CS-5630 / CS-6630 Visualization for Data Science
Filtering & Aggregation

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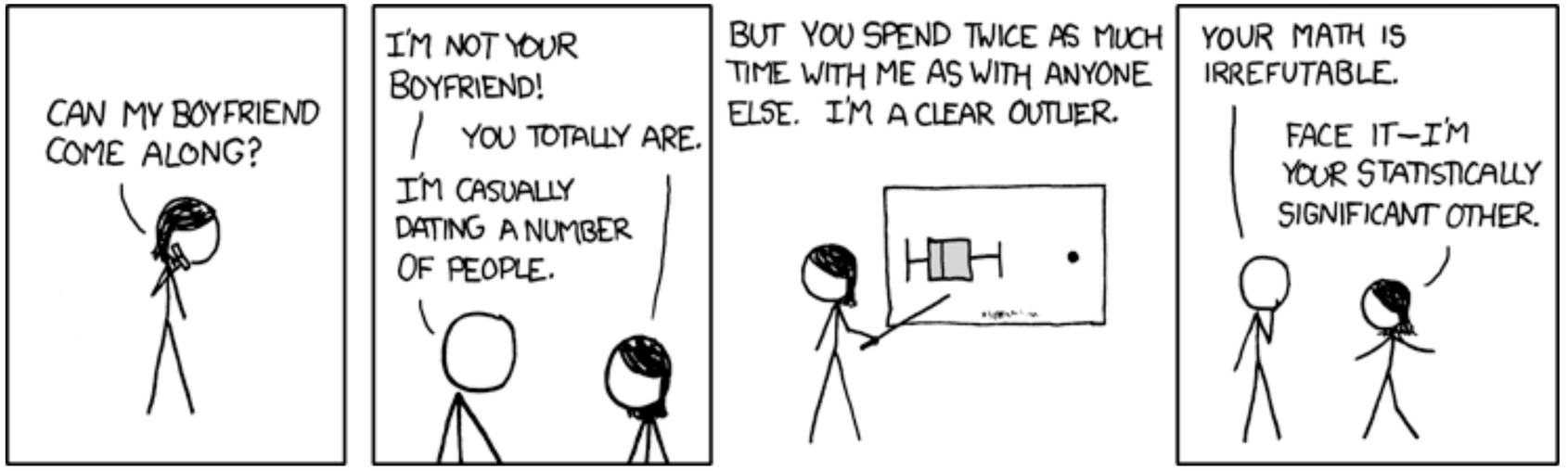
THE UNIVERSITY OF UTAH



[xkcd]

Reducing Items and Attributes

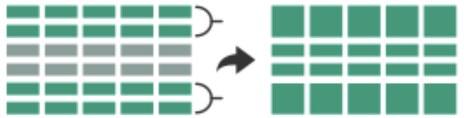
Filter

- Items

- Attributes

Aggregate

- Items



- Attributes

Filter

elements are eliminated

What drives filters?

Any possible function that partitions a dataset into two sets

- Bigger/smaller than x
- Fold-change
- Noisy/insignificant

Dynamic Queries / Filters

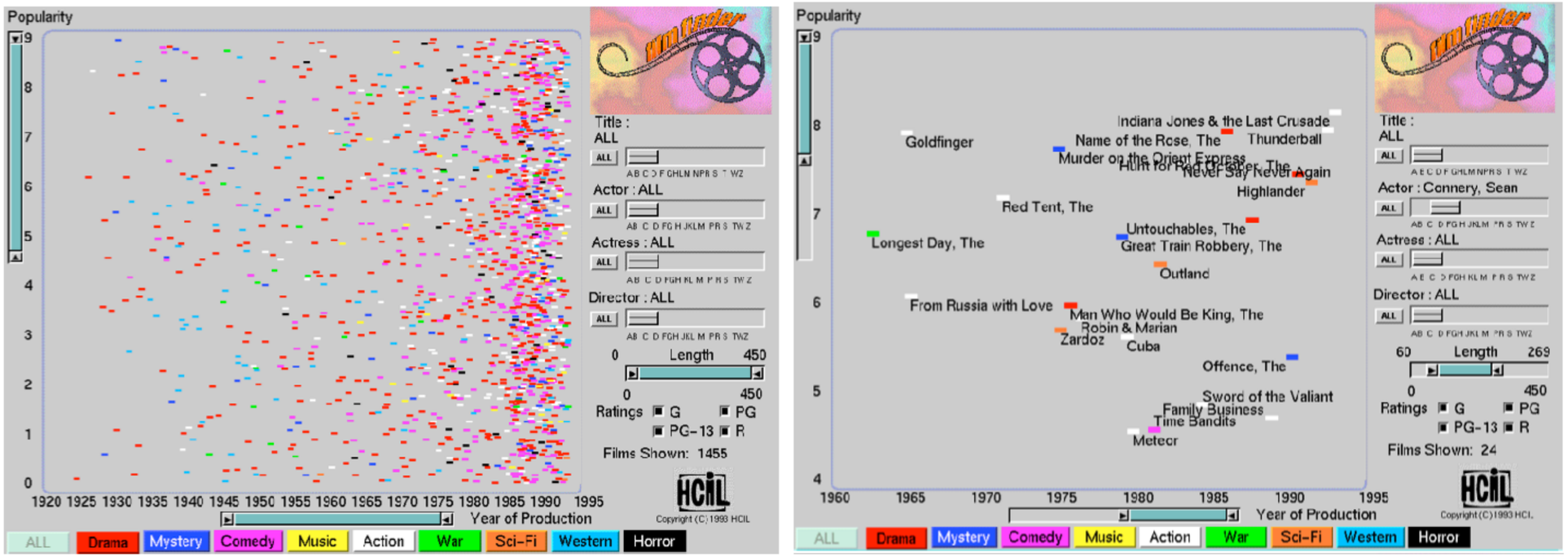
coupling between encoding and interaction so that user can immediately see the results of an action

Queries: start with 0, add in elements

Filters: start with all, remove elements

Approach depends on dataset size

ITEM FILTERING



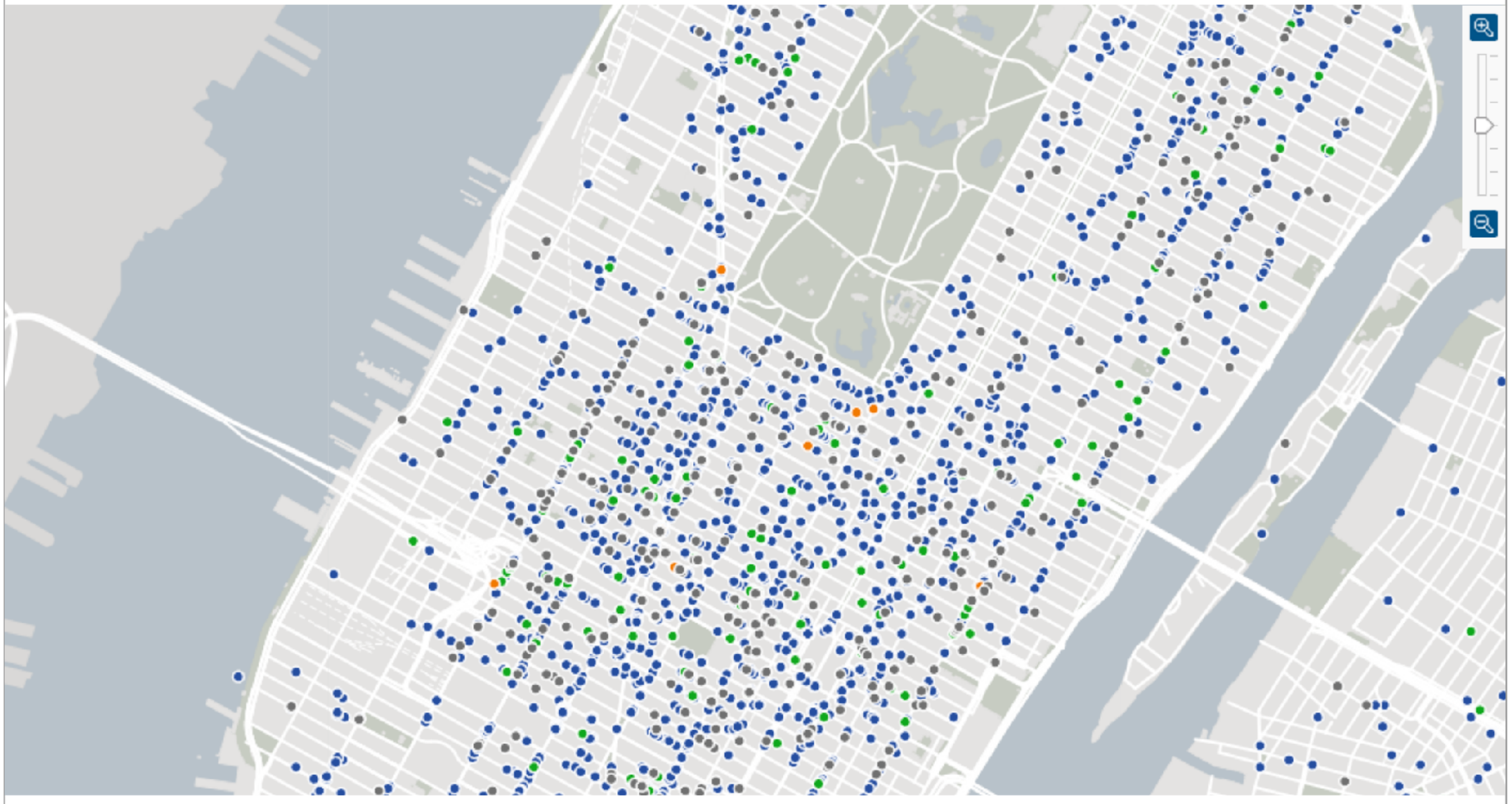
Ahlberg 1994

FIND A RESTAURANT | FIND A LOCATION

Name of restaurant

FILTER

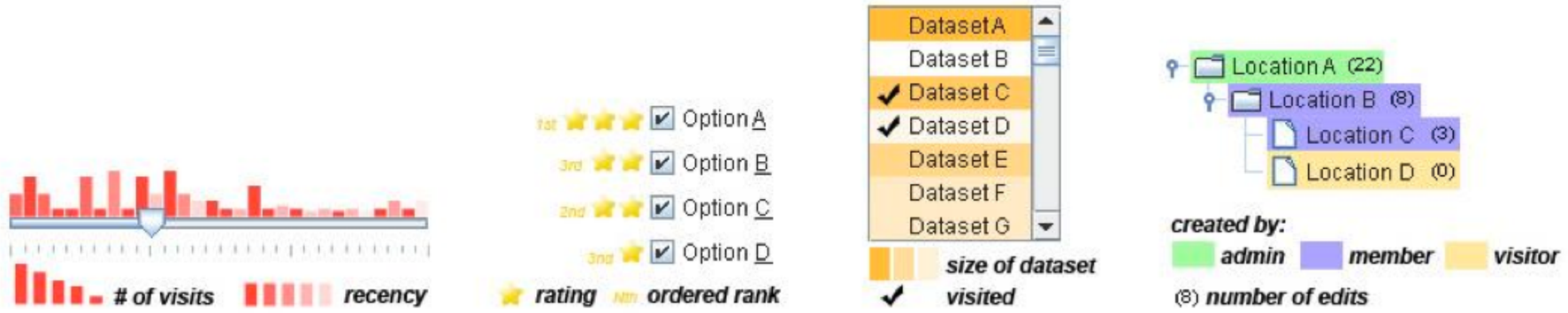
All grades | All violations | All cuisines



Scented Widgets

information scent: user's (imperfect) perception of data

GOAL: lower the cost of information foraging through better cues

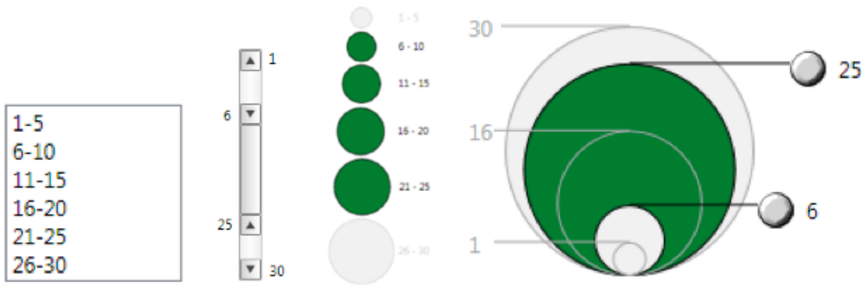


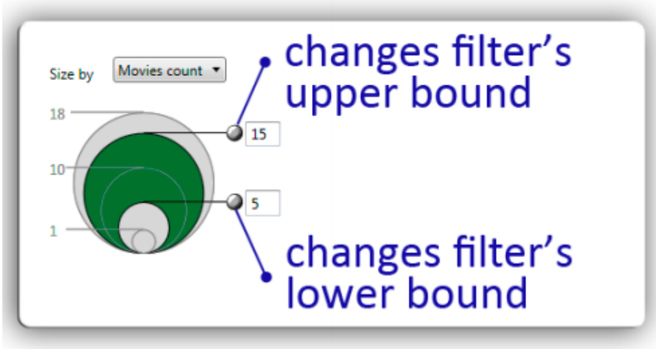
Willett 2007

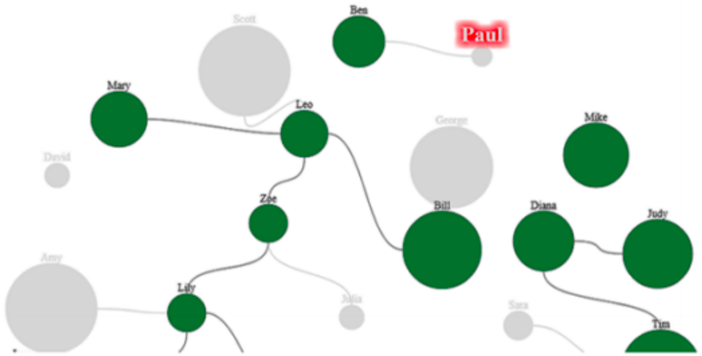
Interactive Legends

Controls combining the visual representation of static legends with interaction mechanisms of widgets

Define and control visual display together





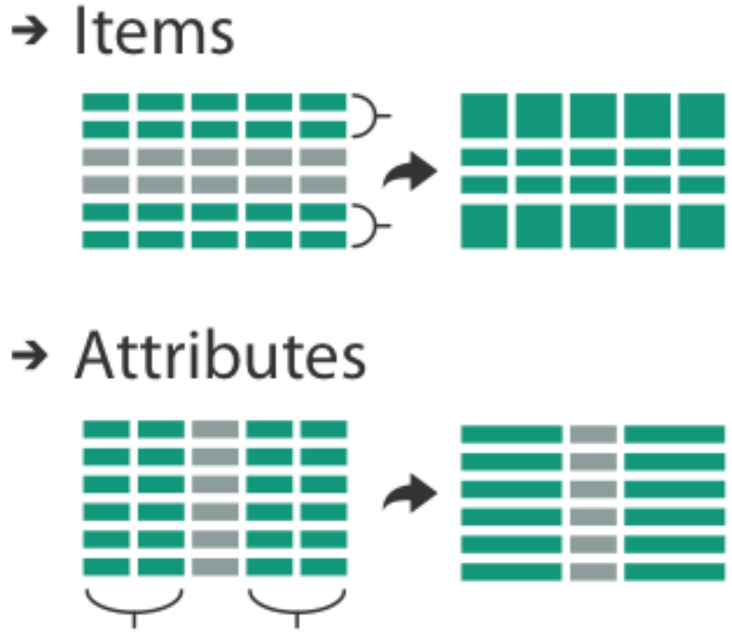


Riche 2010

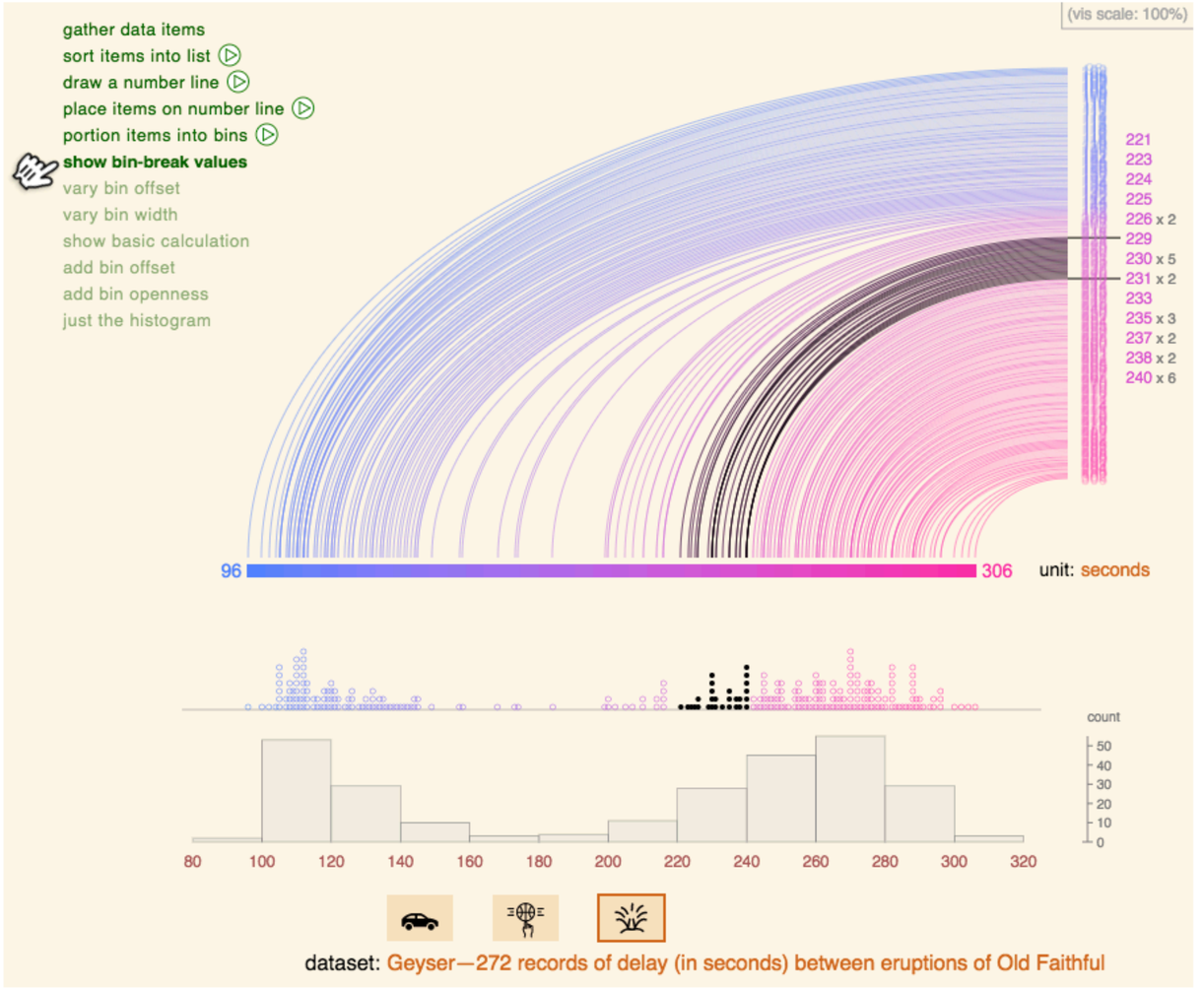
Aggregation

Aggregate

a group of elements is represented by a (typically smaller) number of derived elements



