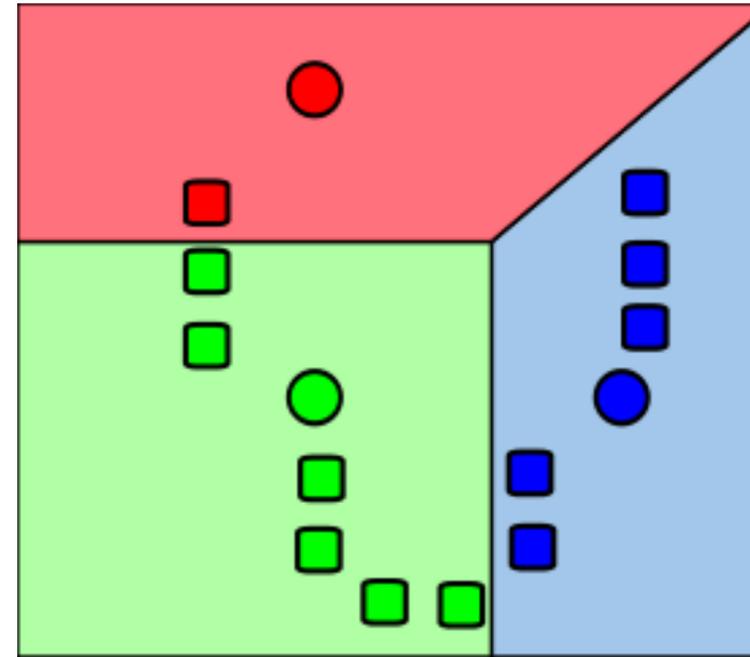
distance between old and new centroid below threshold