Histograms Explained



http://tinlizzie.org/histograms/

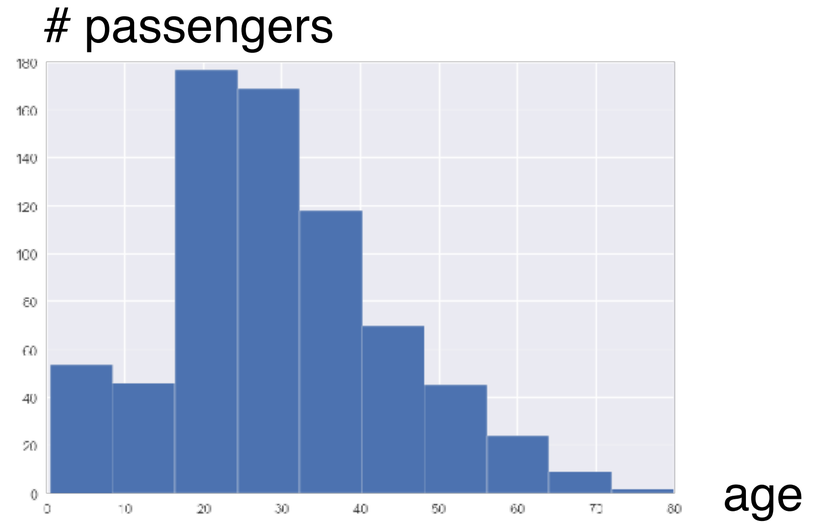
Histogram

Good #bins hard to predict

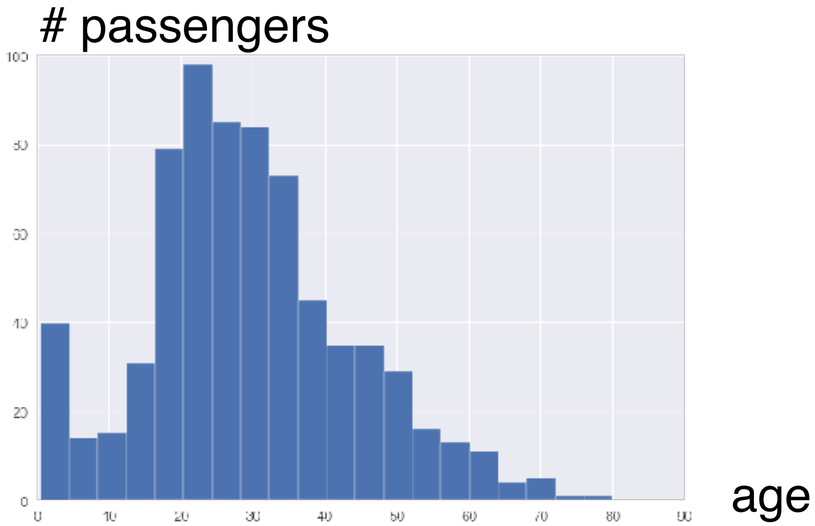
make interactive!

rules of thumb:

- #bins = sqrt(n)
- #bins = log2(n) + 1

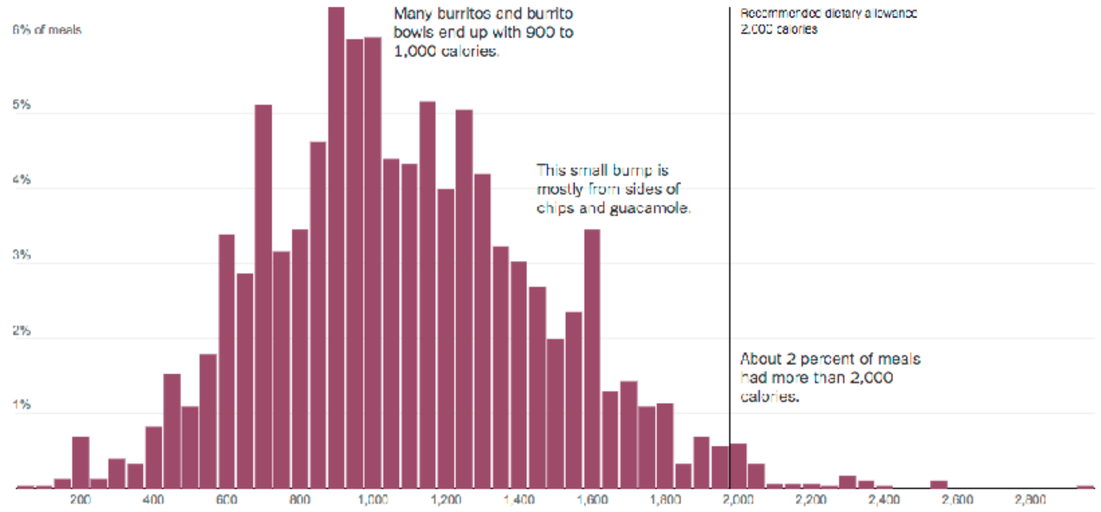


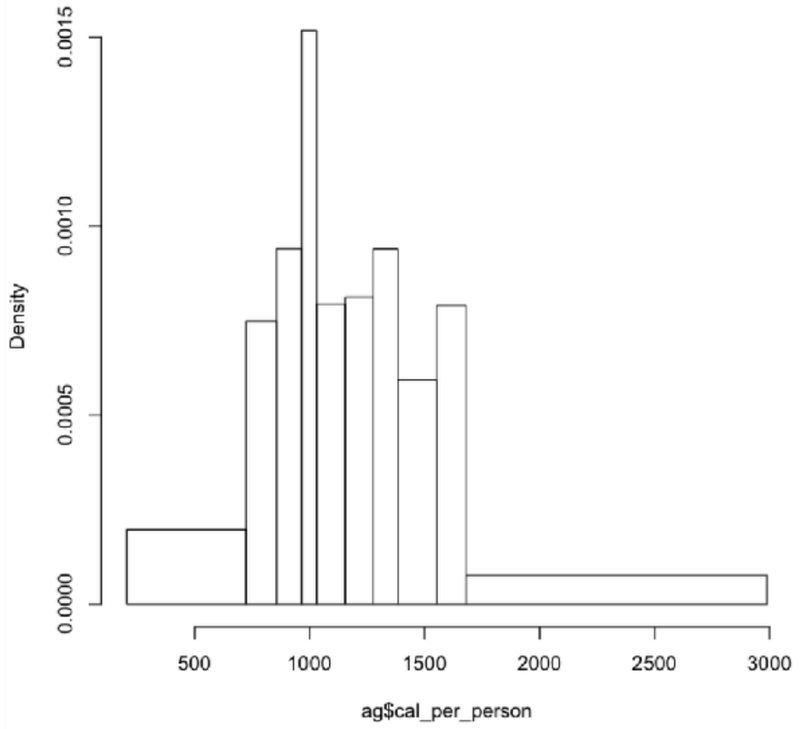
10 Bins



20 Bins

Unequal Bin Width

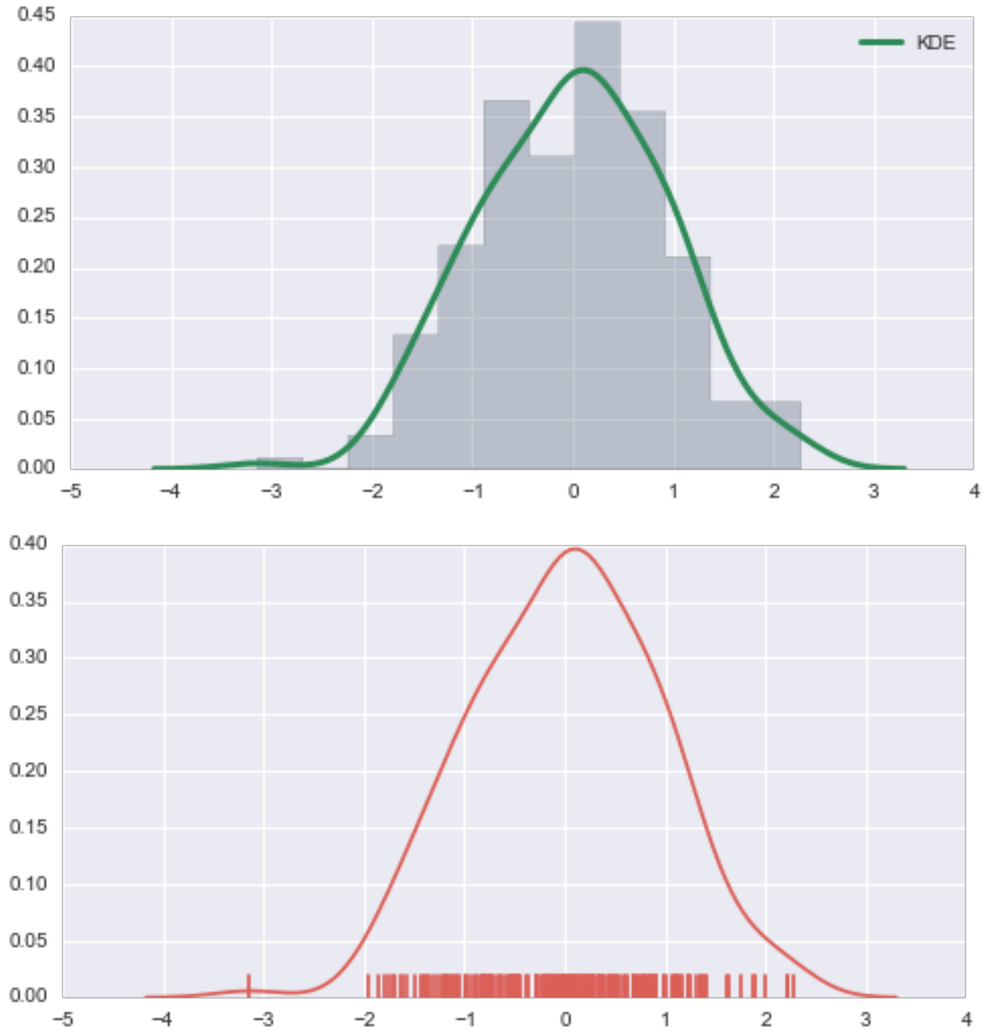




Can be useful if data is much sparser in some areas than others
Show density as area, not hight.

https://www.nytimes.com/interactive/2015/02/17/upshot/what-do-people-actually-order-at-chipotle.html?_r=1

Density Plots



http://web.stanford.edu/~mwaskom/software/seaborn/tutorial/plotting_distributions.html

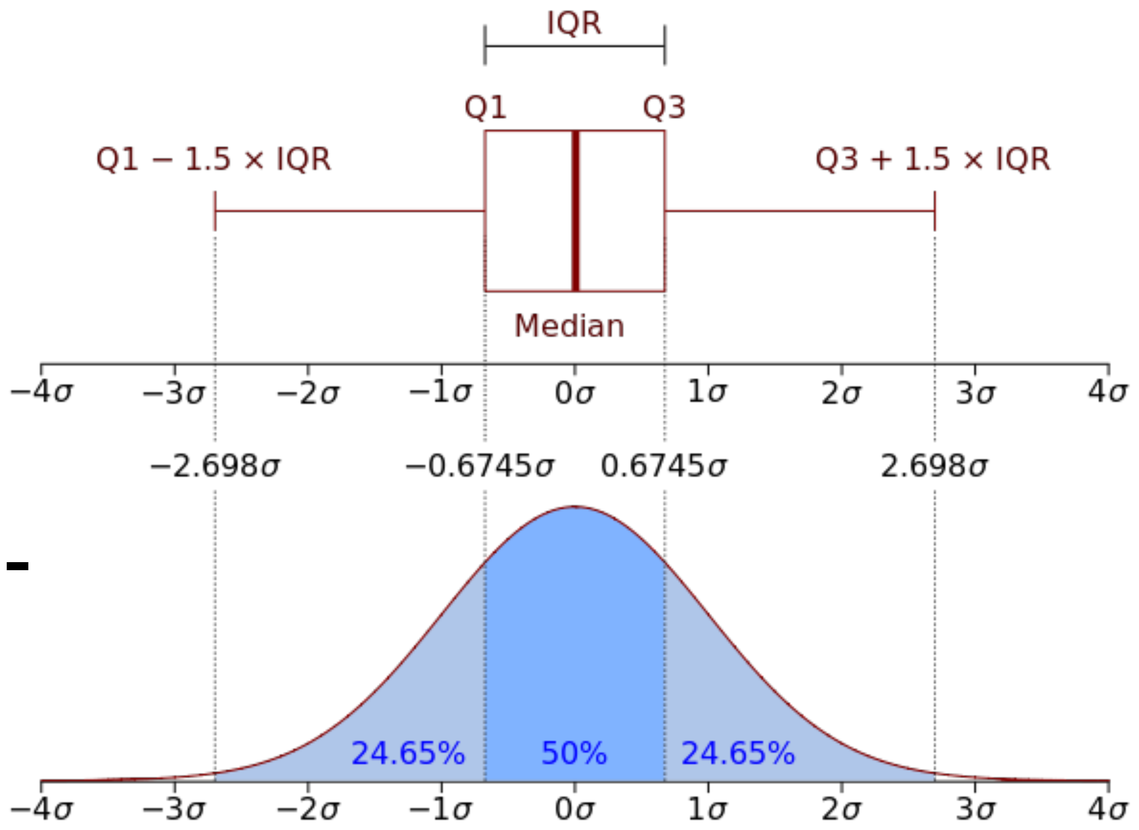
Box Plots

aka Box-and-Whisker Plot

Show outliers as points!

Not so great for non-normal distributed data

Especially bad for bi- or multi-modal distributions



Wikipedia

One Boxplot, Four Distributions

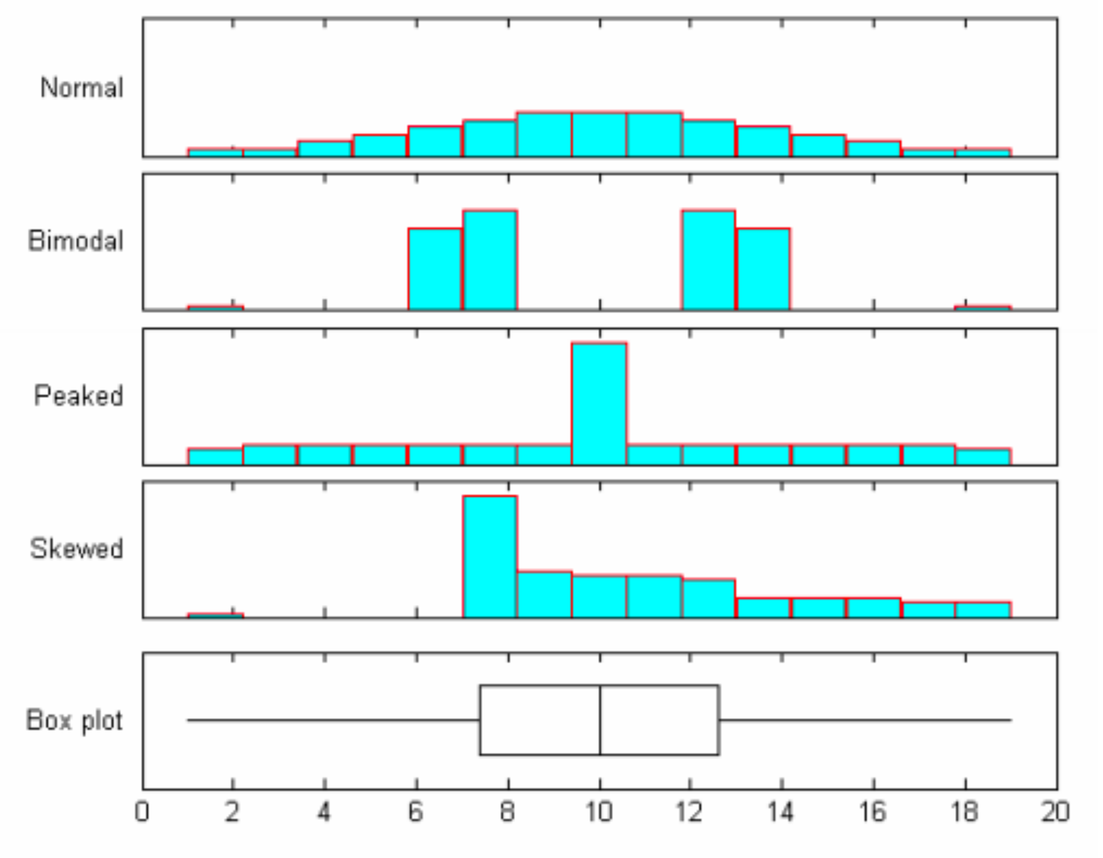


Figure 1: Histograms and box plot: four samples each of size 100

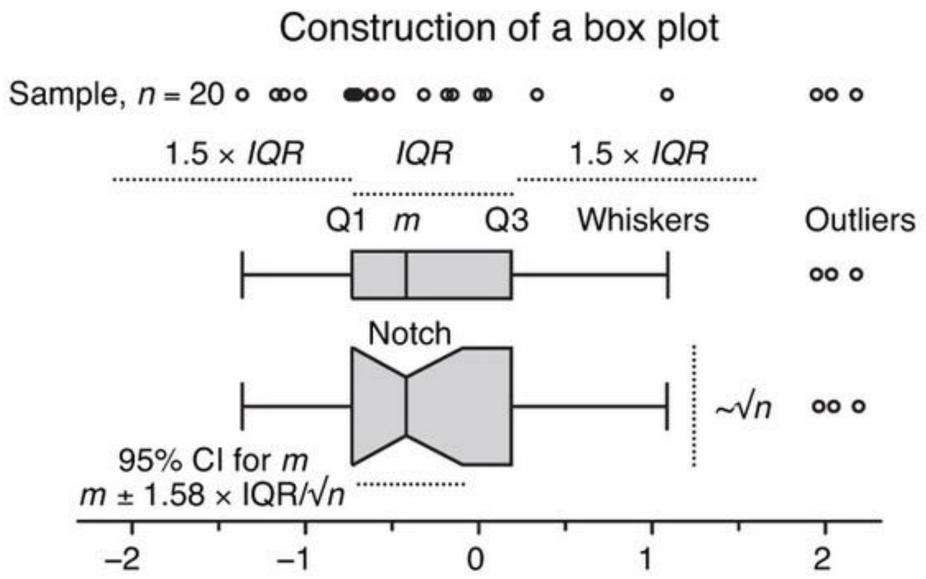
http://stat.mq.edu.au/wp-content/uploads/2014/05/Can_the_Box_Plot_be_Improved.pdf

Notched Box Plots

Notch shows
m +/- 1.5i x IQR/sqrt(n)

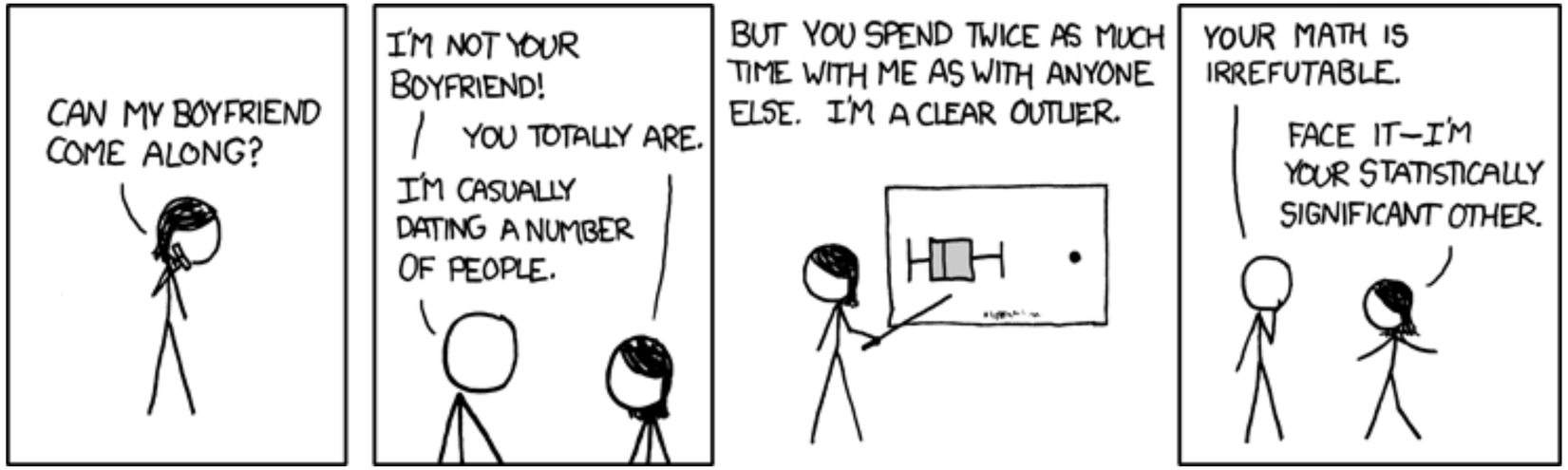
-> 95% Confidence Intervall

A guide to statistical significance.