number of max iterations reached

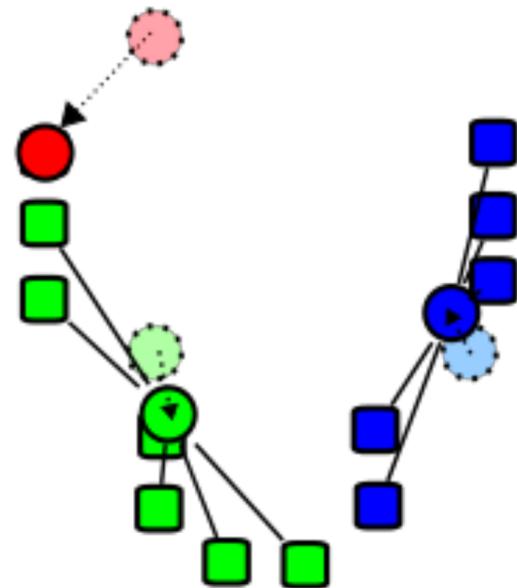
1. Initialization



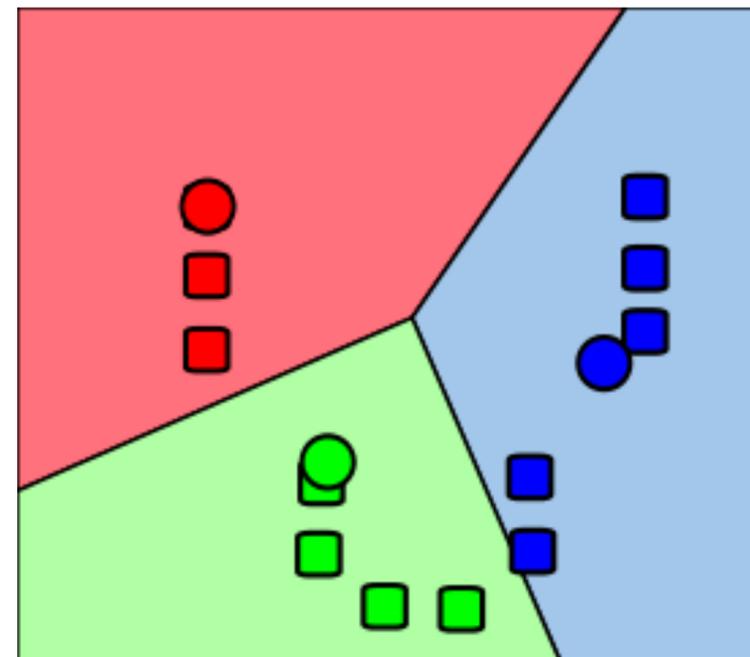
2. Assign Clusters



3. Update Centroids

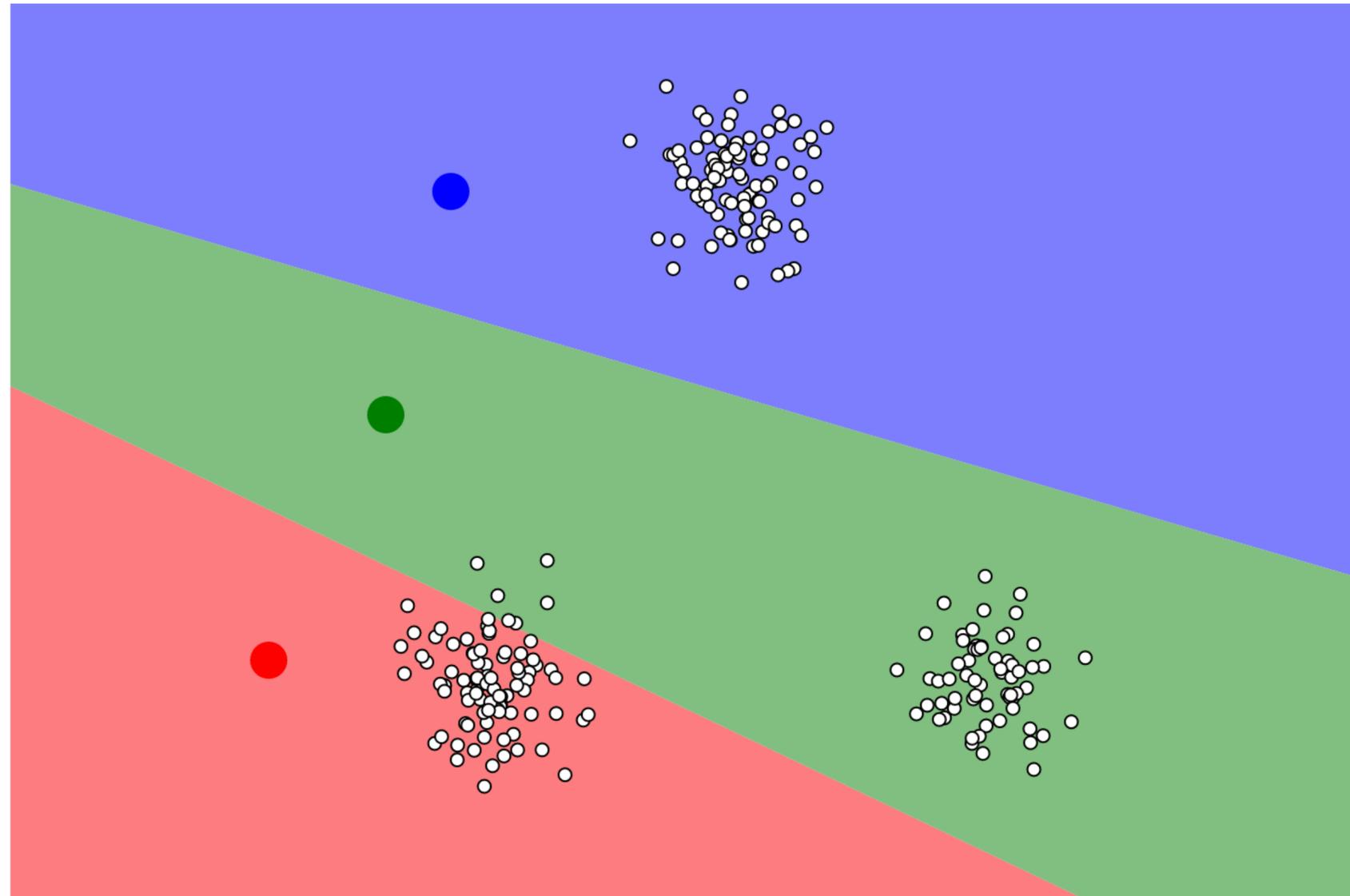


4. Assign Clusters



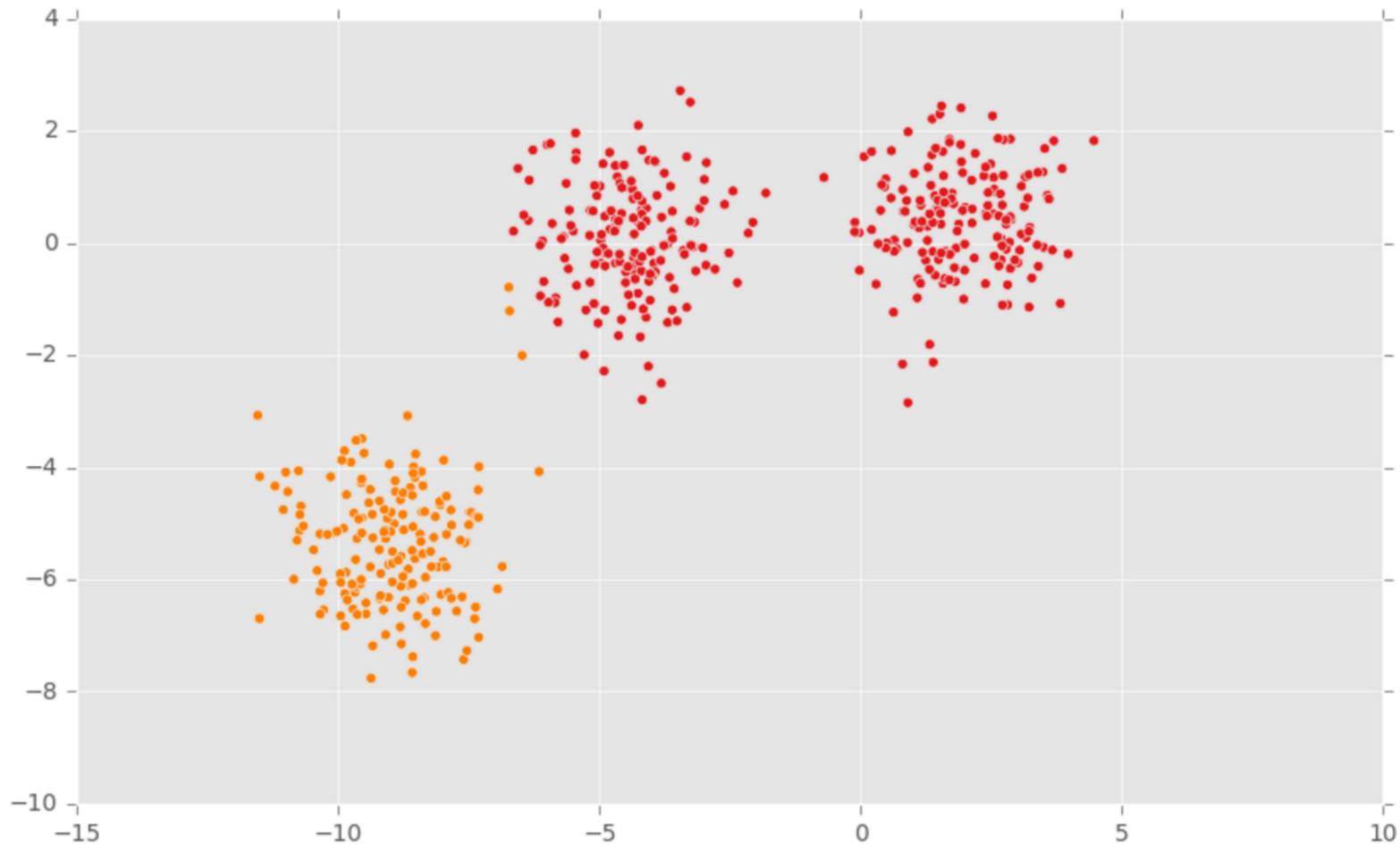
And repeat until converges