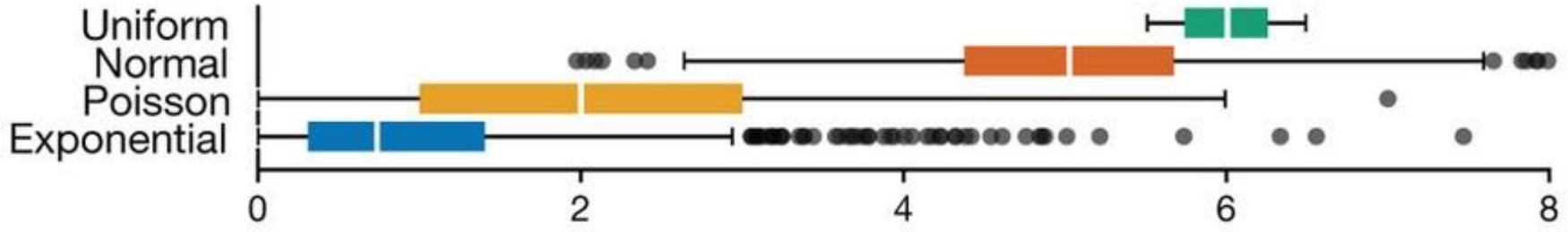


Kryzwinski & Altman, PoS, Nature Methods, 2014

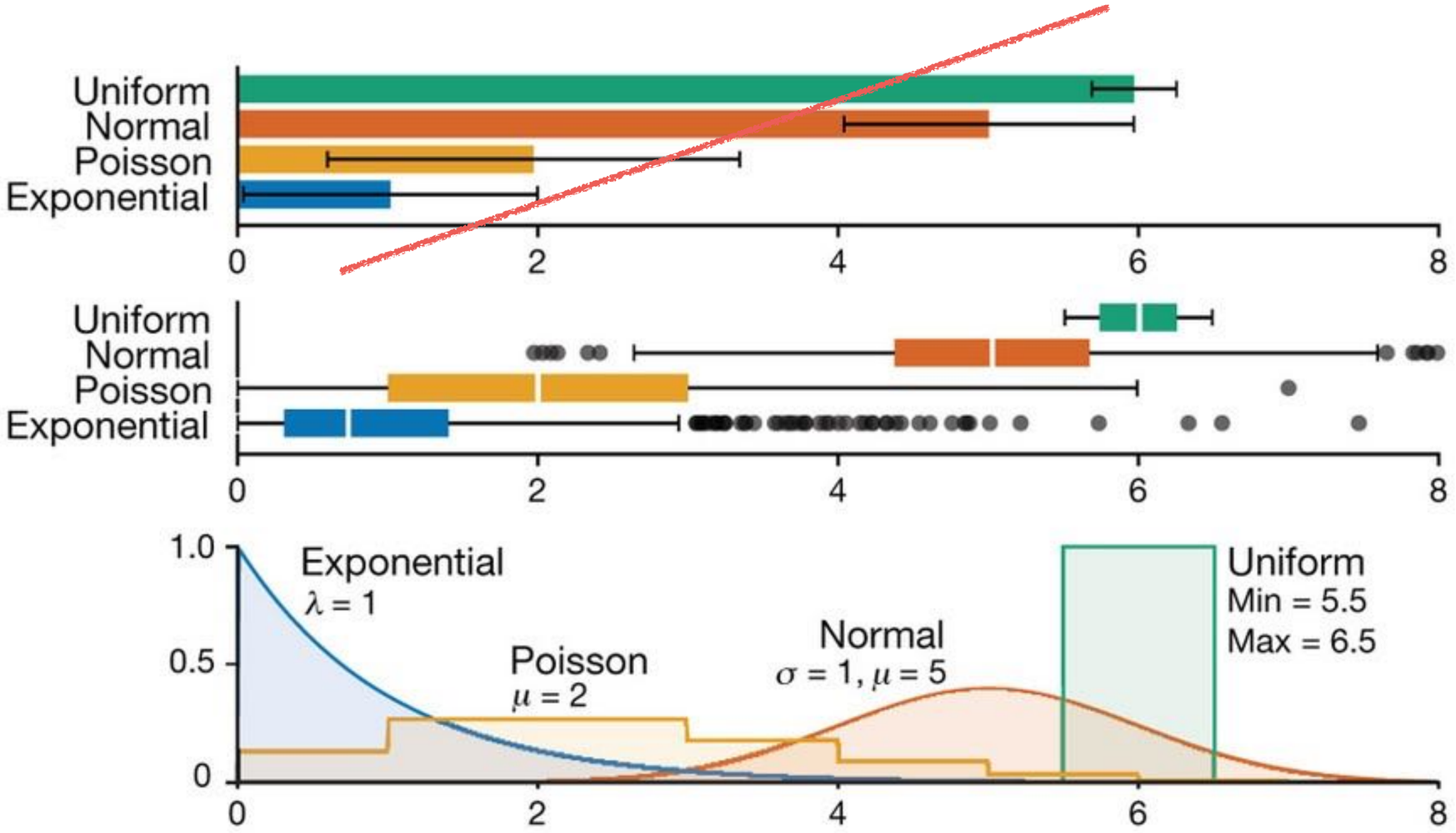
Box(and Whisker) Plots



http://xkcd.com/539/

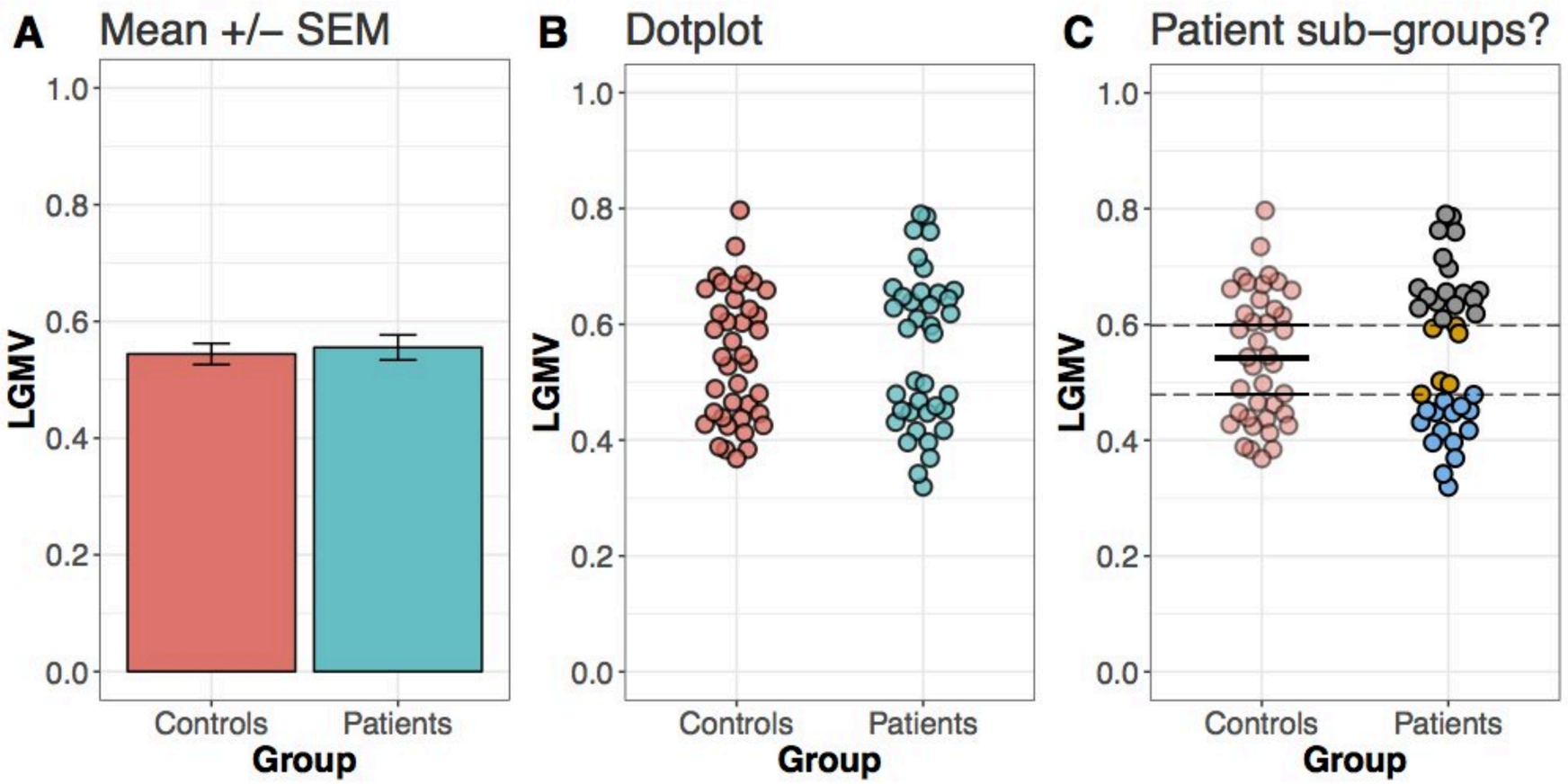


Comparison



Streit & Gehlenborg, PoV, Nature Methods, 2014

Bar Charts vs Dot Plots

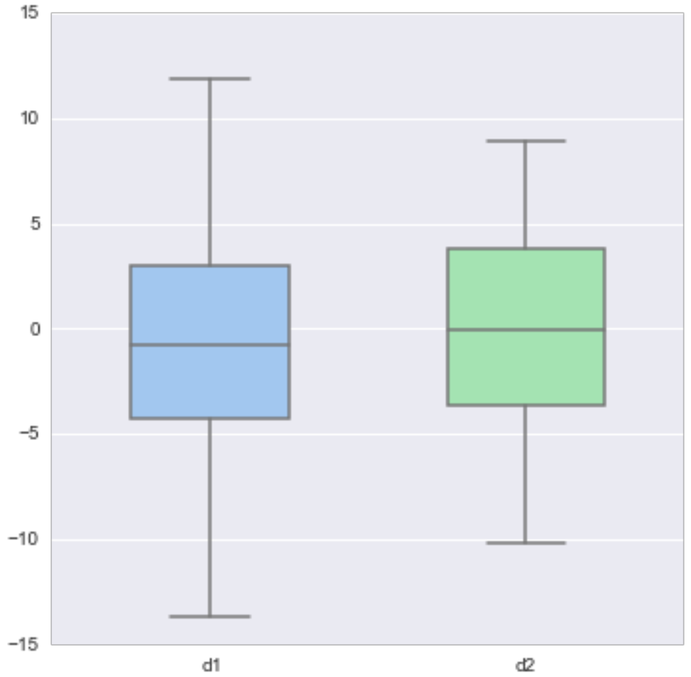


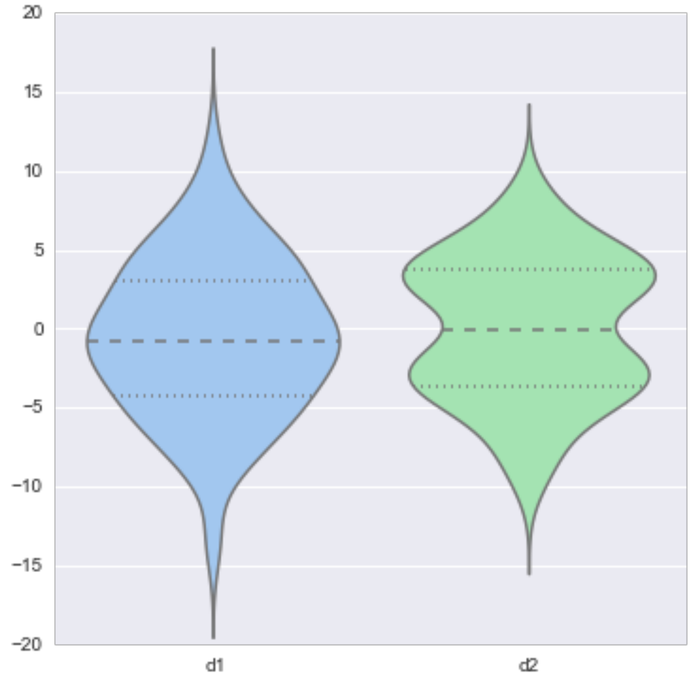
Data Source https://bmcneurosci.biomedcentral.com/articles/10.1186/1471-2202-10-67

https://twitter.com/robustgar/status/859318971920769024

Violin Plot

= Box Plot + Probability Density Function

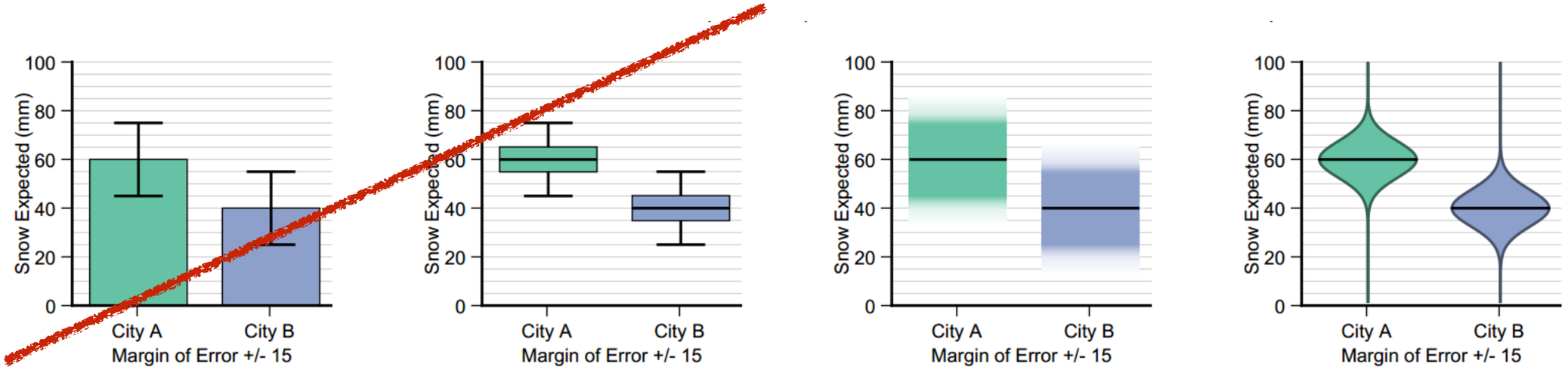




http://web.stanford.edu/~mwaskom/software/seaborn/tutorial/plotting_distributions.html

Showing Expected Values & Uncertainty

NOT a distribution!

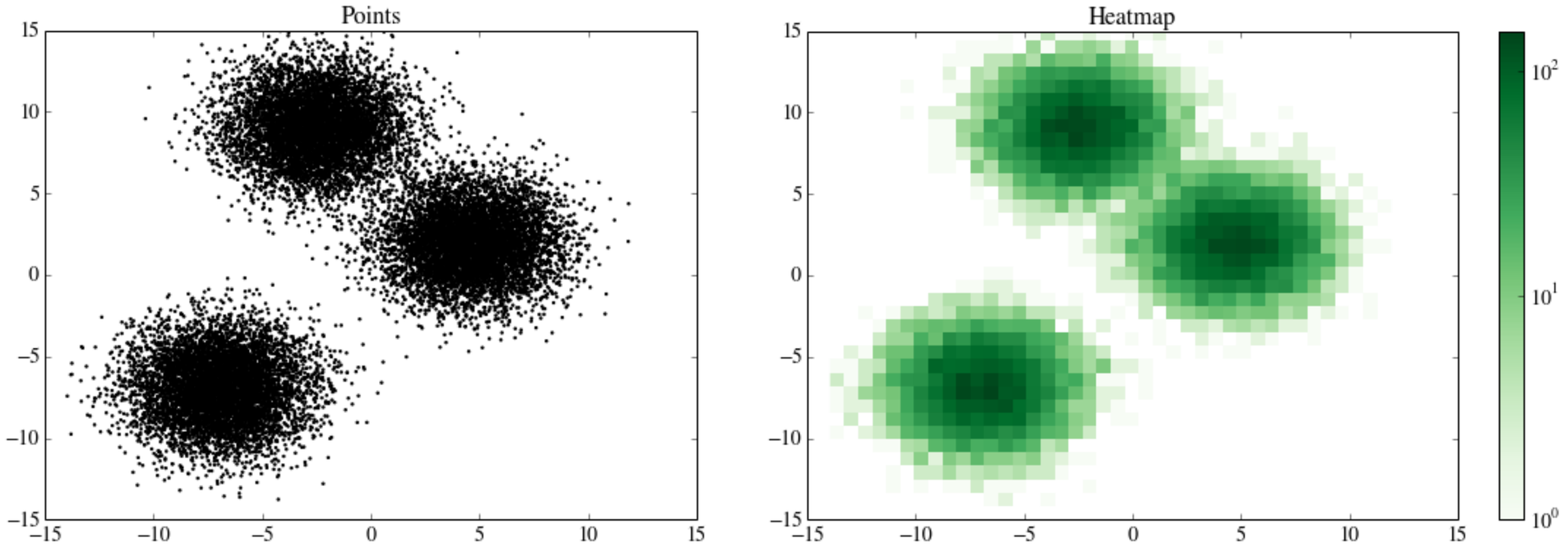


Error Bars Considered Harmful:
Exploring Alternate Encodings for Mean and Error
Michael Correll, and Michael Gleicher

Heat Maps

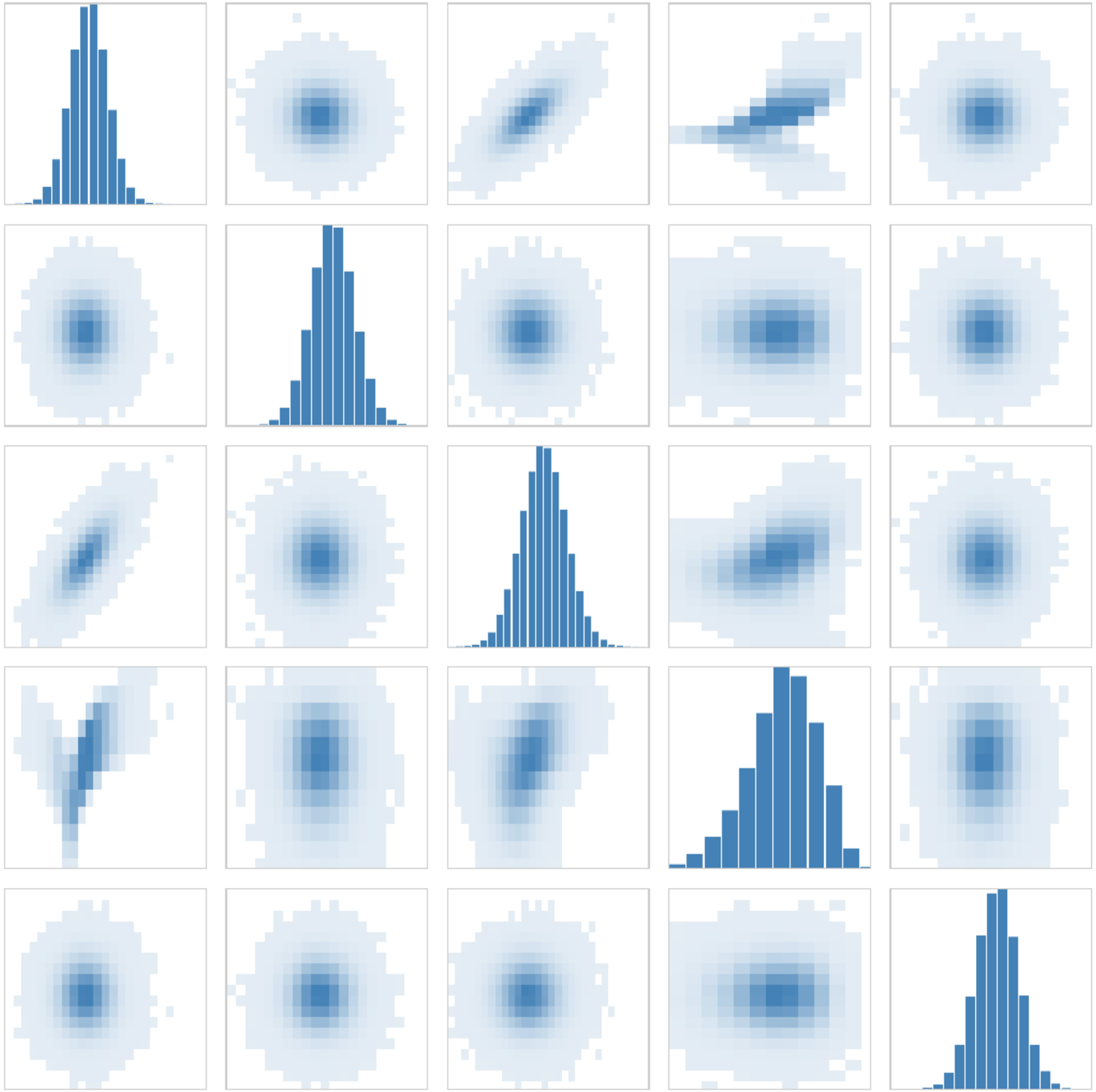
binning of scatterplots

instead of drawing every point, calculate grid and intensities



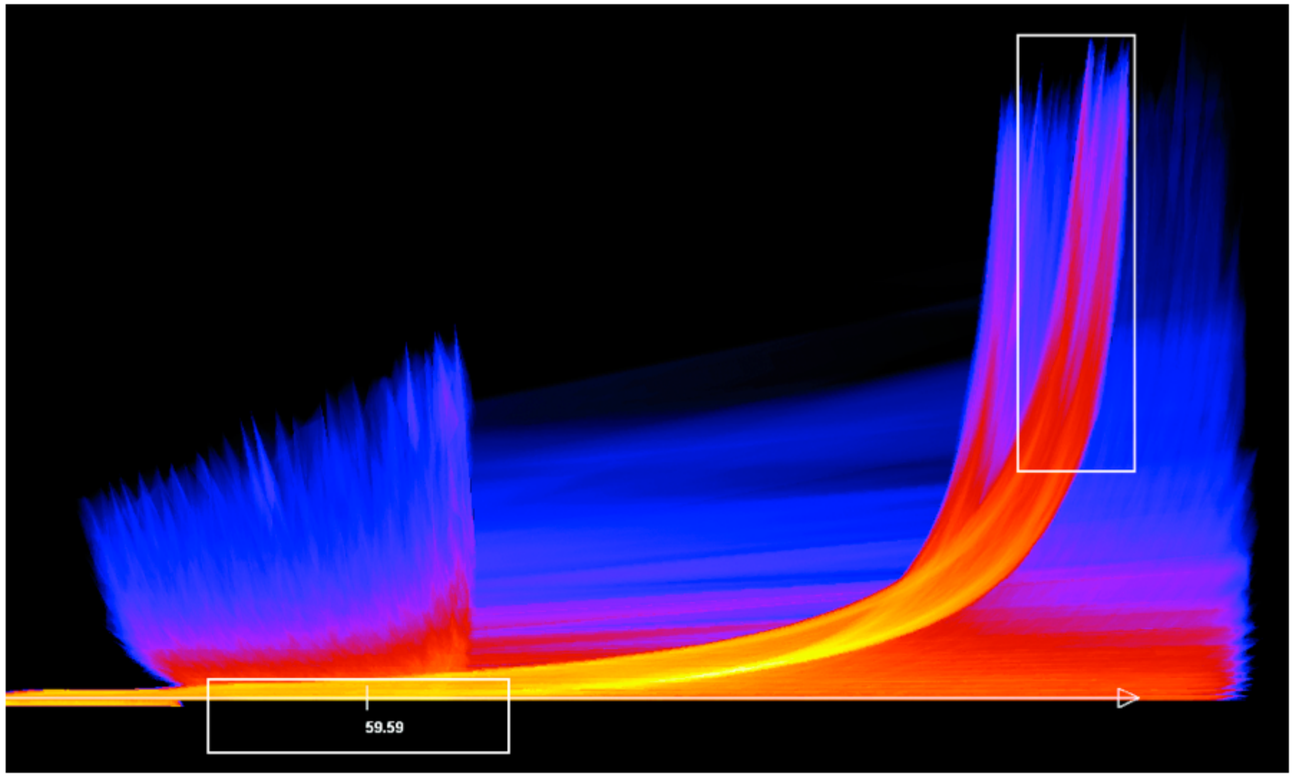
2D Density Plots

Interactive Binned Scatterplot Matrix Dimensions: 5 Bins: 20 Data Points: 100k



Powered by Datavore and D3.

Continuous Scatterplot



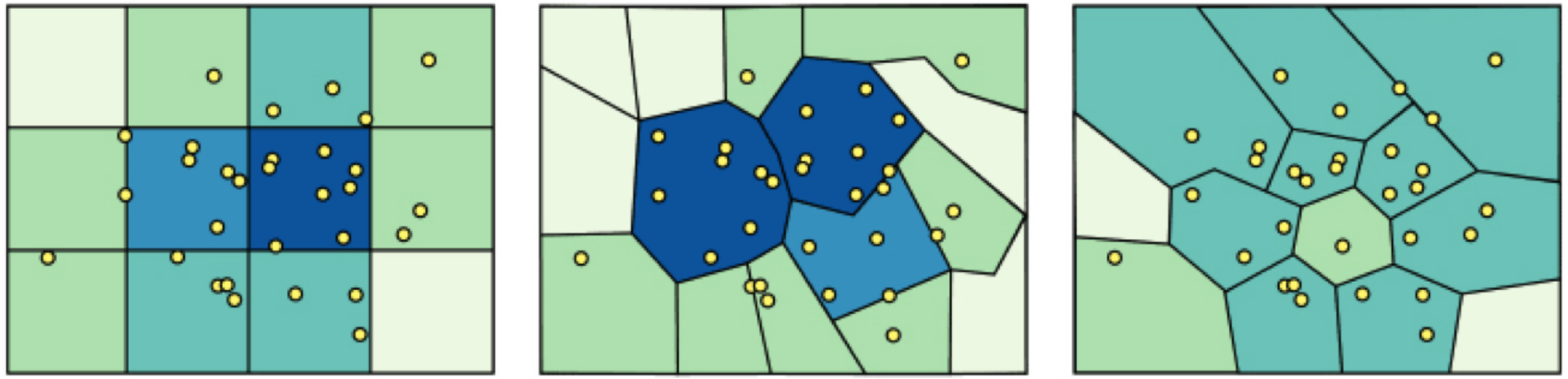
Bachthaler 2008

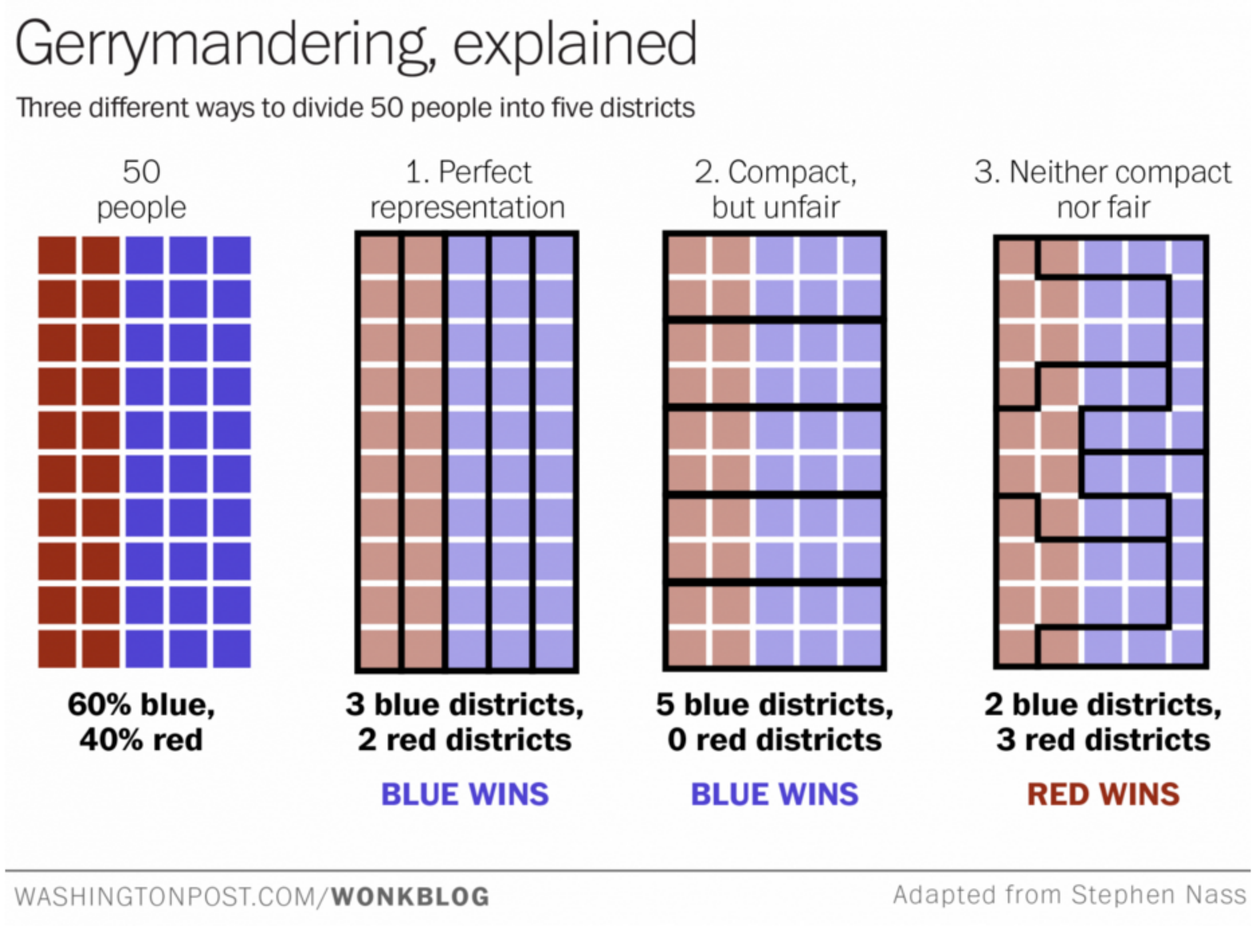
Spatial Aggregation

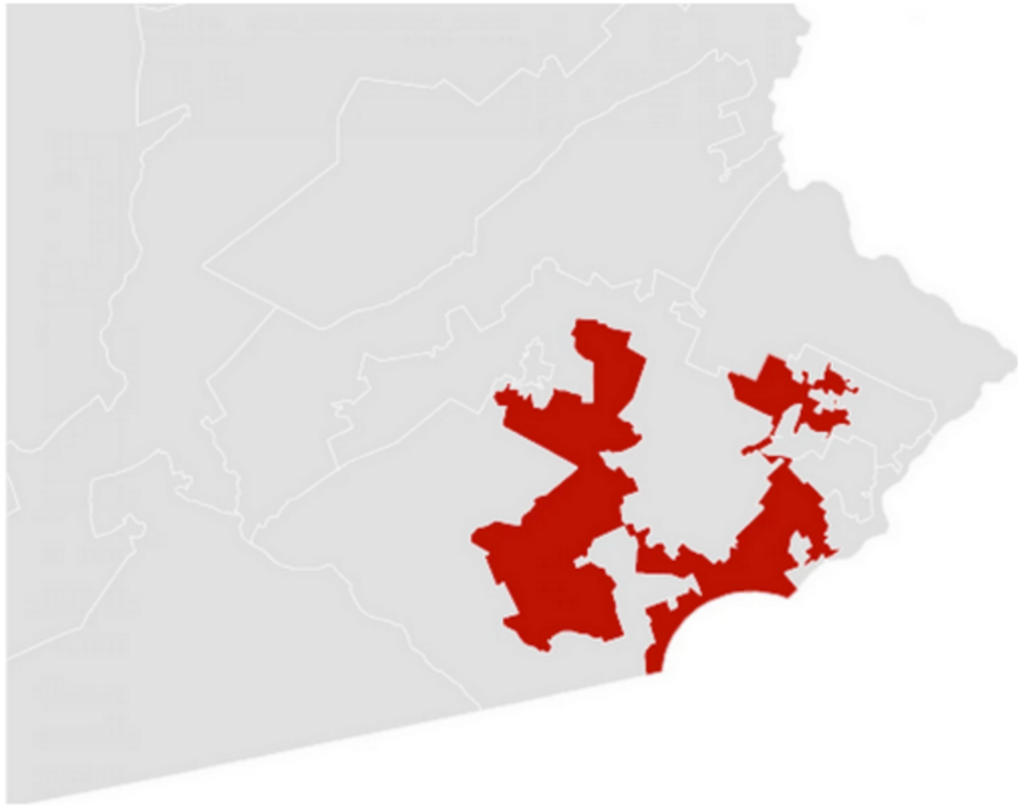
Spatial Aggregation

modifiable areal unit problem

in cartography, changing the boundaries of the regions used to analyze data can yield dramatically different results

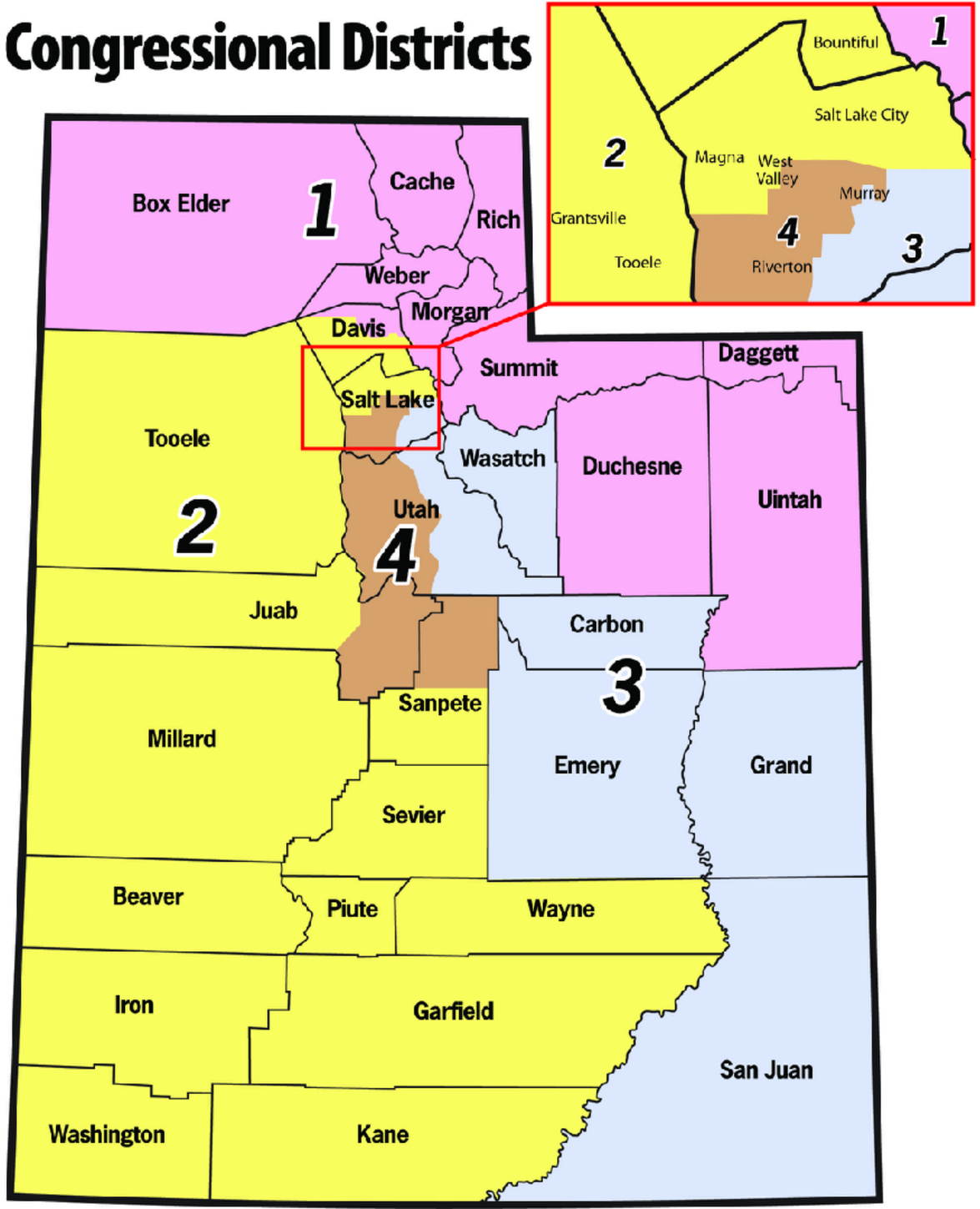


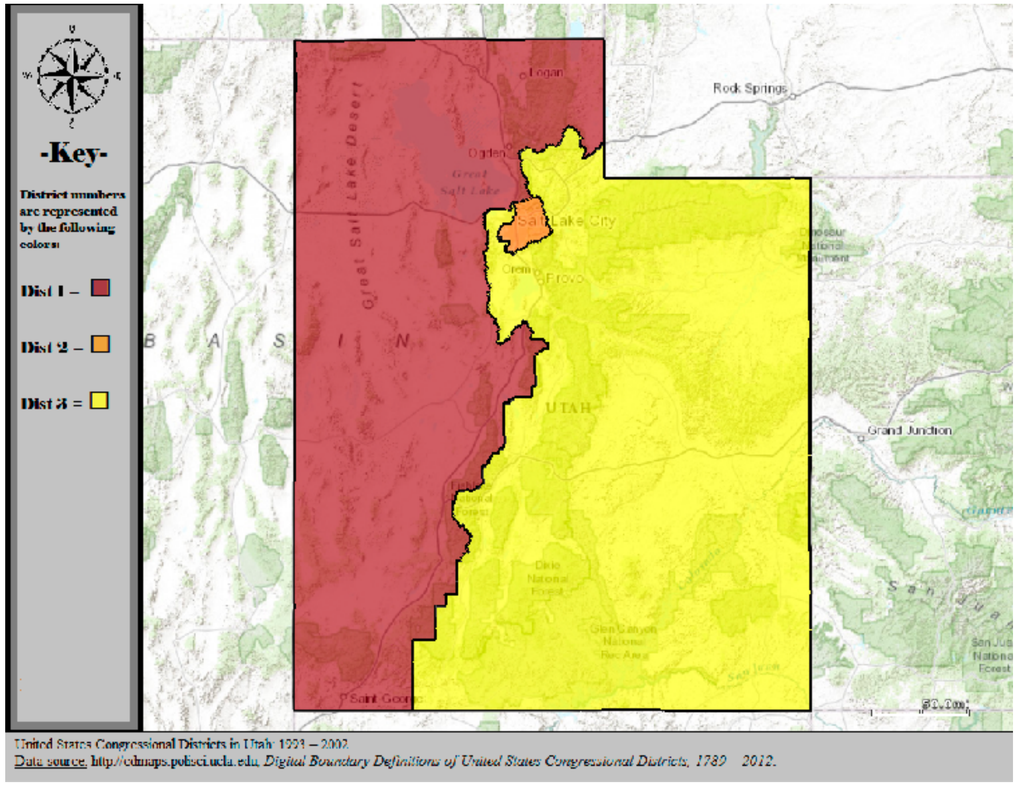




A real district in Pennsylvania
Democrats won 51% of the vote
but only 5 out of 18 house seats

Congressional Districts



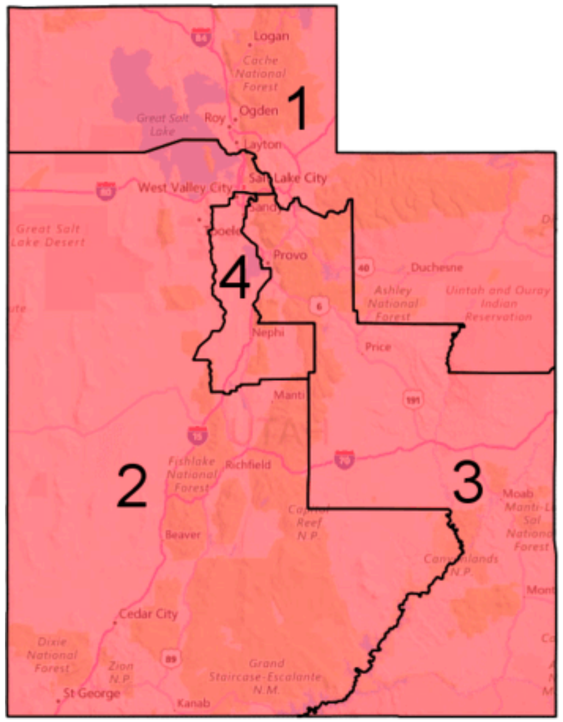


Valid till 2002

http://www.sltrib.com/opinion/1794525-155/lake-salt-republican-county-http-utah

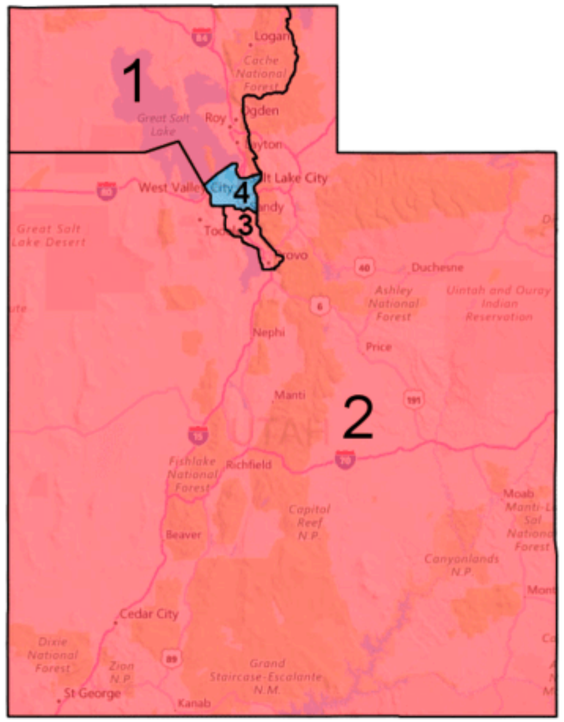
2016 Congressional Elections

Utah's Republican Congressional Map



2016 Outcome
Republican (4)

Hypothetical Nonpartisan Map



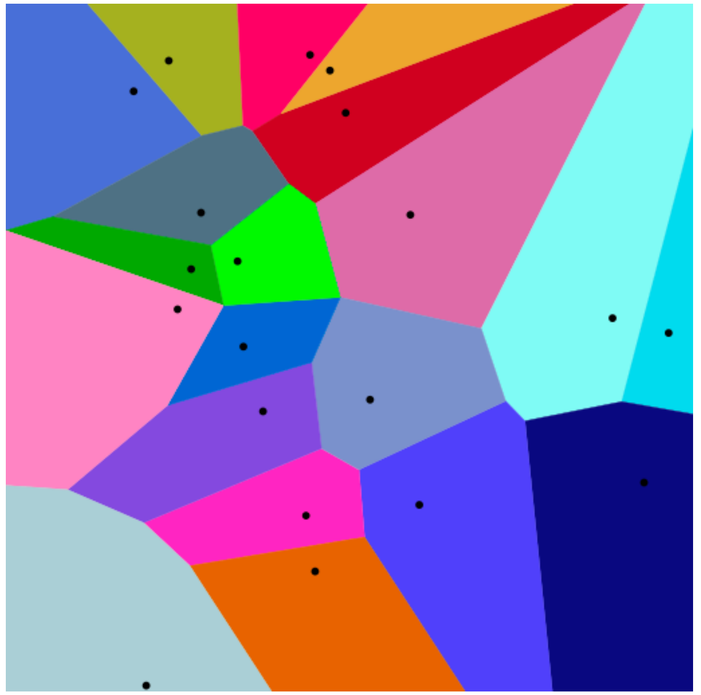
Predicted Outcome
Democratic (1)
Republican (3)