# Illustrated



<https://www.naftaliharris.com/blog/visualizing-k-means-clustering/>

# Choosing K



# Properties

Lloyds algorithm doesn't find a global optimum

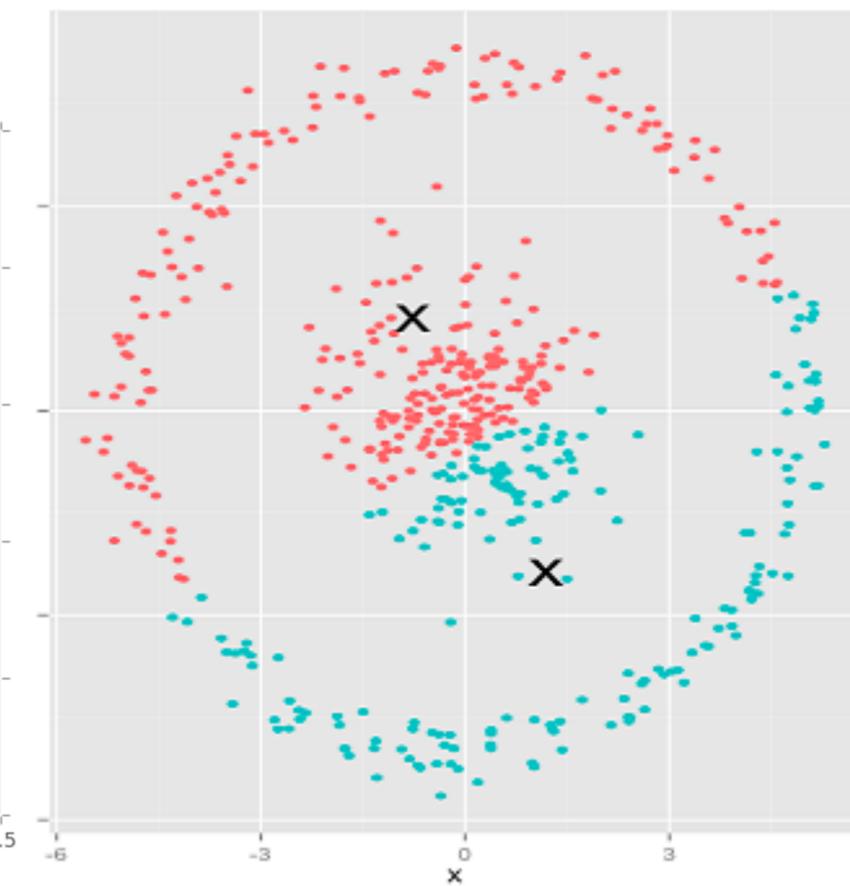
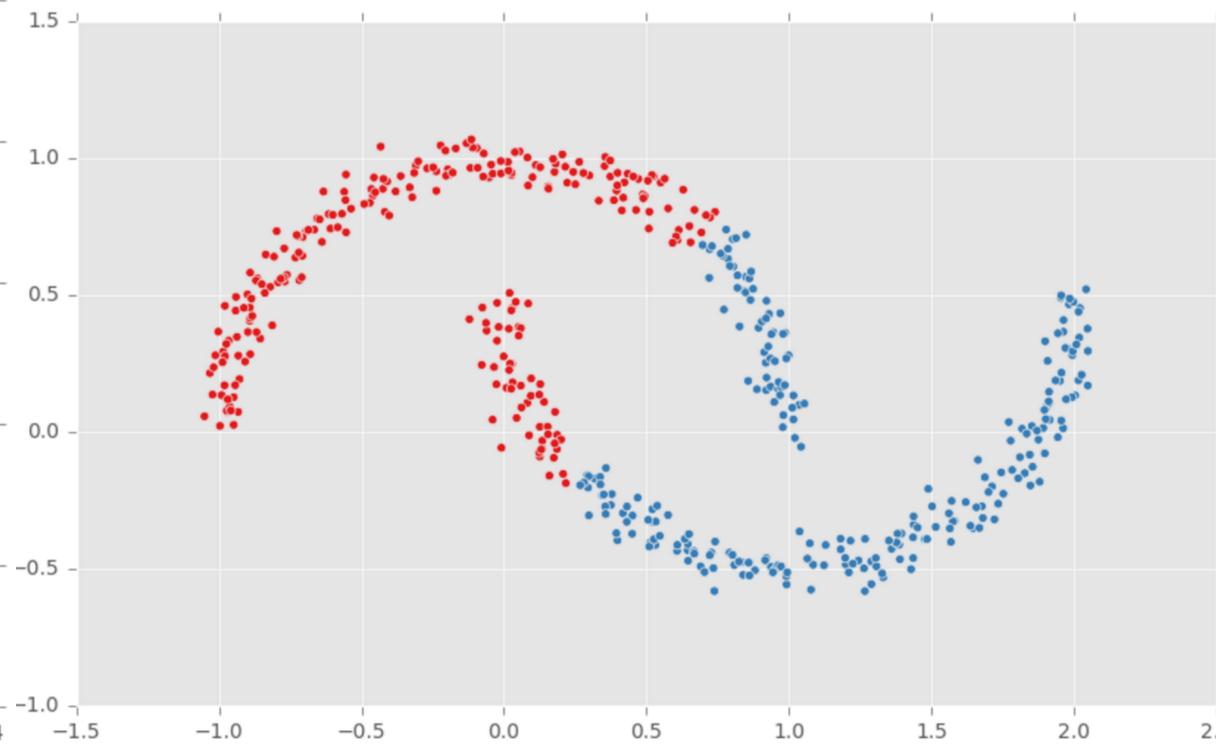
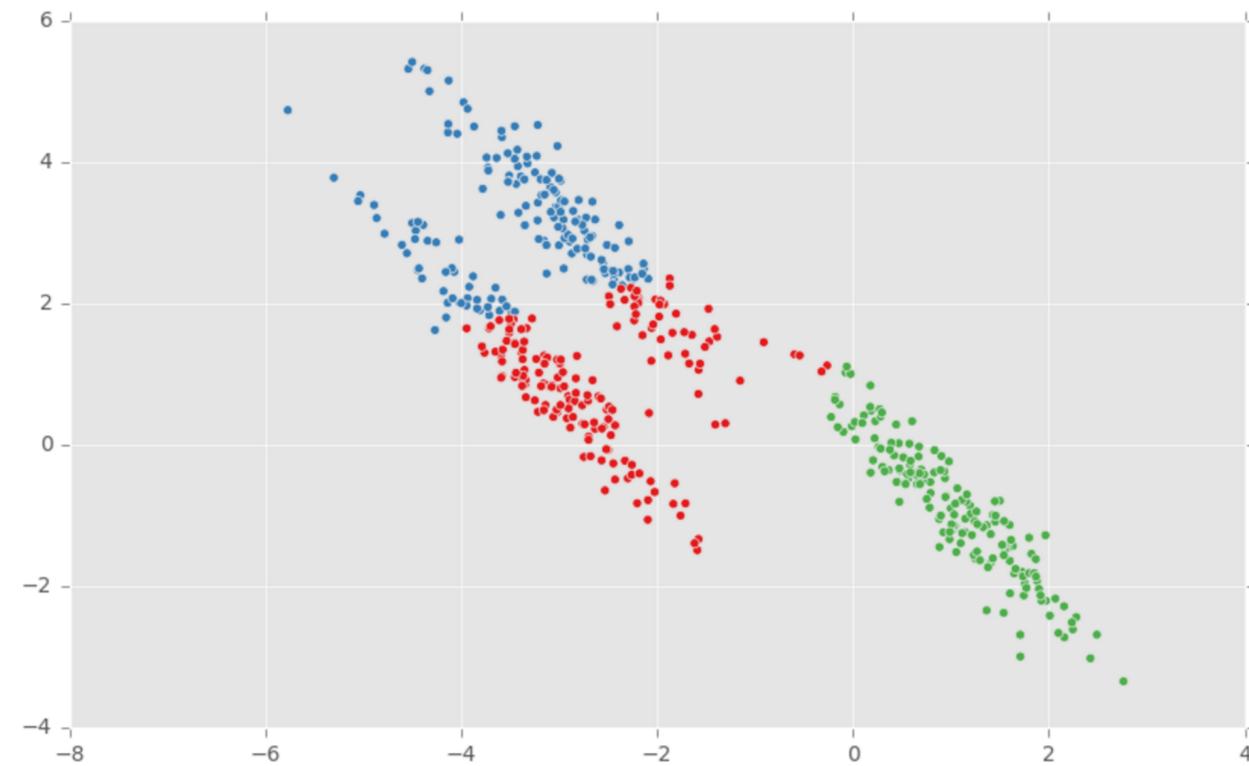
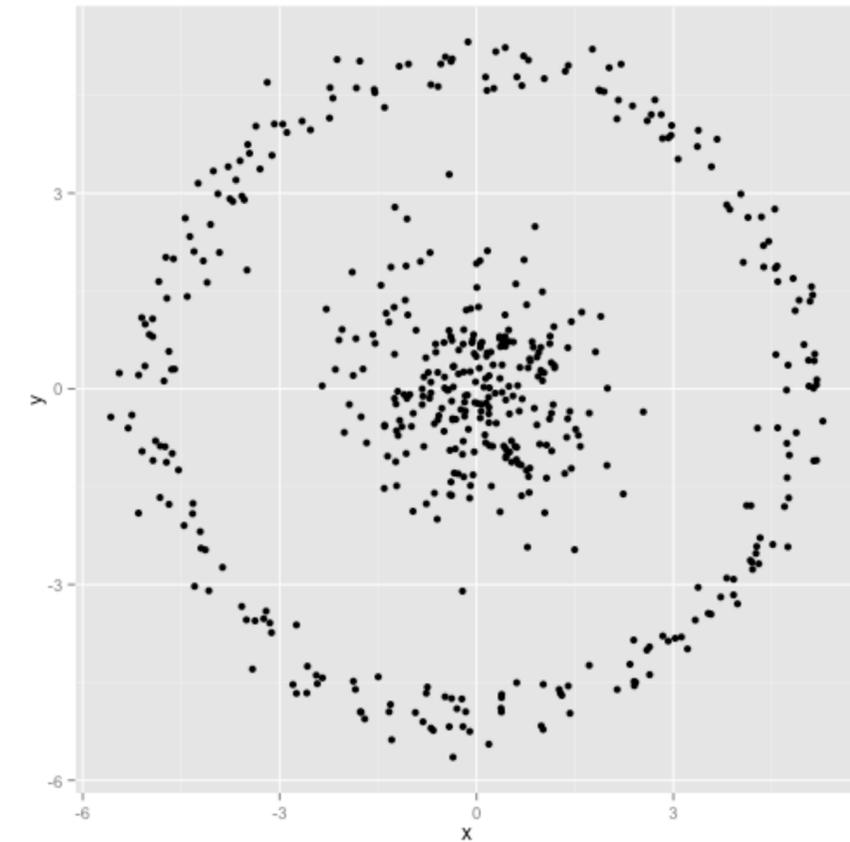
Instead it finds a local optimum

It is very fast:

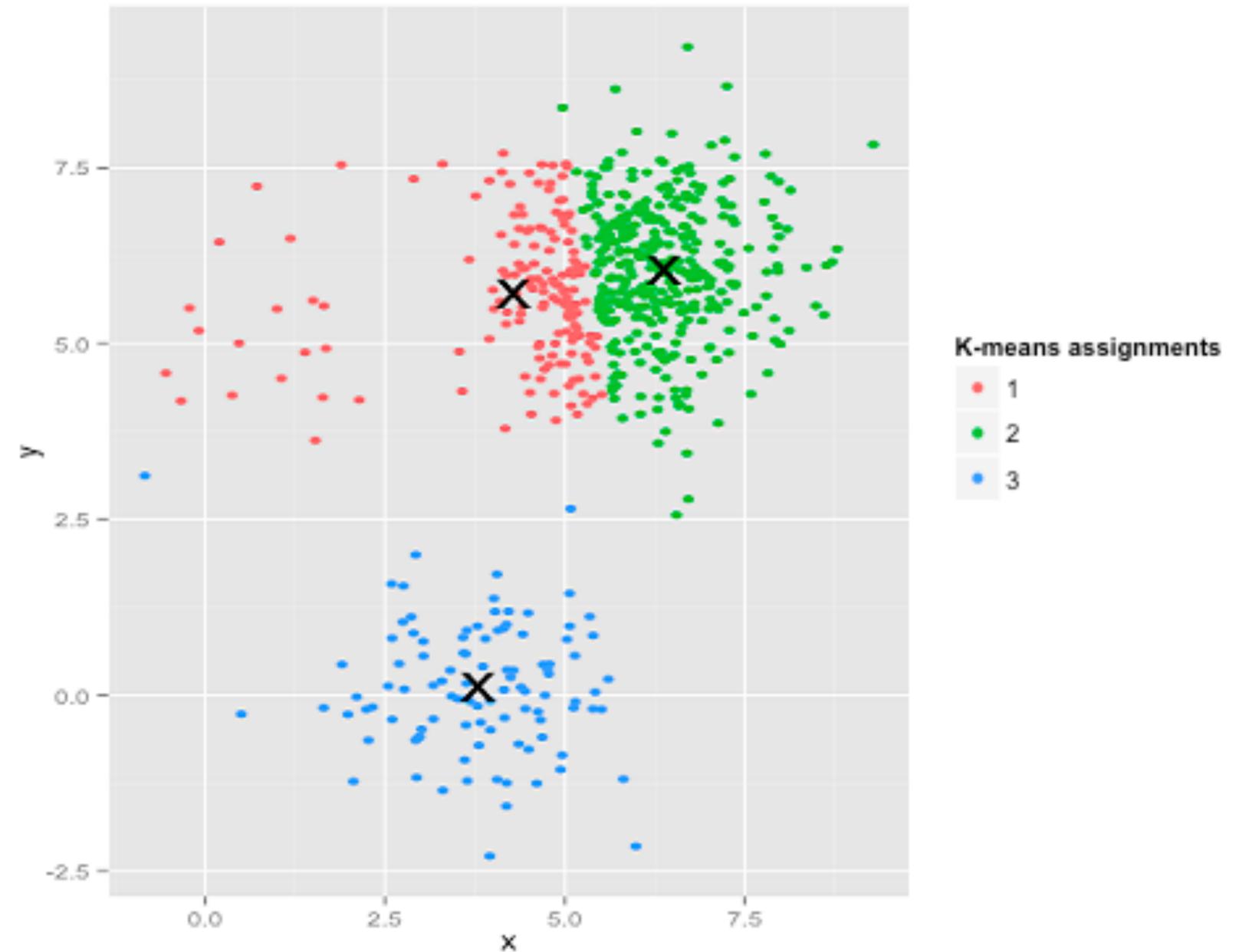
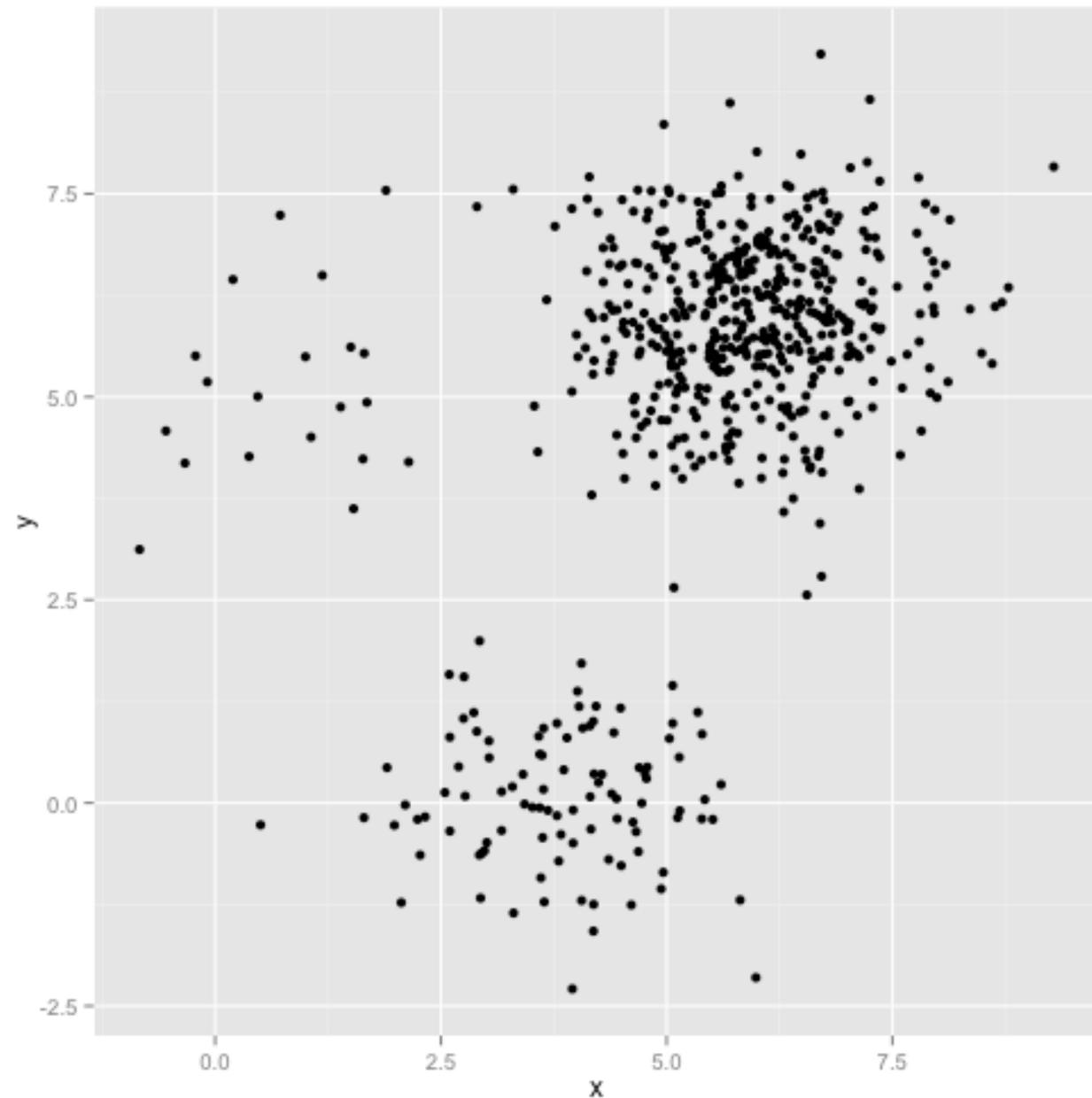
common to run multiple times and pick the solution with the minimum inertia

# K-Means Properties

Assumptions about data:  
roughly “circular” clusters of  
equal size



# K-Means Unequal Cluster Size



# DBScan

Density-based spatial clustering of applications with noise

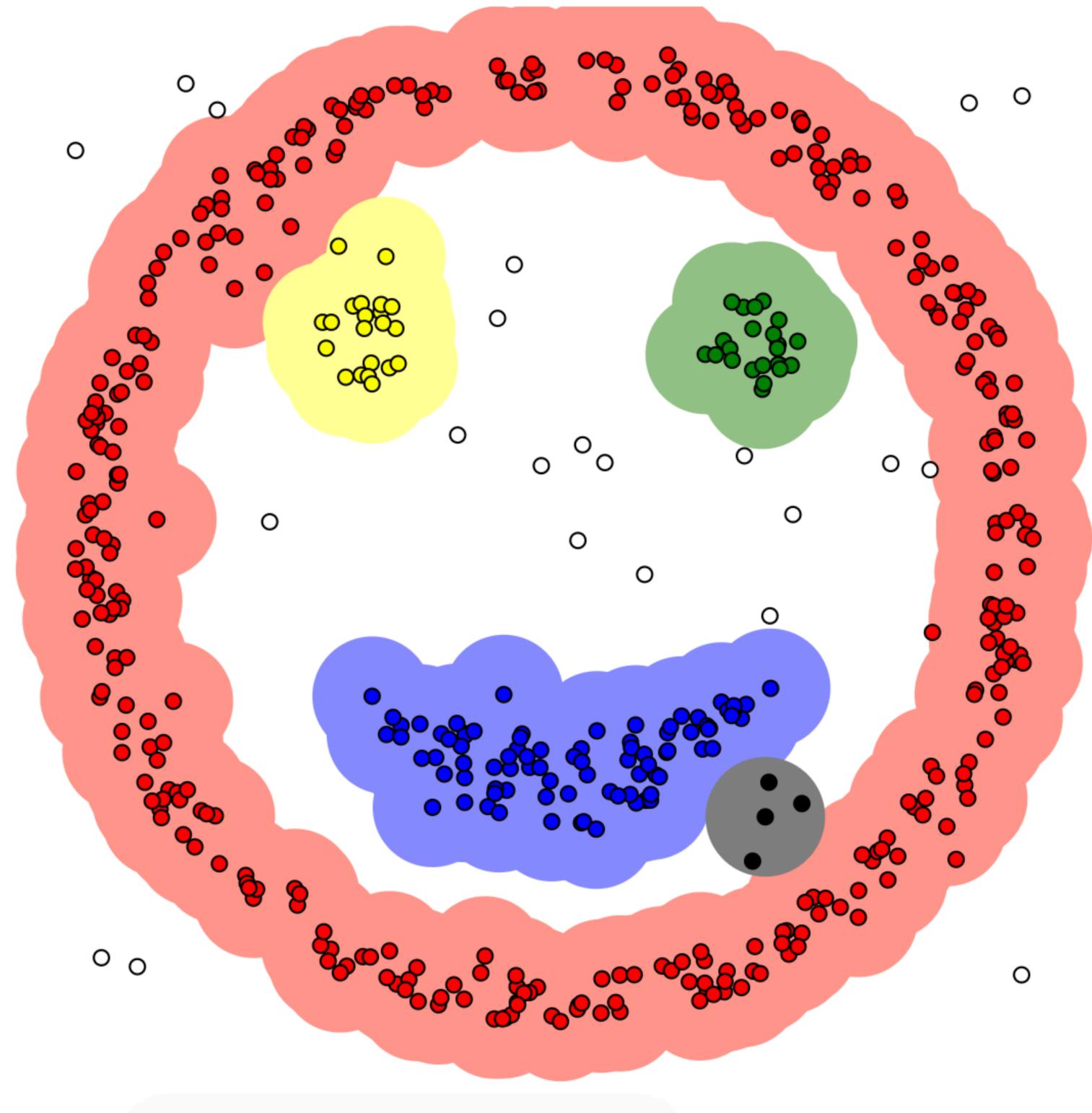
Idea: Clusters are dense groups

if point belongs to a cluster, it should be near to lots of other points in that cluster.