DAILY KOS ELECTIONS

https://www.dailykos.com/stories/2016/12/29/1611906/-Here-s-what-Utah-might-have-looked-like-in-2016-without-congressional-gerrymandering

Voronoi Diagrams

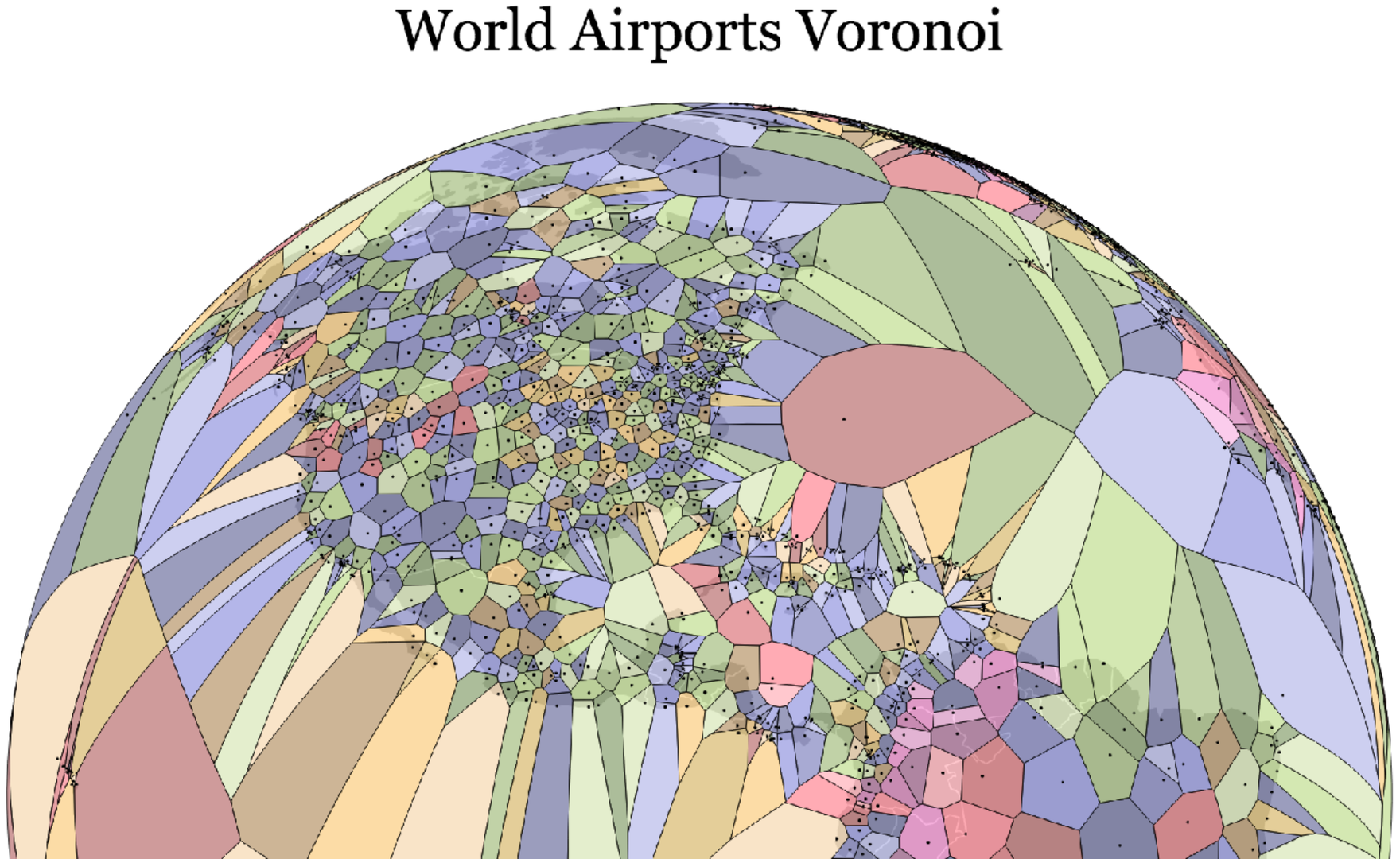
Given a set of locations, for which area is a location n closest?



D3 Voronoi Layout:

https://github.com/d3/d3-voronoi

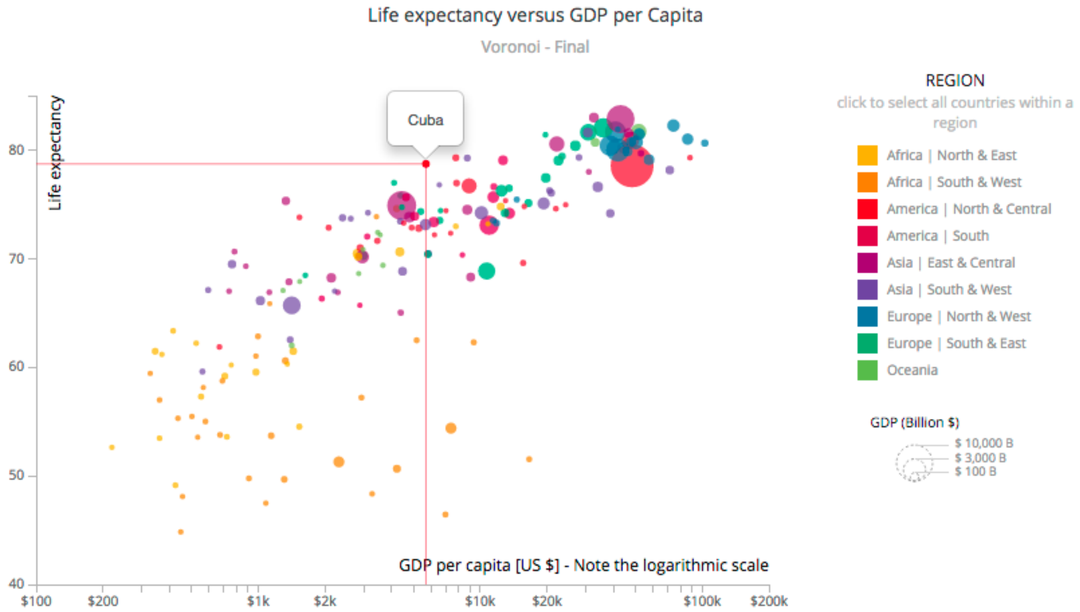
Voronoi Examples



Voronoi for Interaction

Useful for interaction:
Increase size of target area to click/hover

Instead of clicking on point, hover in its region



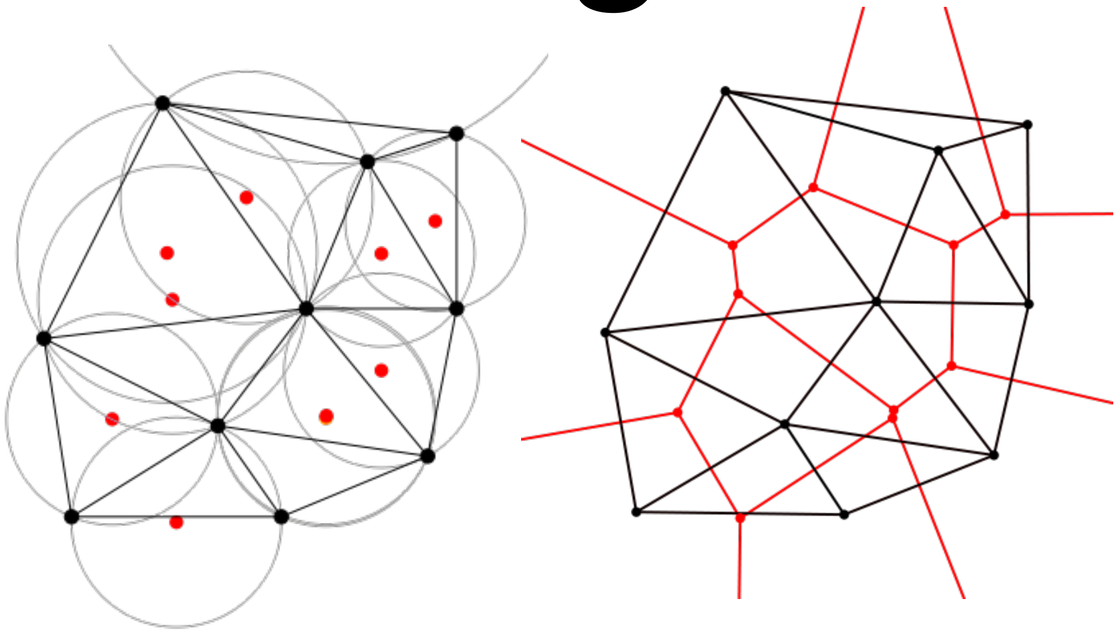
https://github.com/d3/d3-voronoi/

Constructing a Voronoi Diagram

Calculate a Delauney triangulation

- Triangulation where no vertices are in a circle described by the vertices of a triangle

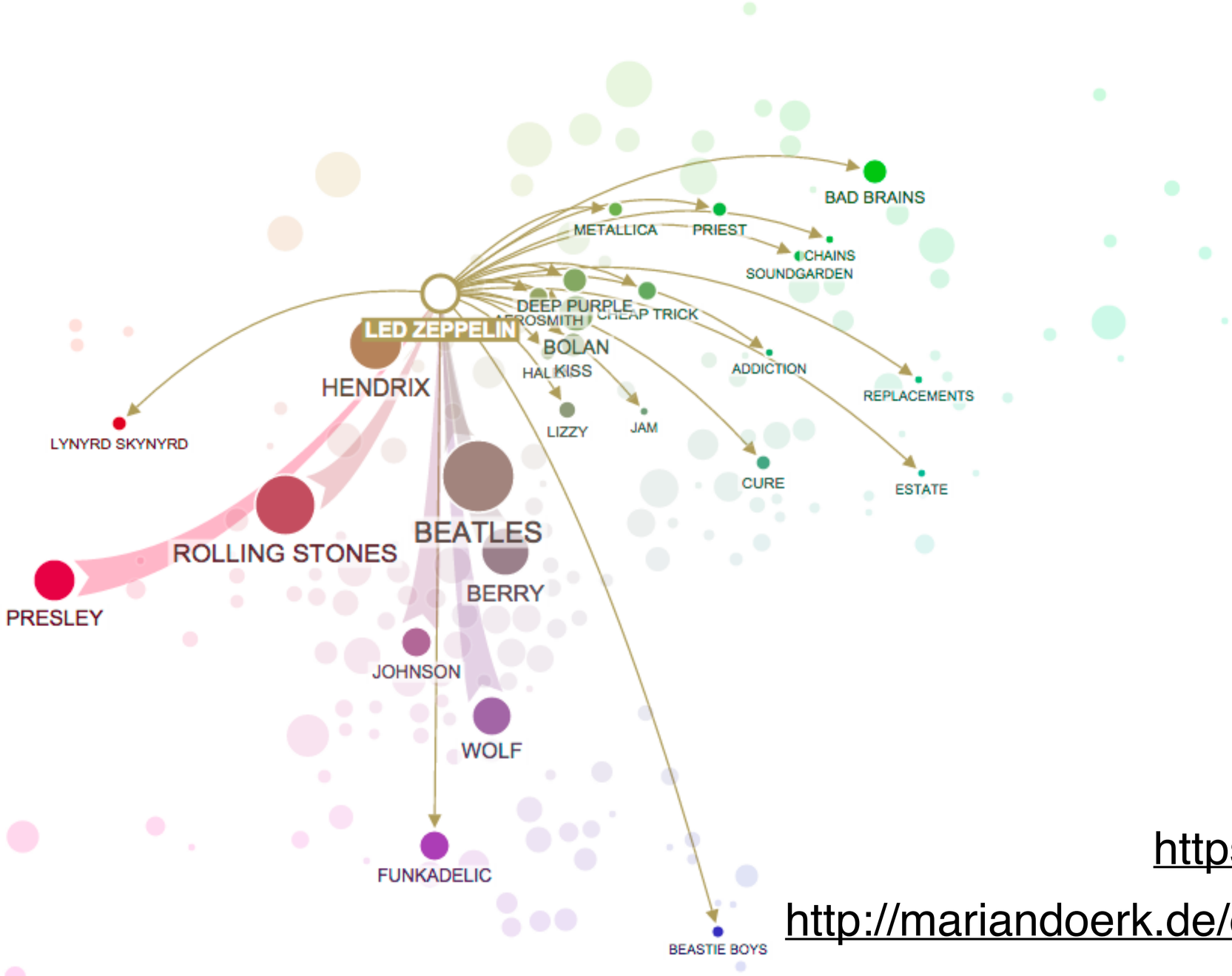
Voronoi edges are perpendicular to triangle edges.



https://en.wikipedia.org/wiki/Delaunay_triangulation

http://paulbourke.net/papers/triangulate/

Design Critique



https://goo.gl/IDRXDl

http://mariandoerk.de/edgemaps/demo/

Clustering

Clustering

Classification of items into “similar” bins

Based on similarity measures

- Euclidean distance, Pearson correlation, ...

Partitional Algorithms

- divide data into set of bins
- # bins either manually set (e.g., k-means) or automatically determined (e.g., affinity propagation)

Hierarchical Algorithms

- Produce “similarity tree” – dendrogram

Bi-Clustering

- Clusters dimensions & records

Fuzzy clustering

- allows occurrence of elements in multiples clusters

Clustering Applications

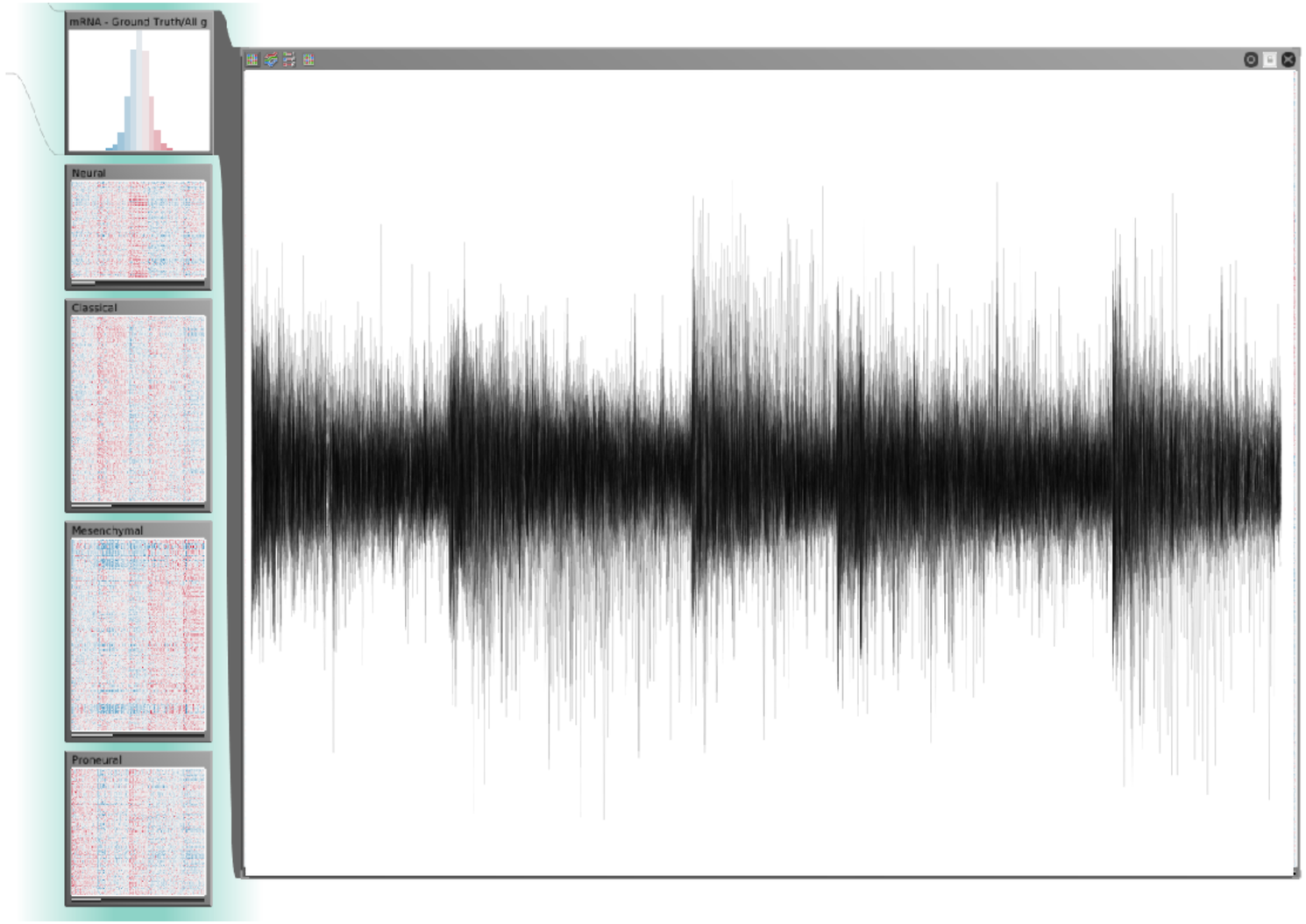
Clusters can be used to

- order (pixel based techniques)
- brush (geometric techniques)
- aggregate

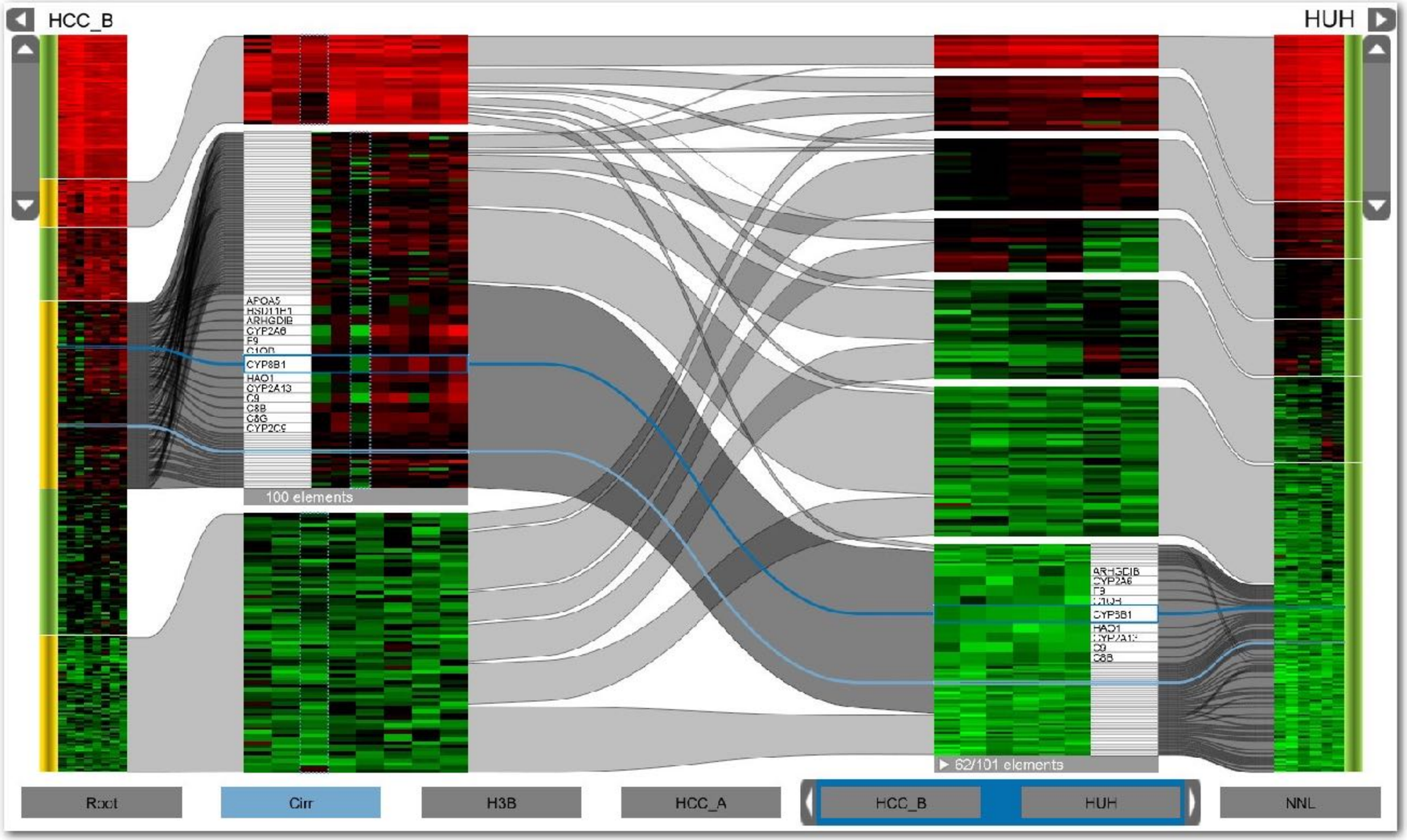
Aggregation

- cluster more homogeneous than whole dataset
- statistical measures, distributions, etc. more meaningful