Parameters:

Epsilon: if new point distance to closest point in cluster is  $<$  epsilon, add to cluster

Min points: what's the smallest cluster (outliers)



# Hierarchical Clustering

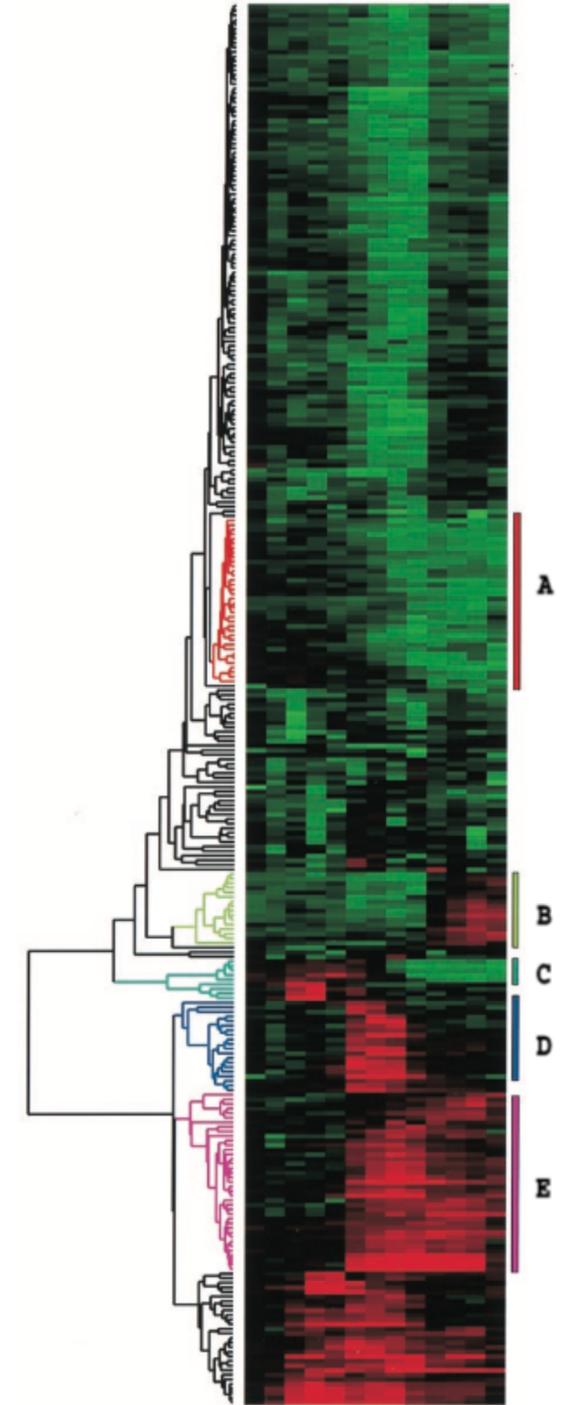
Two types:

**agglomerative** clustering

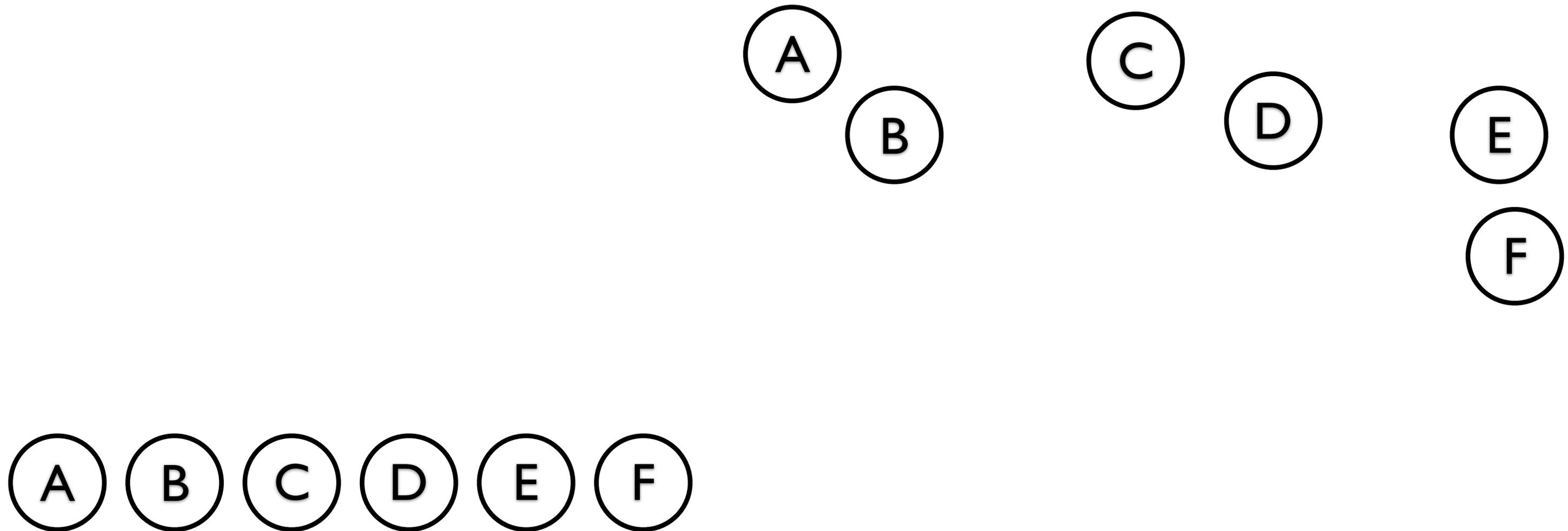
start with each node as a cluster and merge

**divisive** clustering

start with one cluster, and split



# Agglomerative Clustering Idea



# Linkage Criteria

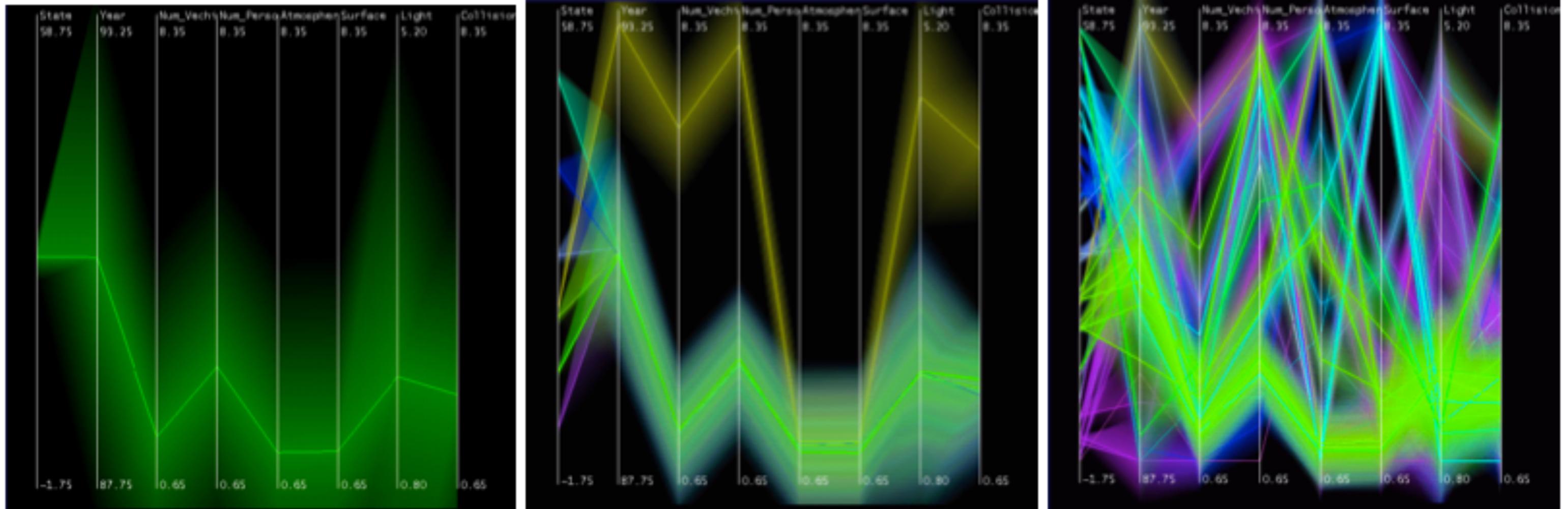
How do you define similarity between two clusters to be merged (A and B)?

- maximum linkage distance: two elements that are apart the furthest
- use minimum linkage distance: the two closest elements
- use average linkage distance
- use centroid distance

Names	Formula
Maximum or complete-linkage clustering	$\max \{ d(a, b) : a \in A, b \in B \}.$
Minimum or single-linkage clustering	$\min \{ d(a, b) : a \in A, b \in B \}.$
Mean or average linkage clustering, or UPGMA	$\frac{1}{ A  B } \sum_{a \in A} \sum_{b \in B} d(a, b).$
Centroid linkage clustering, or UPGMC	$\ c_s - c_t\ $ where $c_s$ and $c_t$ are the centroids of clusters $s$ and $t$ , respectively.



# Hierarchical Parallel Coordinates



# Dimensionality Reduction

# Dimensionality Reduction

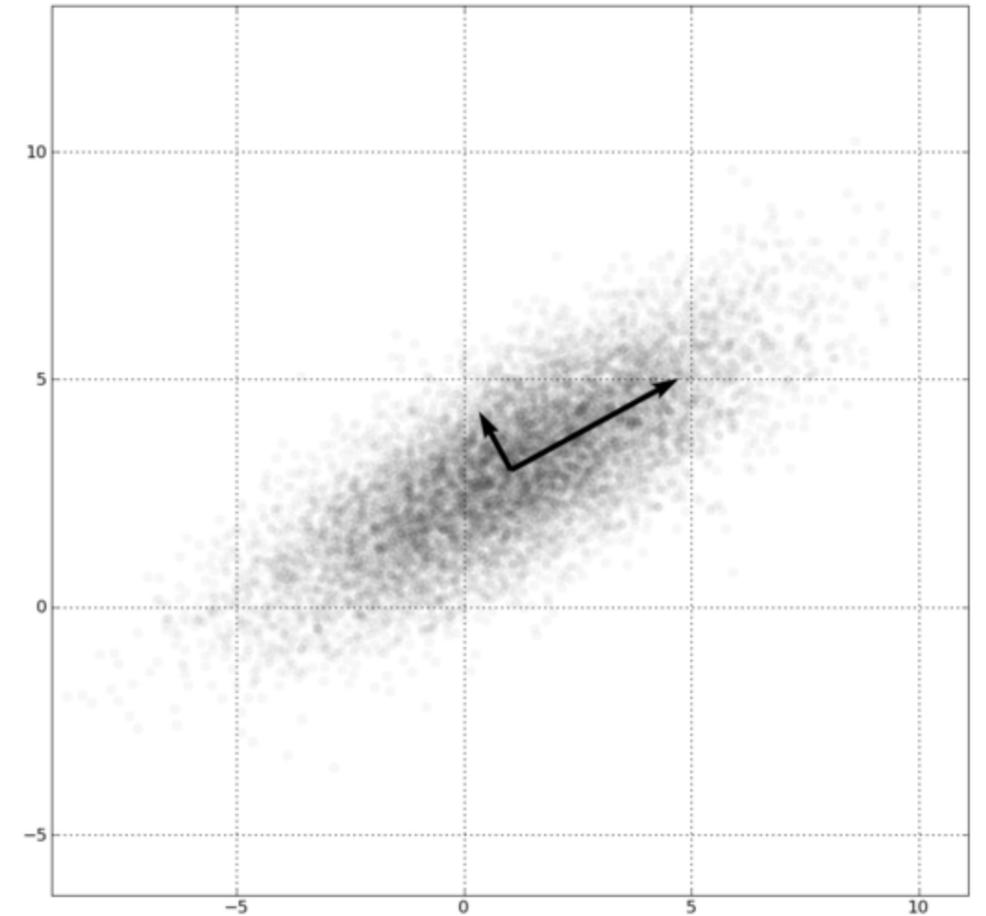
Reduce high dimensional to lower dimensional space

Preserve as much of variation as possible

Plot lower dimensional space

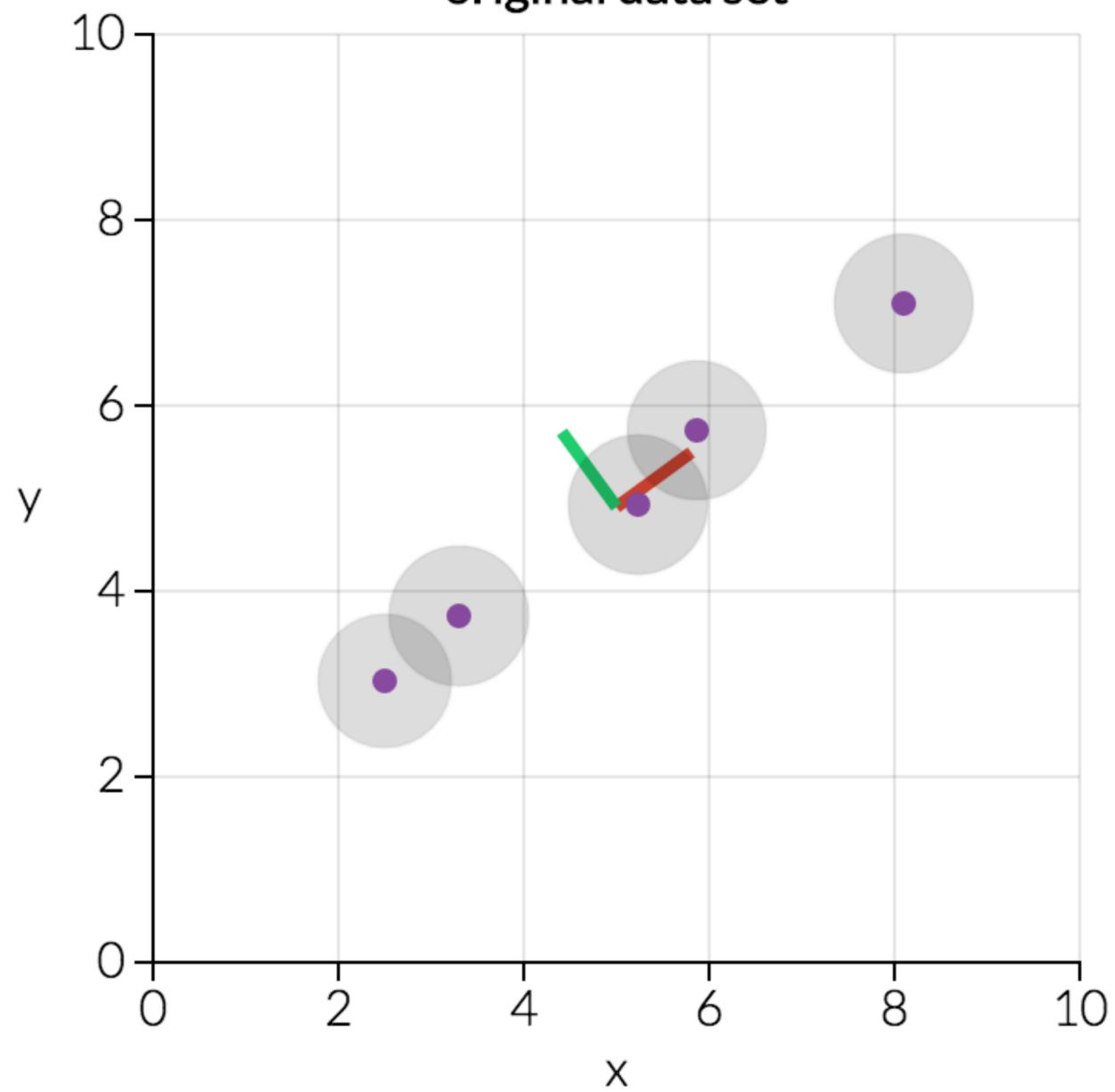
*Principal Component Analysis (PCA)*

linear mapping, by order of variance

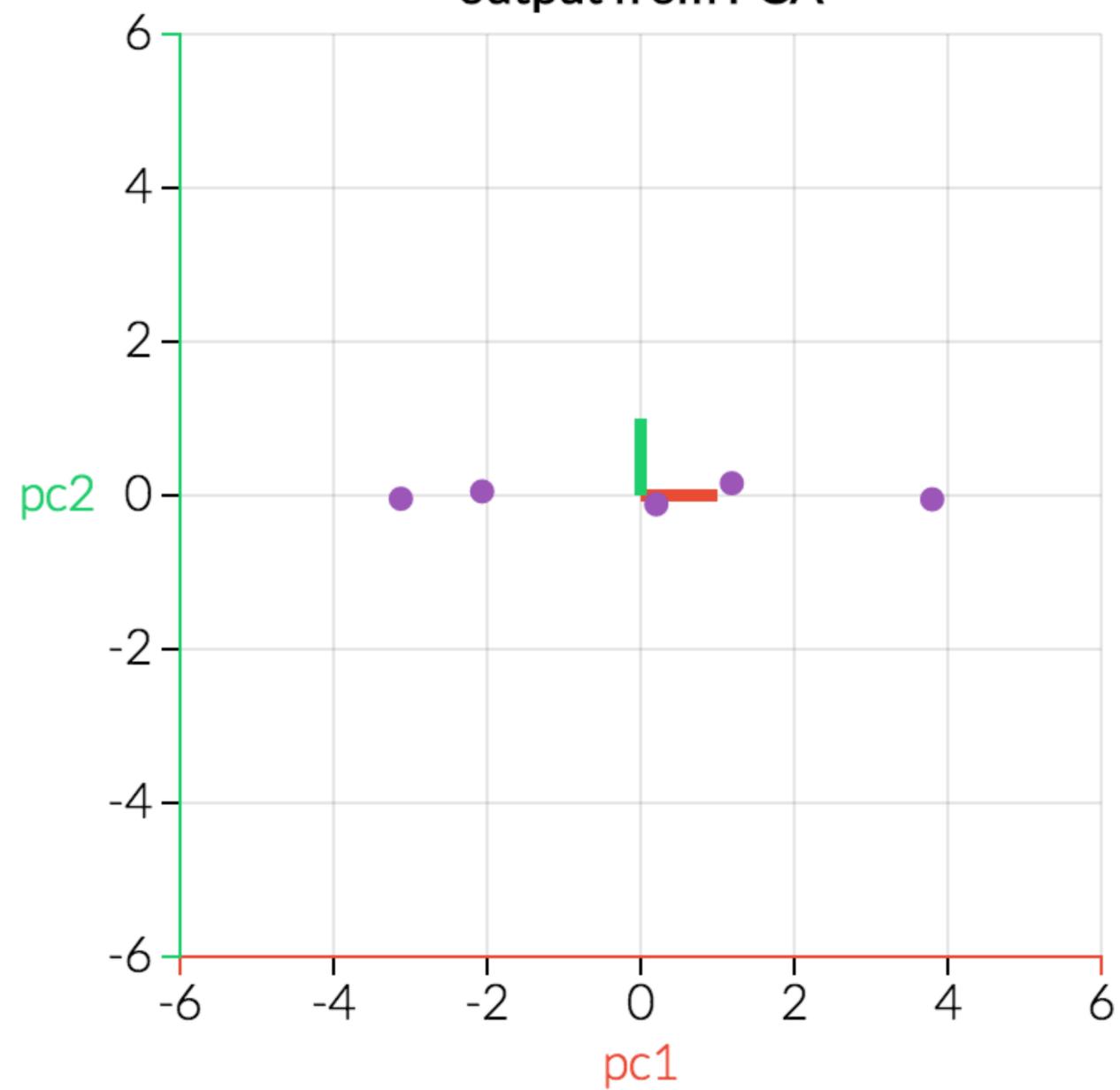


# PCA

original data set



output from PCA



# Multidimensional Scaling

Multiple approaches

Works based on projecting a similarity matrix

How do you compute similarity?