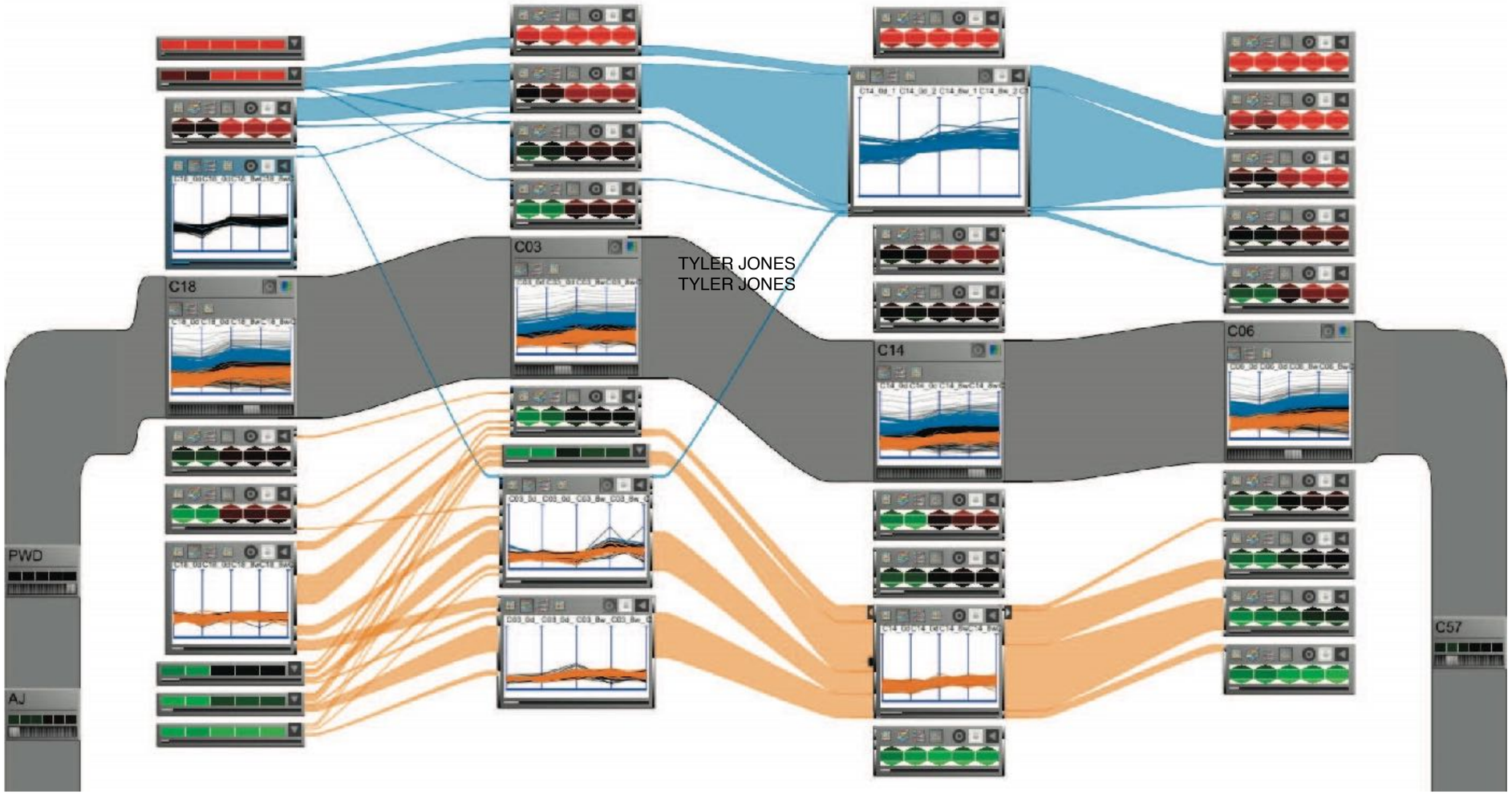
Clustered Heat Map



Cluster Comparison



Aggregation



Example: K-Means

Goal: Minimize aggregate intra-custer distance (*inertia*)

$$\underset{C}{argmin} \sum_{i=1}^{k} \sum_{x \in C_i} \|x - \mu_i\|^2$$

total squared distance from point to center of its cluster

for euclidian distance: this is the variance

measure of how internally coherent clusters are

Lloyd's Algorithm

Input: set of records $x_1 \ldots x_n$, and k (nr clusters)

Pick k starting points as centroids $c_1 \ldots c_k$

While not converged:

1. for each point x_i find closest centroid c_j
   - for every c_j calculate distance $D(x_i, c_j)$
   - assign x_i to cluster j defined by smallest distance
2. for each cluster j, compute a new centroid c_j
   by calculating the average of all x_i assigned to cluster j

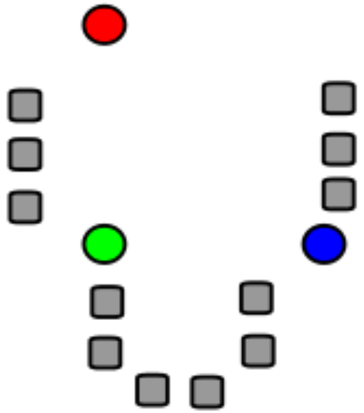
Repeat until convergence, e.g.,

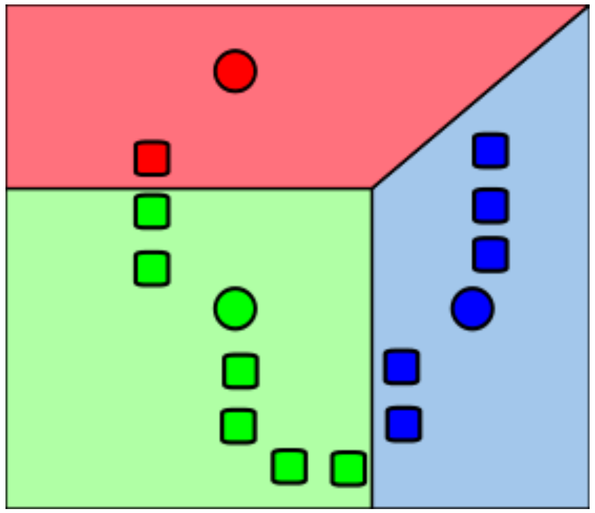
no point has changed cluster

distance between old and new centroid below threshold

number of max iterations reached

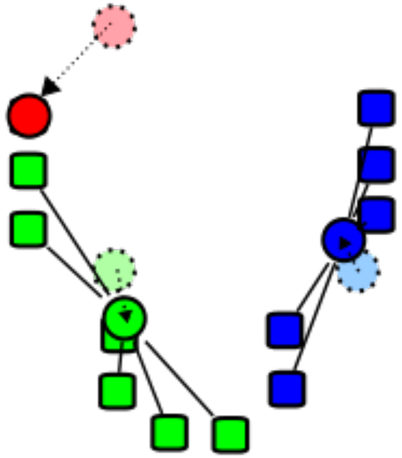
1. Initialization

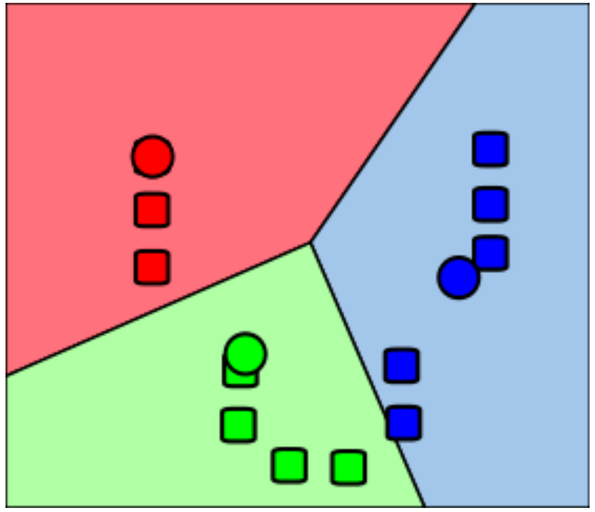




2. Assign Clusters

3. Update Centroids

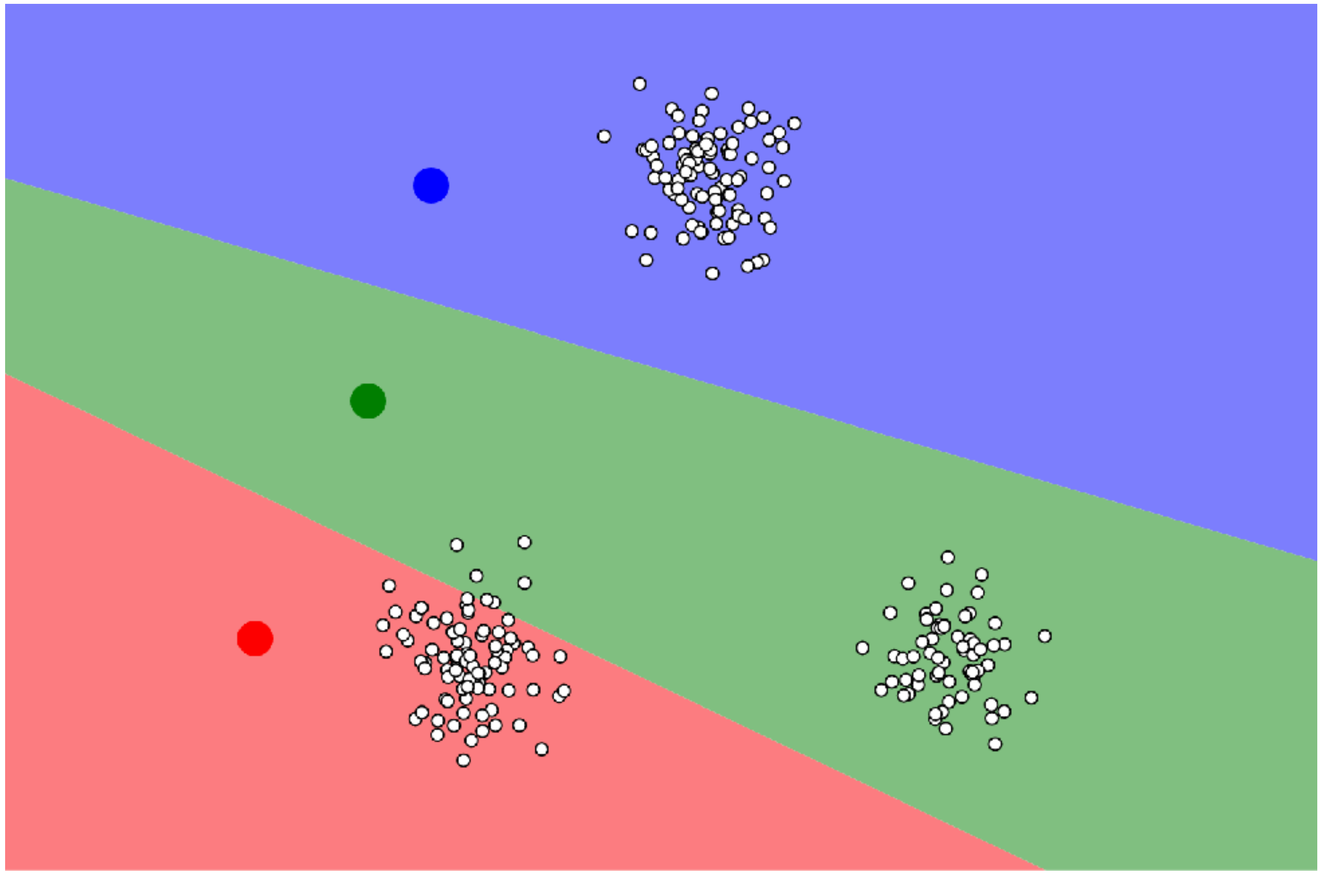




4. Assign Clusters

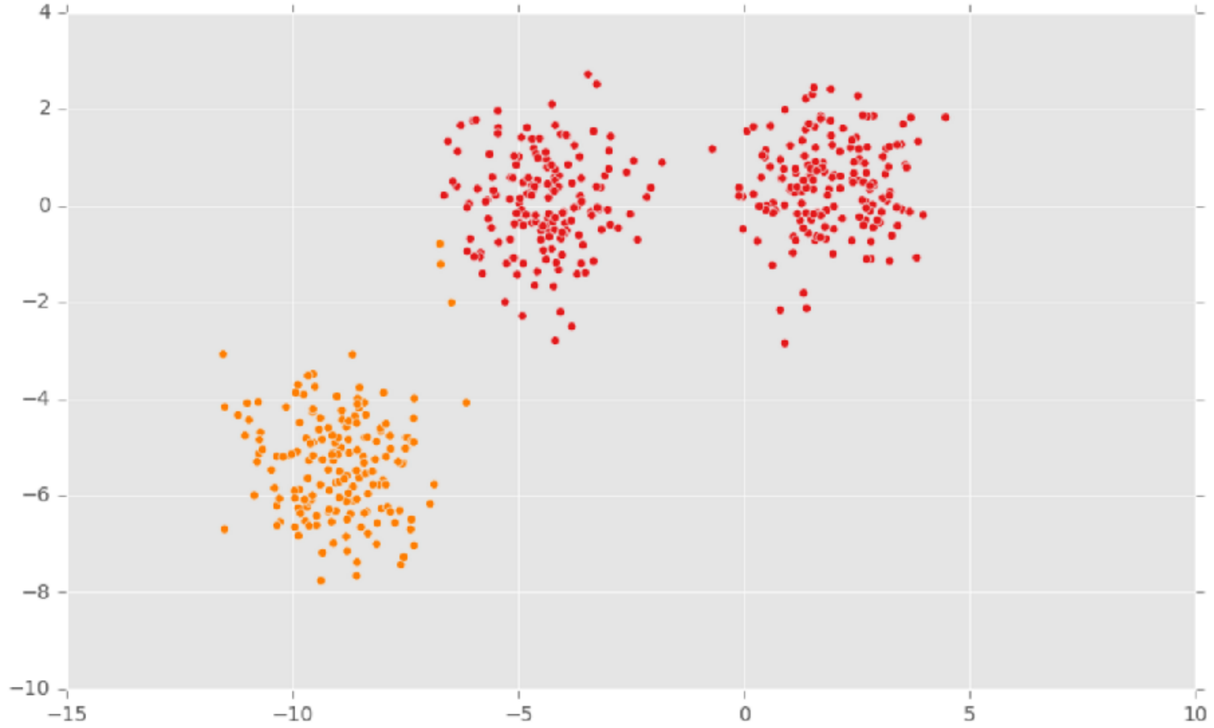
And repeat until converges

Illustrated



https://www.naftaliharris.com/blog/visualizing-k-means-clustering/

Choosing K



Properties

Lloyds algorithm doesn’t find a global optimum

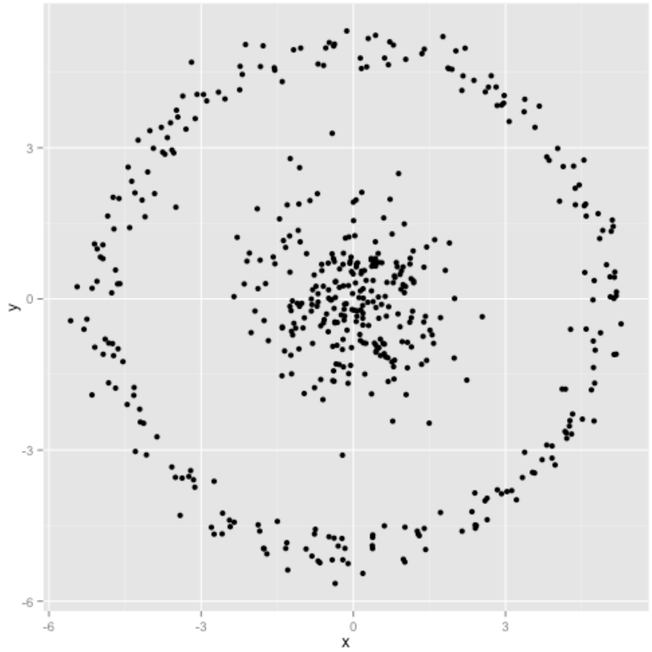
Instead it finds a local optimum

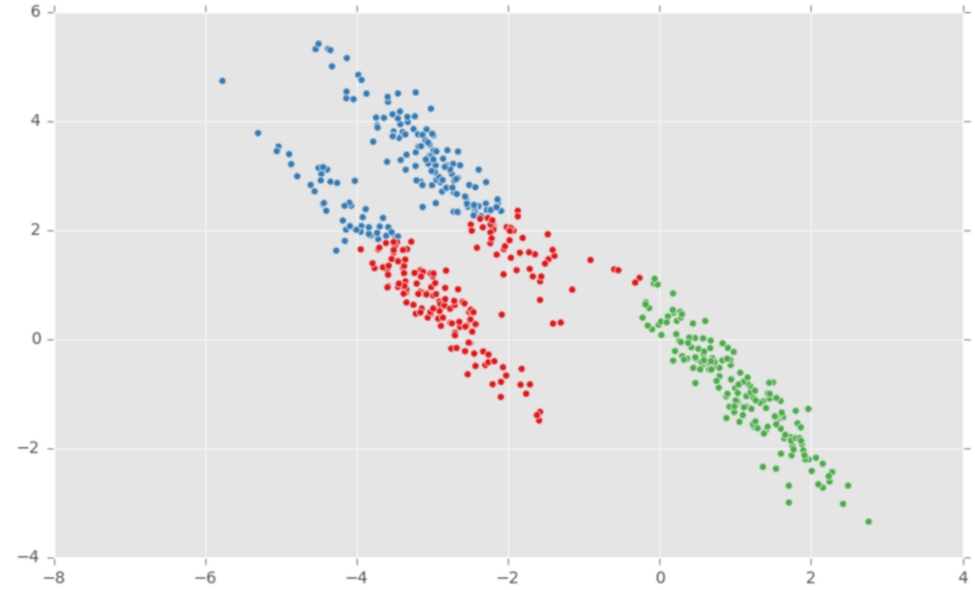
It is very fast:

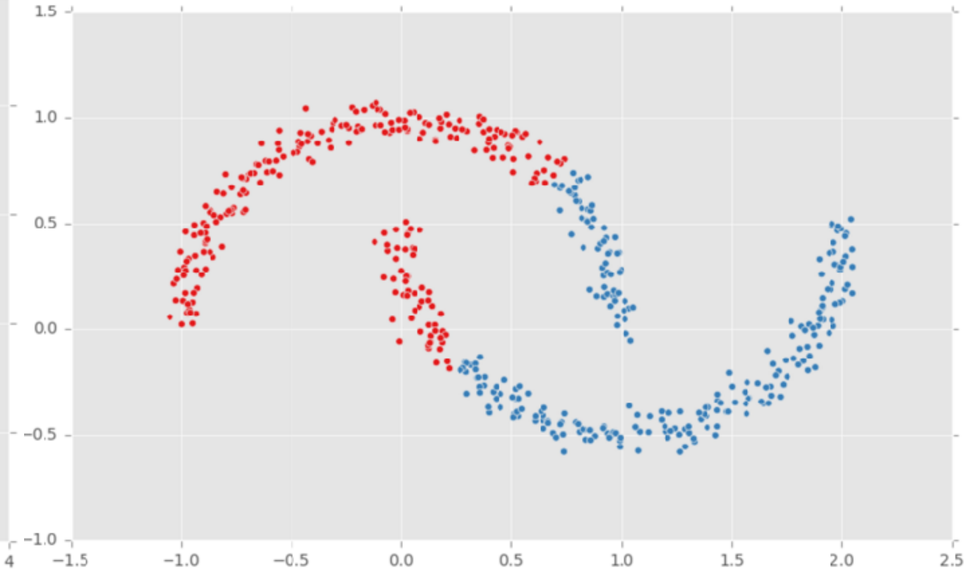
- common to run multiple times and pick the solution with the minimum inertia