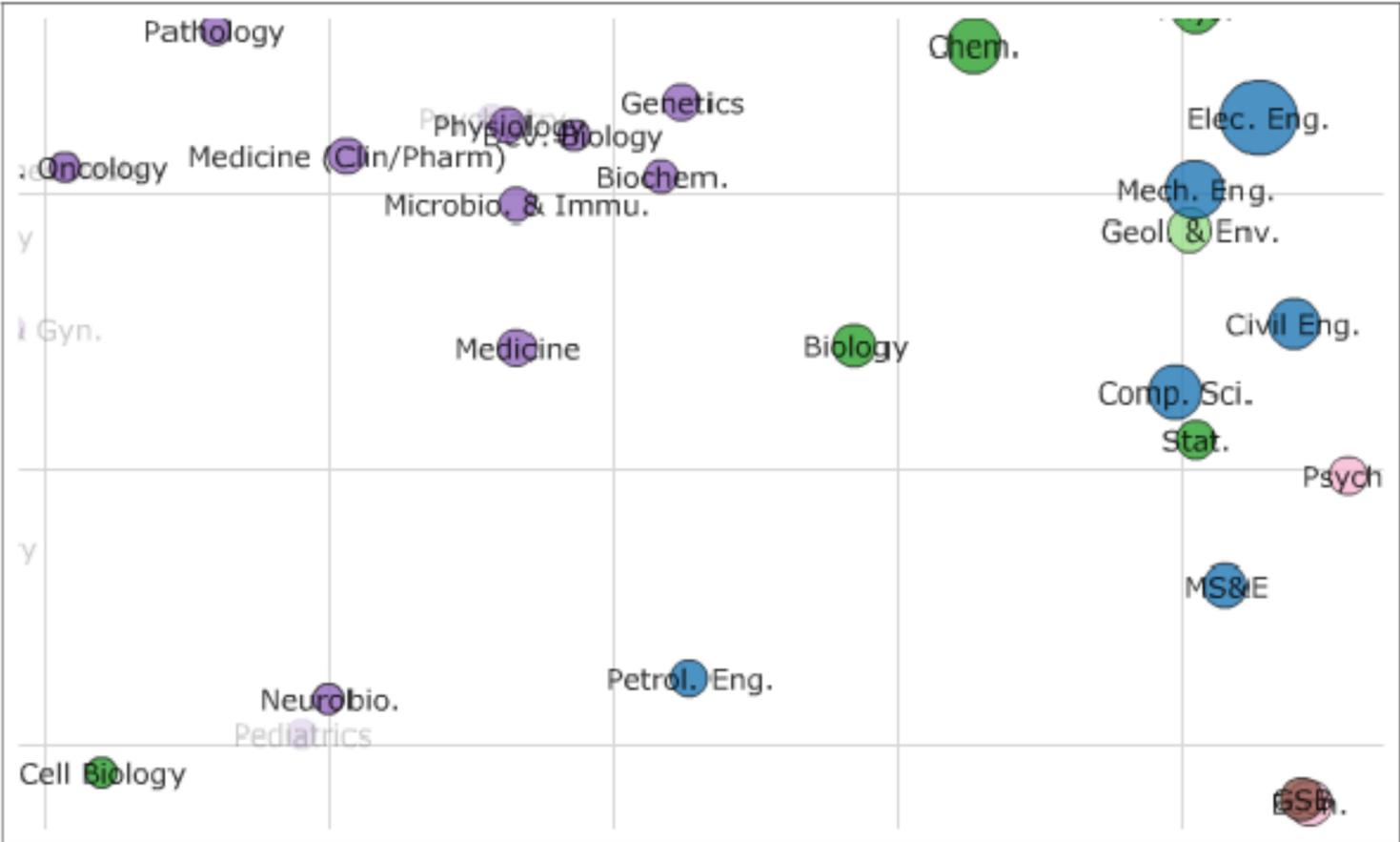
How do you project the points?

Popular for text analysis

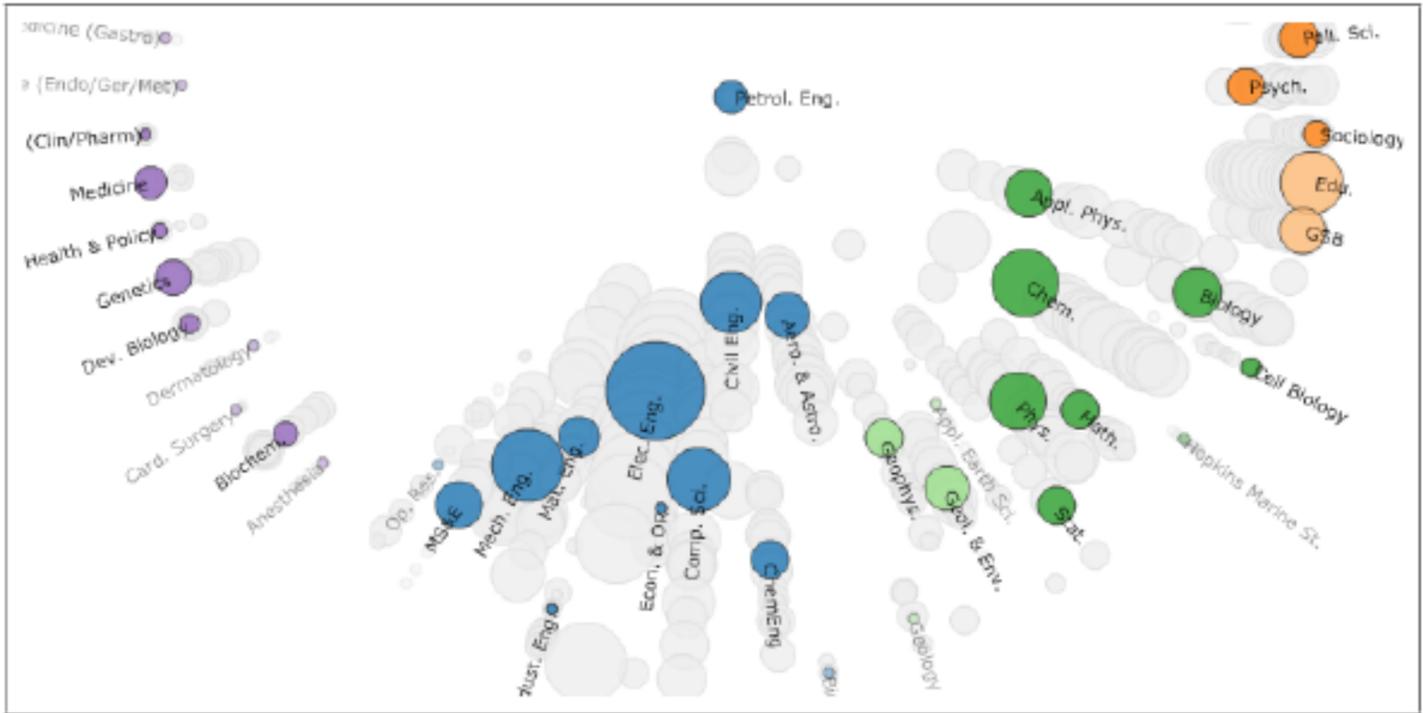


# Can we Trust Dimensionality Reduction?

Topical distances between departments in a 2D projection



Topical distances between the selected Petroleum Engineering and the others.



[Chuang et al., 2012]

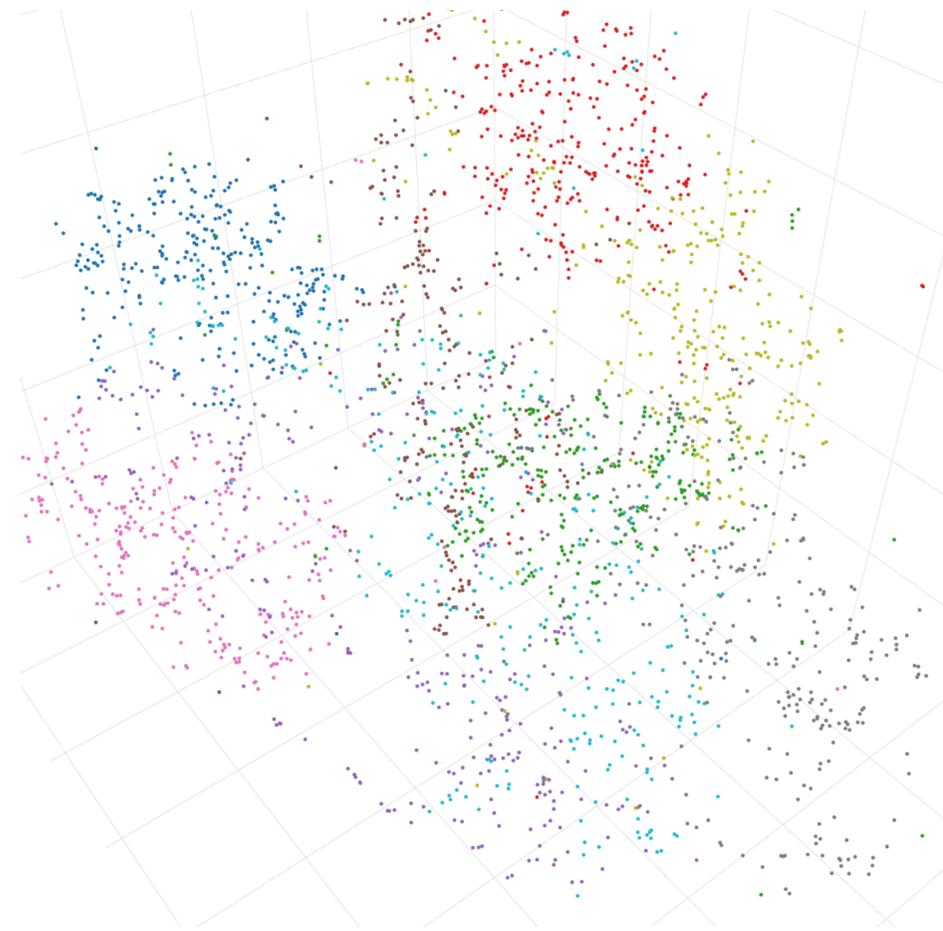
# Probing Projections



# t-SNE

t-distributed stochastic neighbor embedding

non-linear algorithm: different transformations for different regions



# How to Use t-SNE Effectively

Although extremely useful for visualizing high-dimensional data, t-SNE plots can sometimes be mysterious or misleading. By exploring how it behaves in simple cases, we can learn to use it more effectively.



Step  
5,000

Two clusters with equal  
numbers of points.

[Share this view](#)

Points Per Cluster 50



Dimensions 2



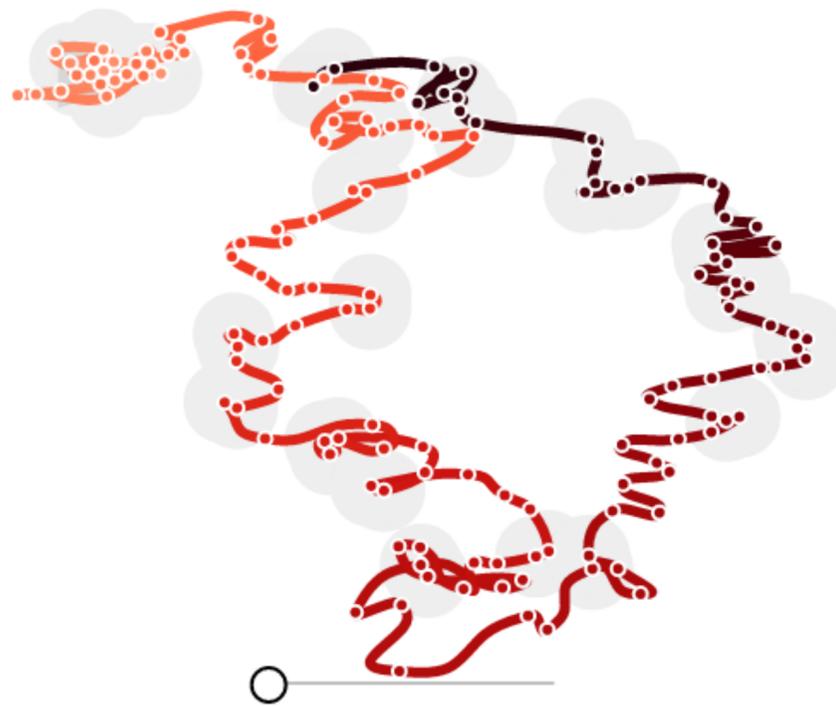
Perplexity 10



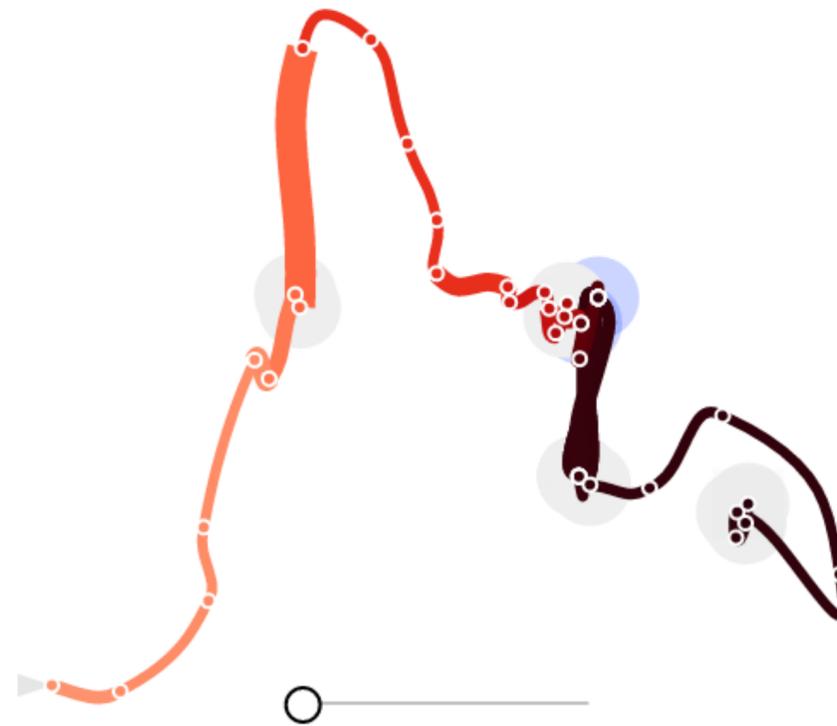
Epsilon 5



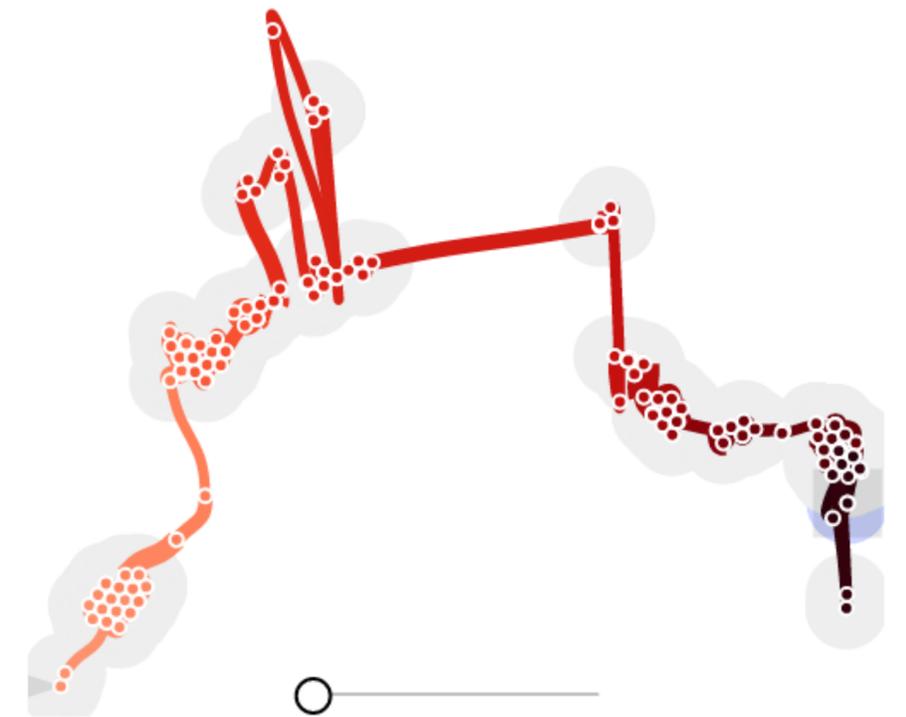
# MDS for Temporal Data: TimeCurves



Video: Global Cloud Circulation (146)



Wikipedia: Chocolate (46) 



Wikipedia: Palestine 200 1 (200) 