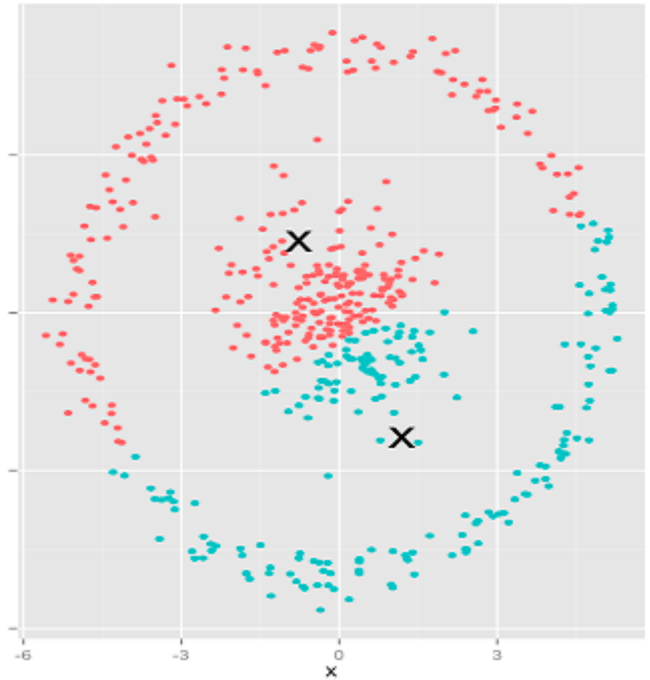
K-Means Properties

Assumptions about data:
roughly “circular” clusters of
equal size

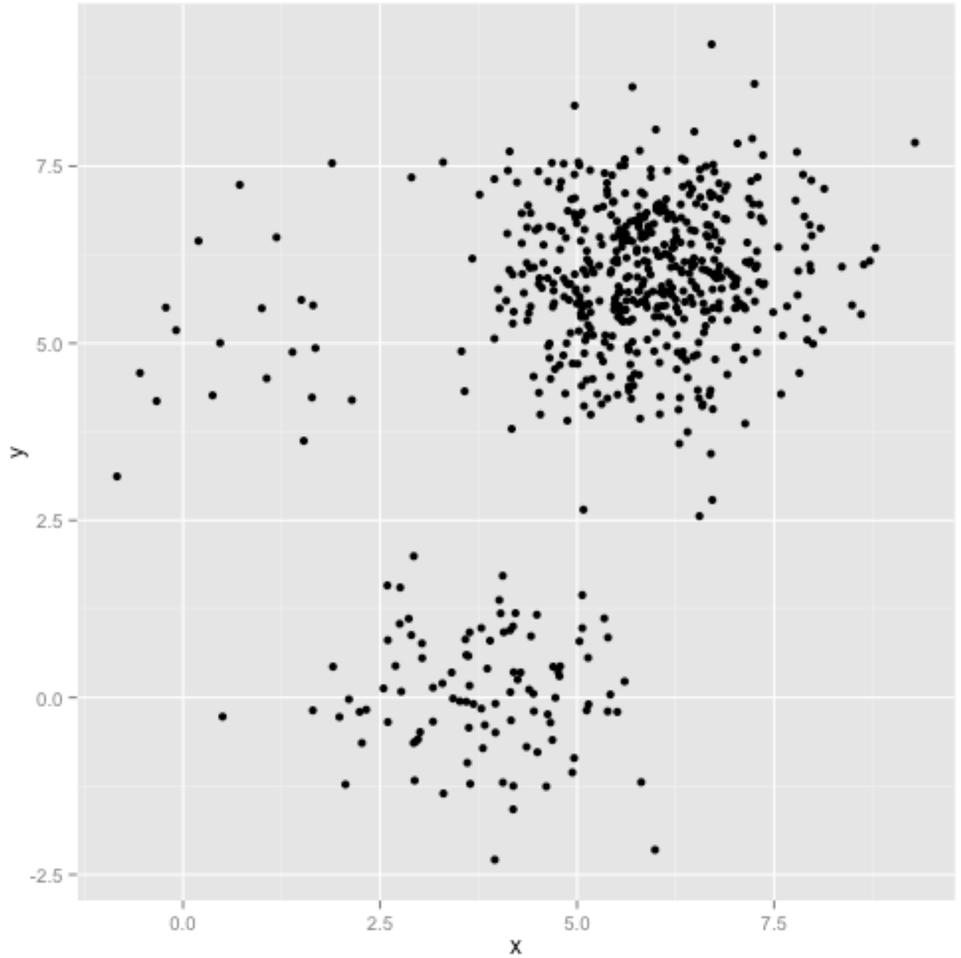








K-Means Unequal Cluster Size



http://stats.stackexchange.com/questions/133656/how-to-understand-the-drawbacks-of-k-means

Hierarchical Clustering

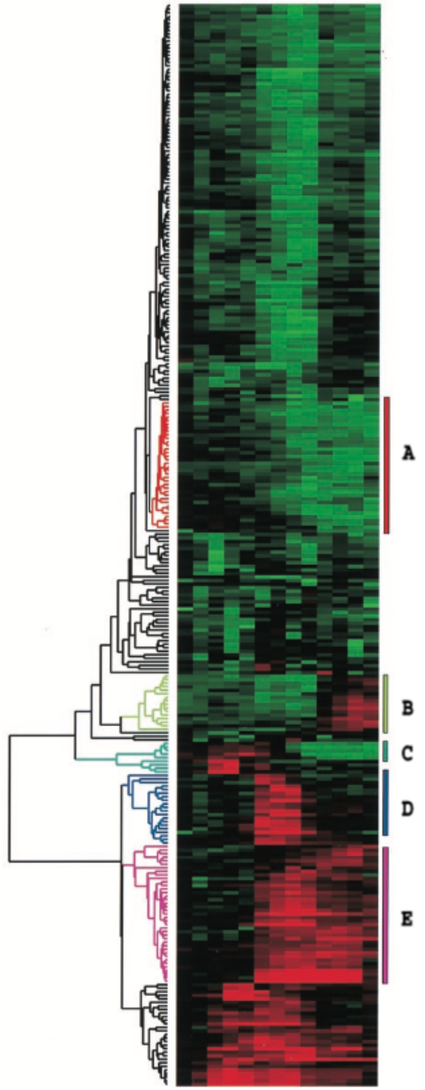
Two types:

agglomerative clustering

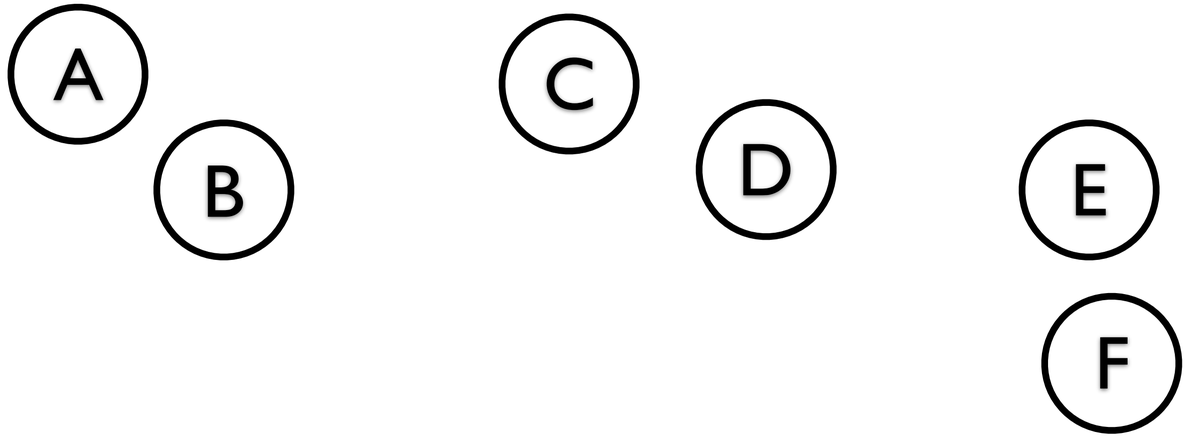
start with each node as a cluster and merge

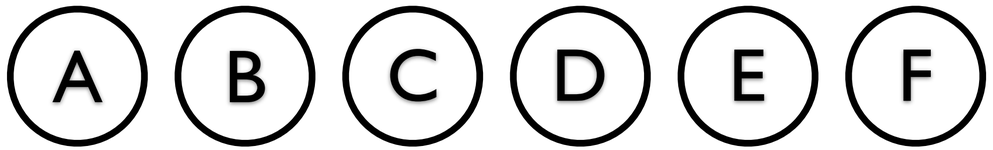
divisive clustering

start with one cluster, and split



Agglomerative Clustering Idea





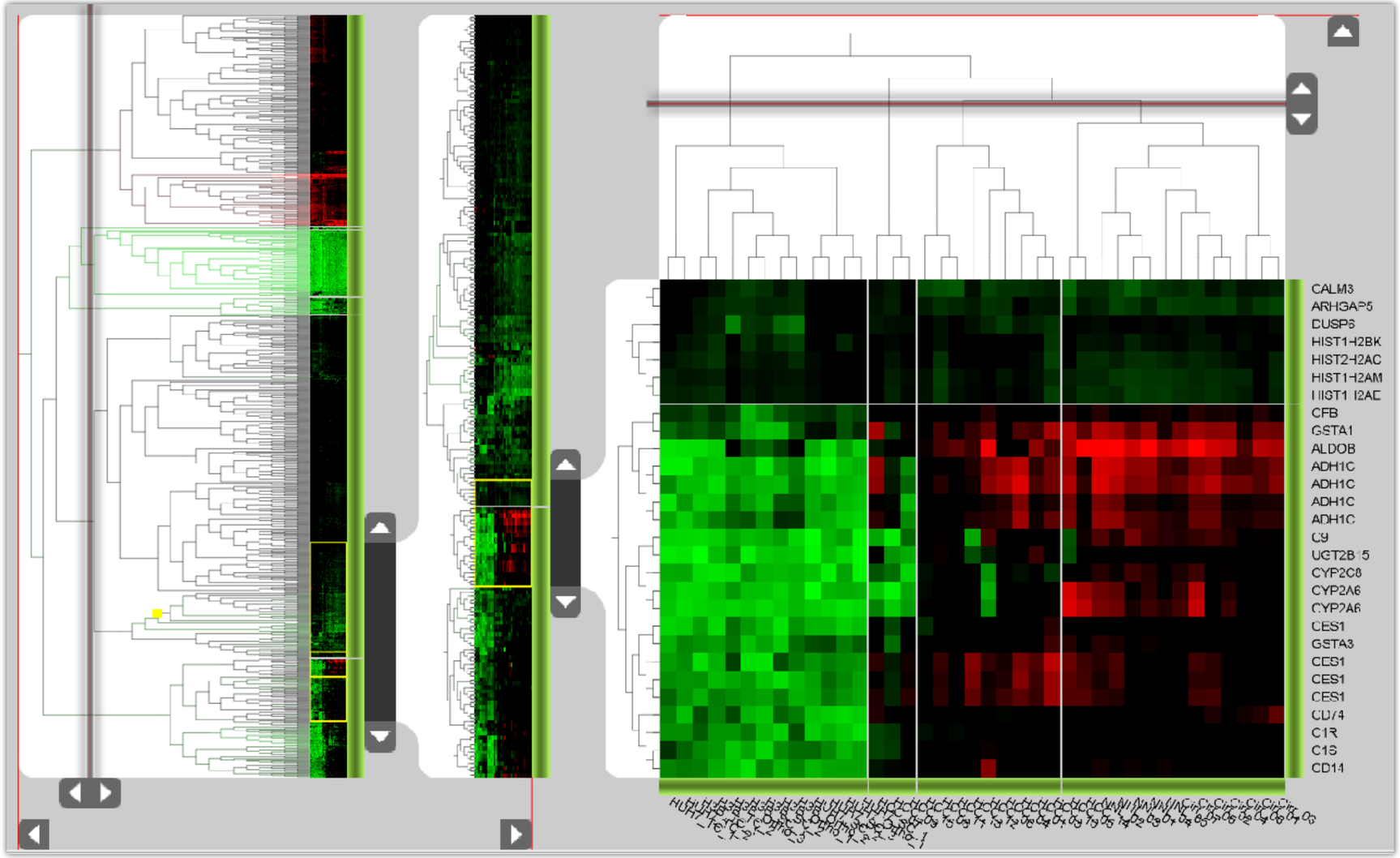
Linkage Criteria

How do you define similarity between two clusters to be merged (A and B)?

- maximum linkage distance: two elements that are apart the furthest
- use minimum linkage distance: the two closest elements
- use average linkage distance
- use centroid distance

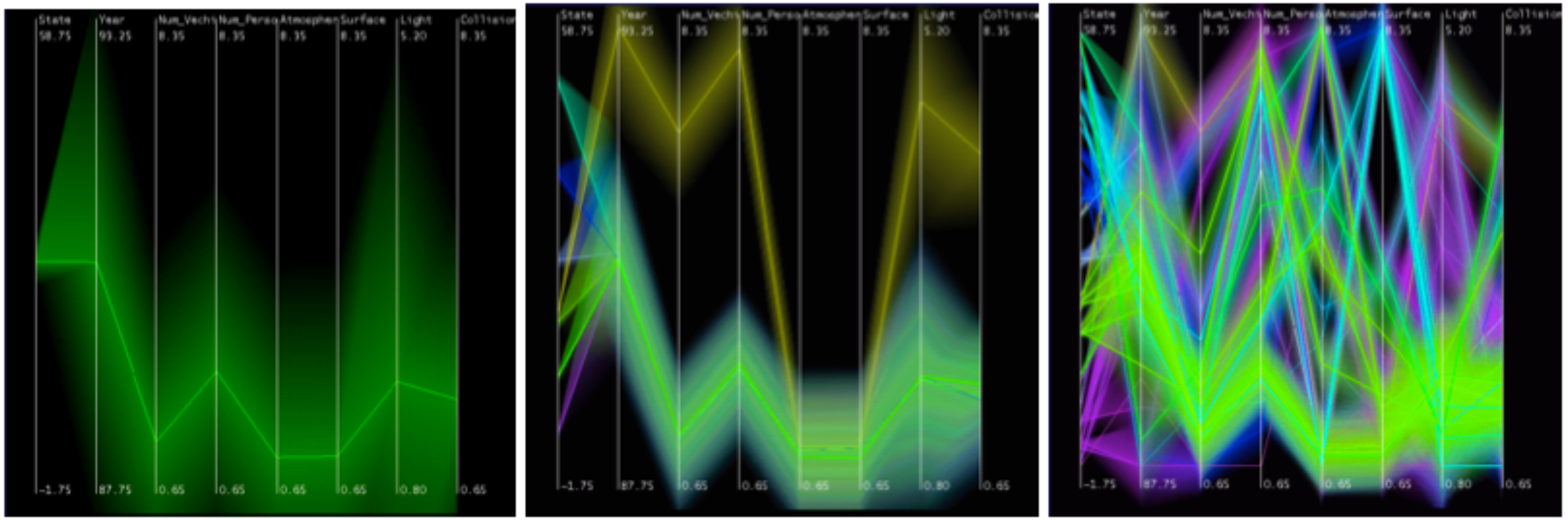
Names	Formula
Maximum or complete-linkage clustering	$\max \{\, d(a,b) : a \in A,\, b \in B \}.$
Minimum or single-linkage clustering	$\min \{\, d(a,b) : a \in A,\, b \in B \}.$
Mean or average linkage clustering, or UPGMA	$\frac{1}{\|A\|\|B\|} \sum_{a \in A} \sum_{b \in B} d(a,b).$
Centroid linkage clustering, or UPGMC	$\|c_s - c_t\|$ where c_s and c_t are the centroids of clusters s and t, respectively.

F+C Approach, with Dendrograms



[Lex, PacificVis 2010]

Hierarchical Parallel Coordinates



Fua 1999

Dimensionality Reduction

Dimensionality Reduction

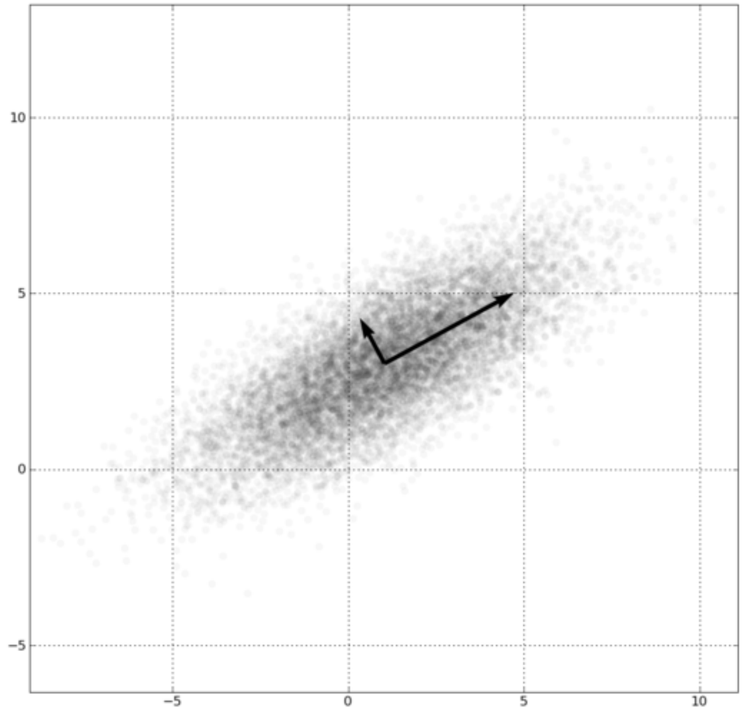
Reduce high dimensional to lower dimensional space

Preserve as much of variation as possible

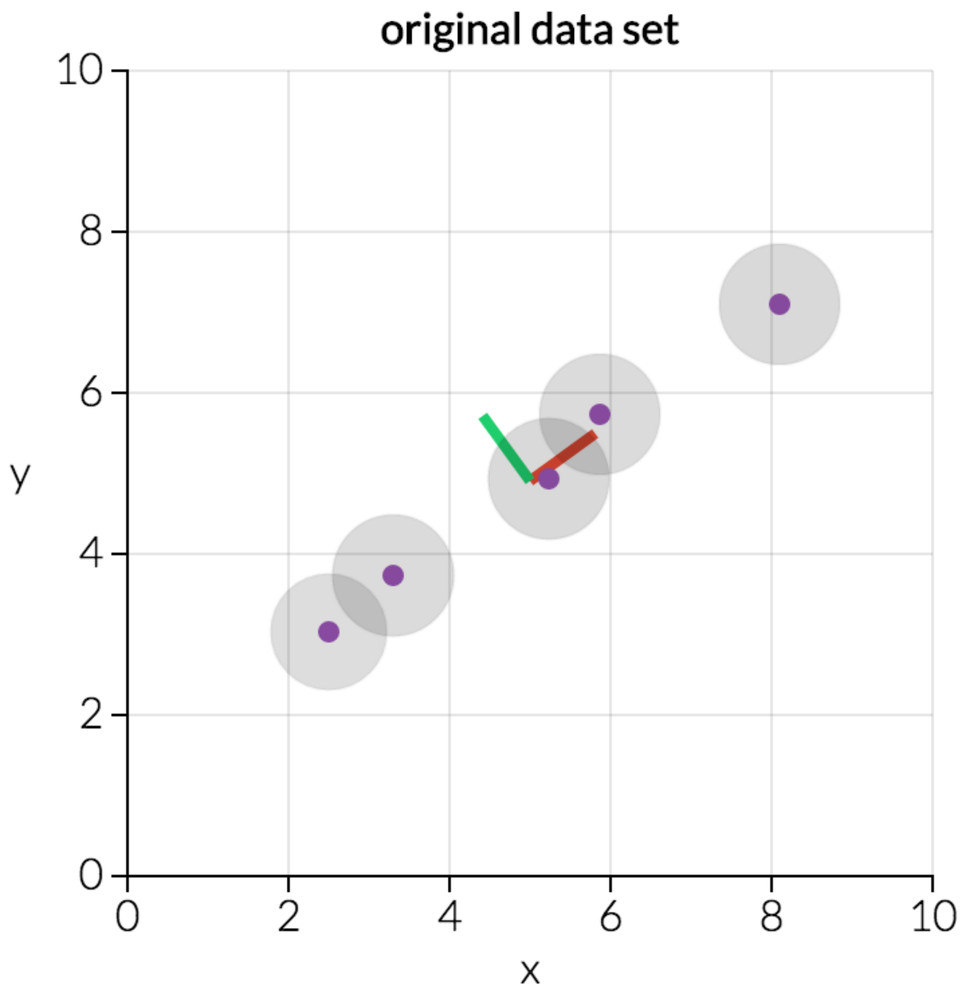
Plot lower dimensional space

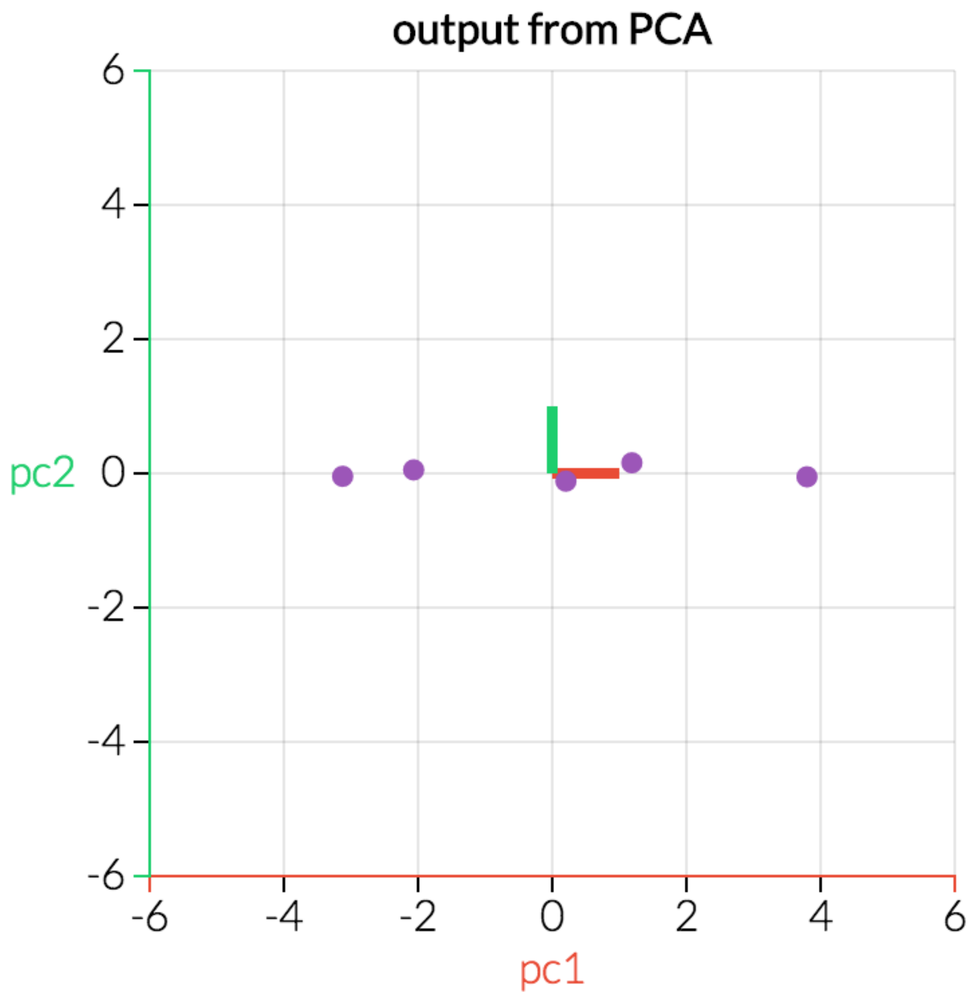
Principal Component Analysis (PCA)

linear mapping, by order of variance

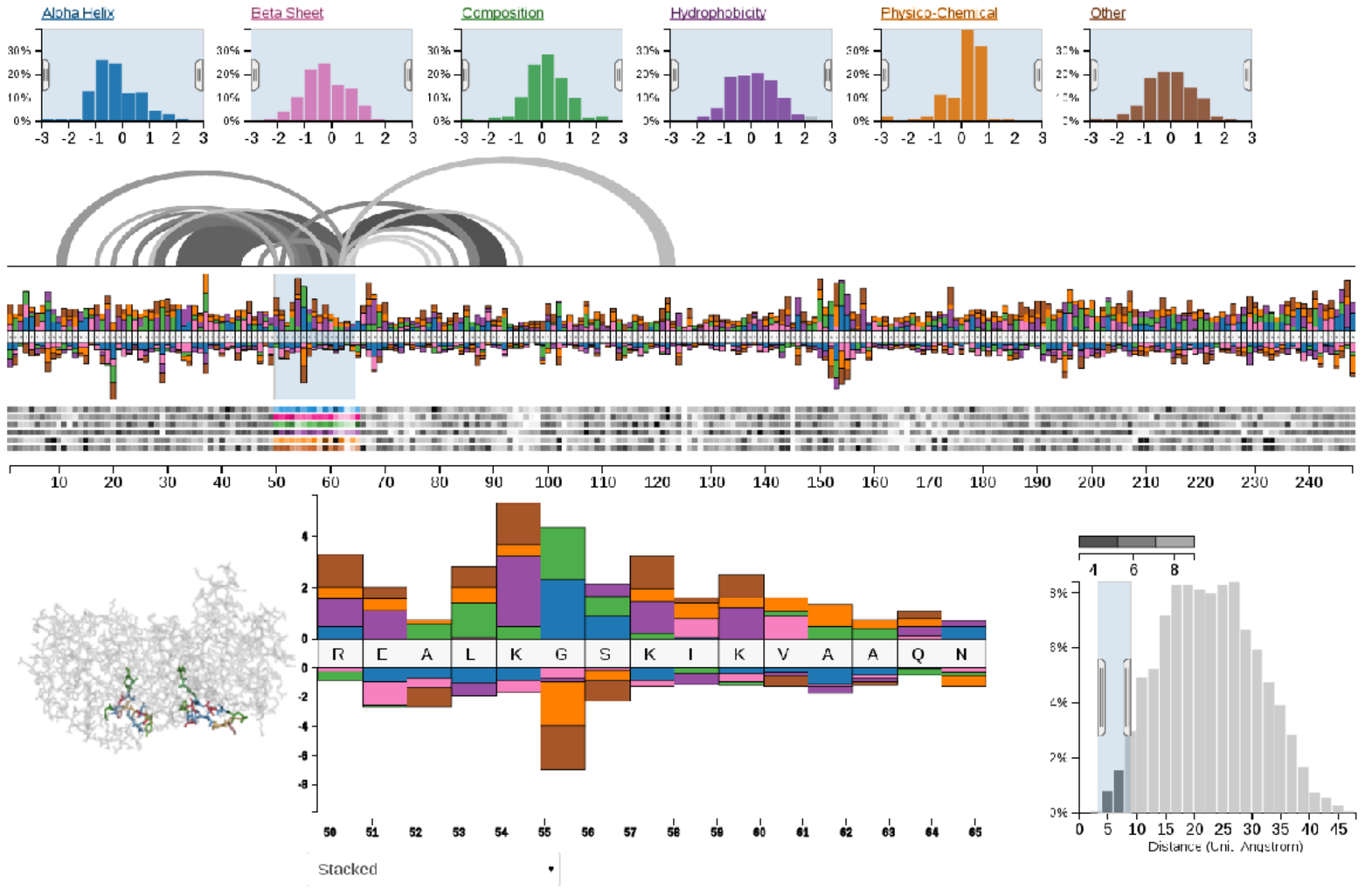


PCA


original data set
10
8
6
4
2
0
y
0
2
4
6
8
10
x


output from PCA
6
4
2
pc2 0
-2
-4
-6
-6
-4
-2
0
2
4
6
pc1

PCA Example – Class Project 2013



http://mu-8.com/

[Mercer & Pandian]

Multidimensional Scaling

Nonlinear, better suited for some DS

Multiple approaches

Works based on projecting a similarity matrix

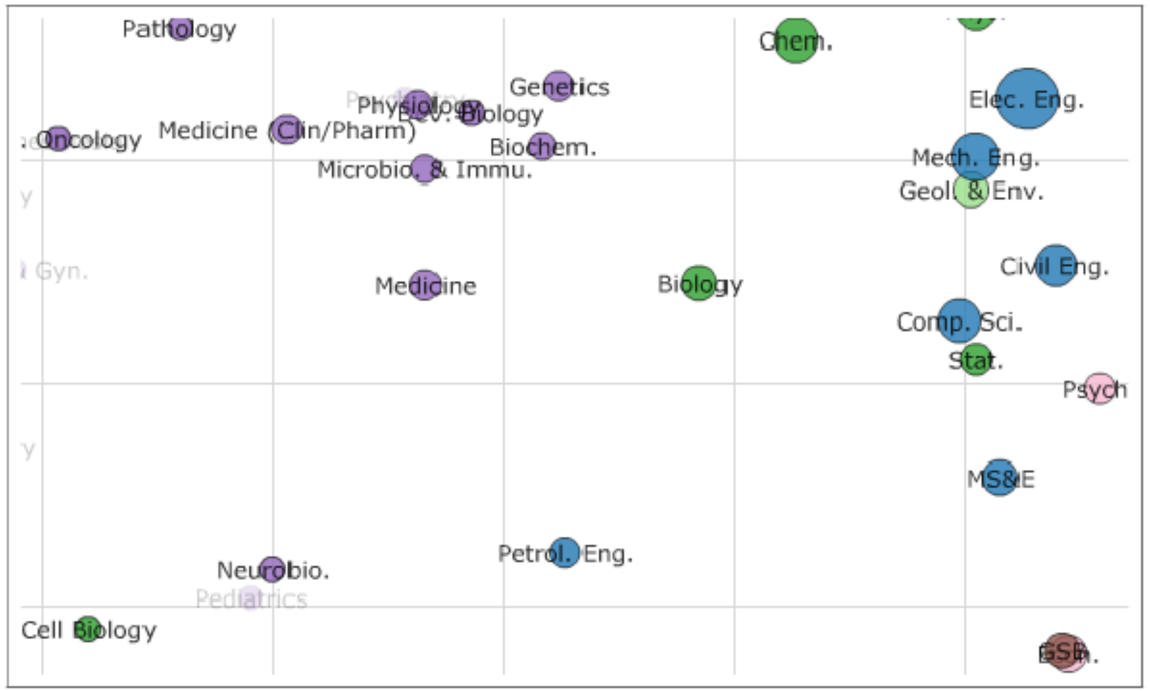
- How do you compute similarity?
- How do you project the points?

Popular for text analysis

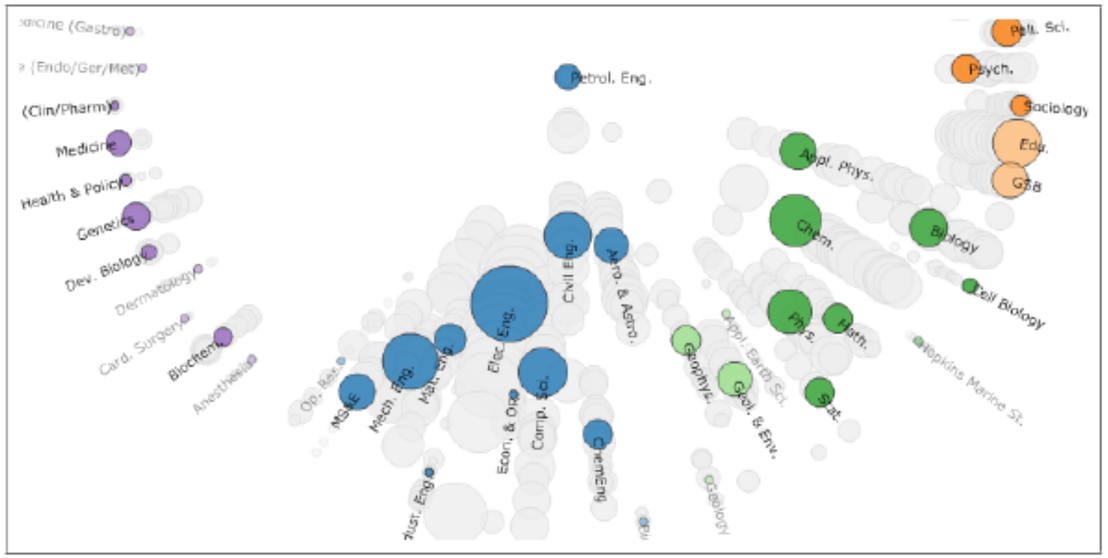
[Doerk 2011]

Can we Trust Dimensionality Reduction?

Topical distances between departments in a 2D projection



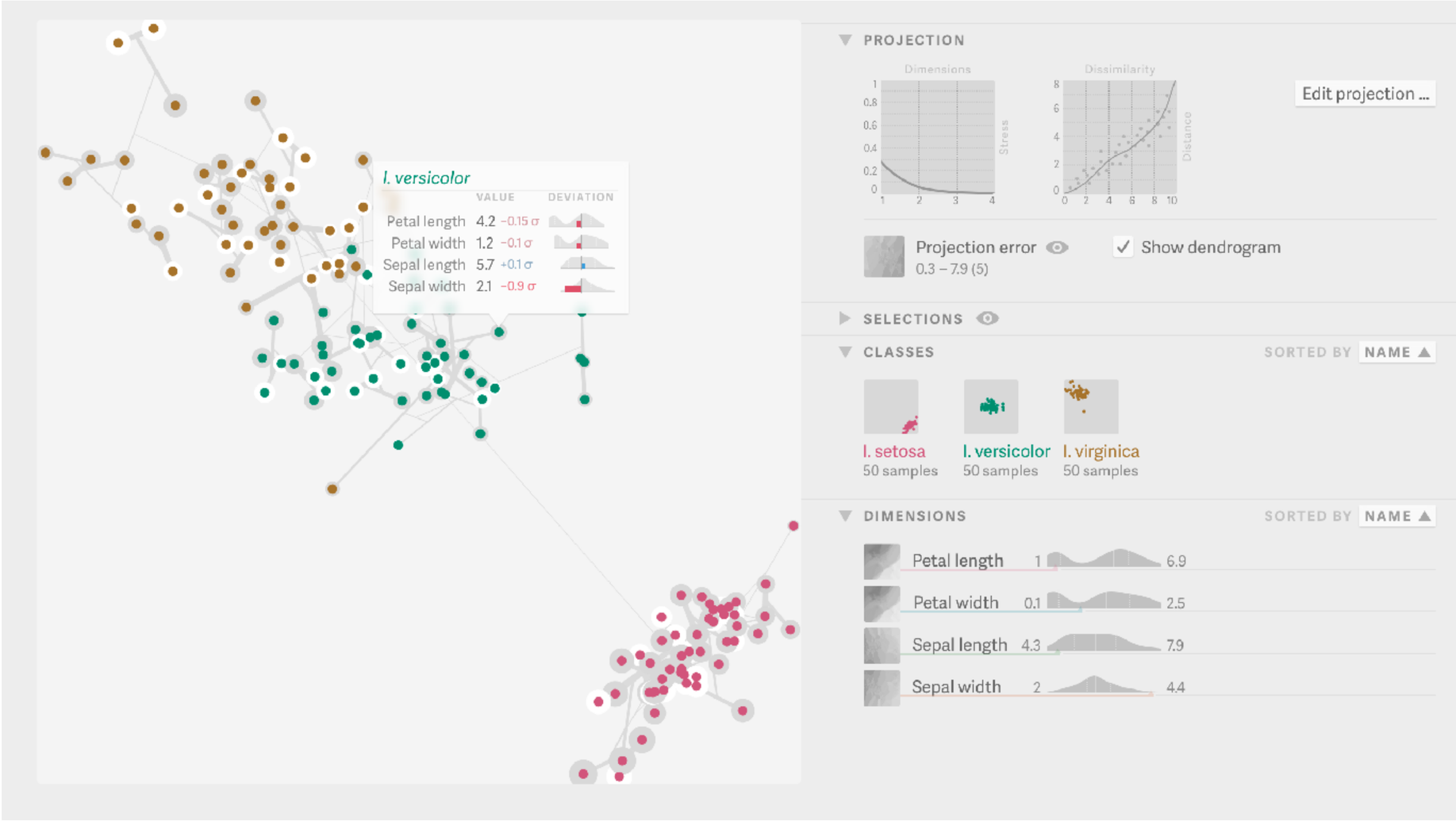
Topical distances between the selected Petroleum Engineering and the others.



[Chuang et al., 2012]

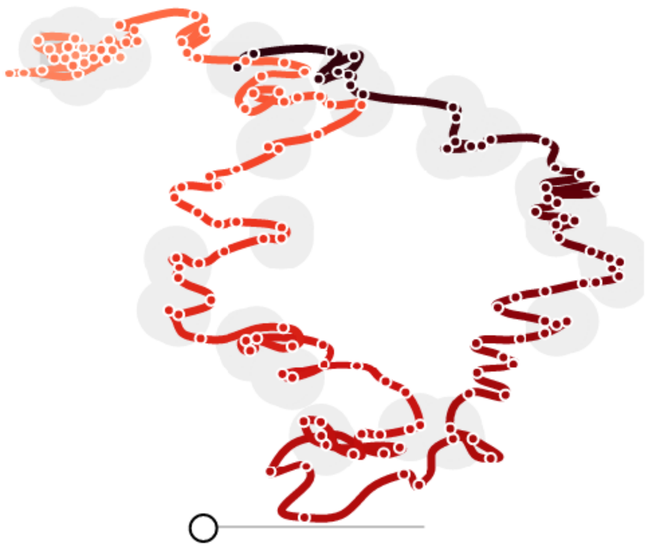
http://www-nlp.stanford.edu/projects/dissertations/browser.html

Probing Projections

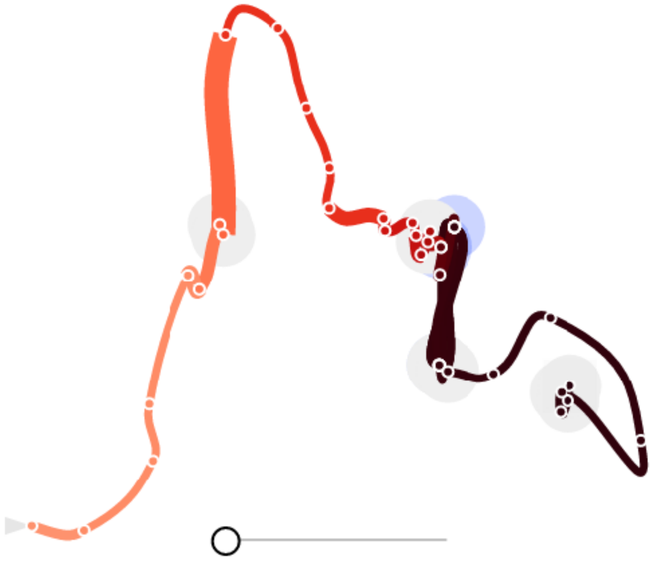


http://julianstahnke.com/probing-projections/

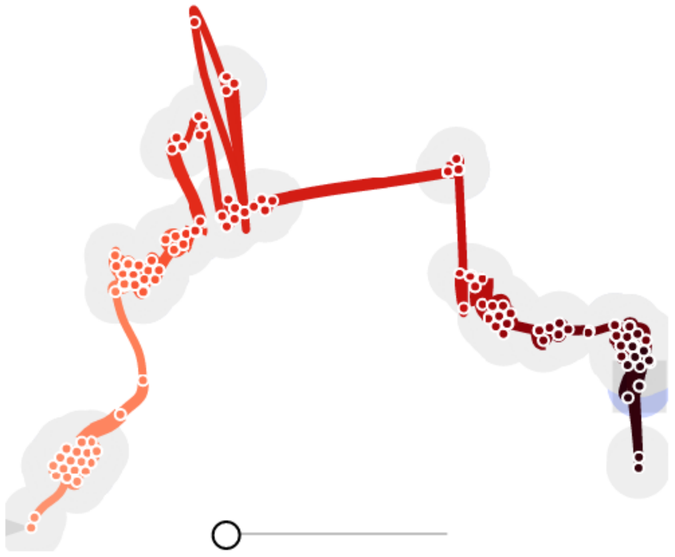
MDS for Temporal Data: TimeCurves



Video: Global Cloud Circulation (146)



Wikipedia: Chocolate (46)



Wikipedia: Palestine 200 1 (200)

http://aviz.fr/~bbach/timecurves/