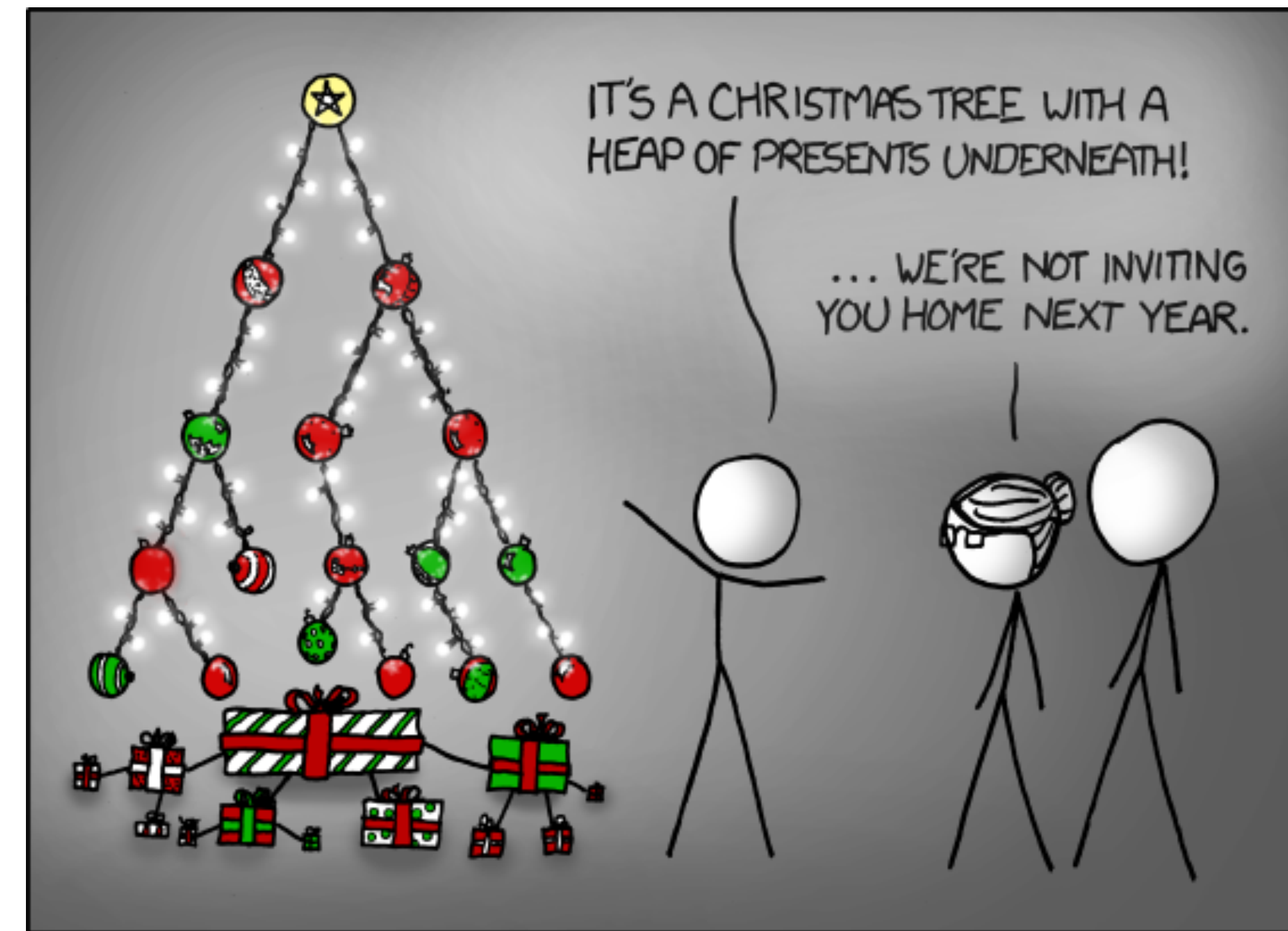


# CS-5630 / CS-6630 Visualization

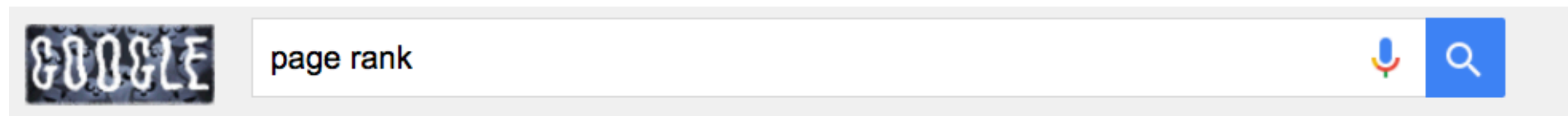
## Graphs

Alexander Lex  
[alex@sci.utah.edu](mailto:alex@sci.utah.edu)



# Applications of Graphs

Without graphs, there would be none of these:



All News Images Videos Books More Search tools

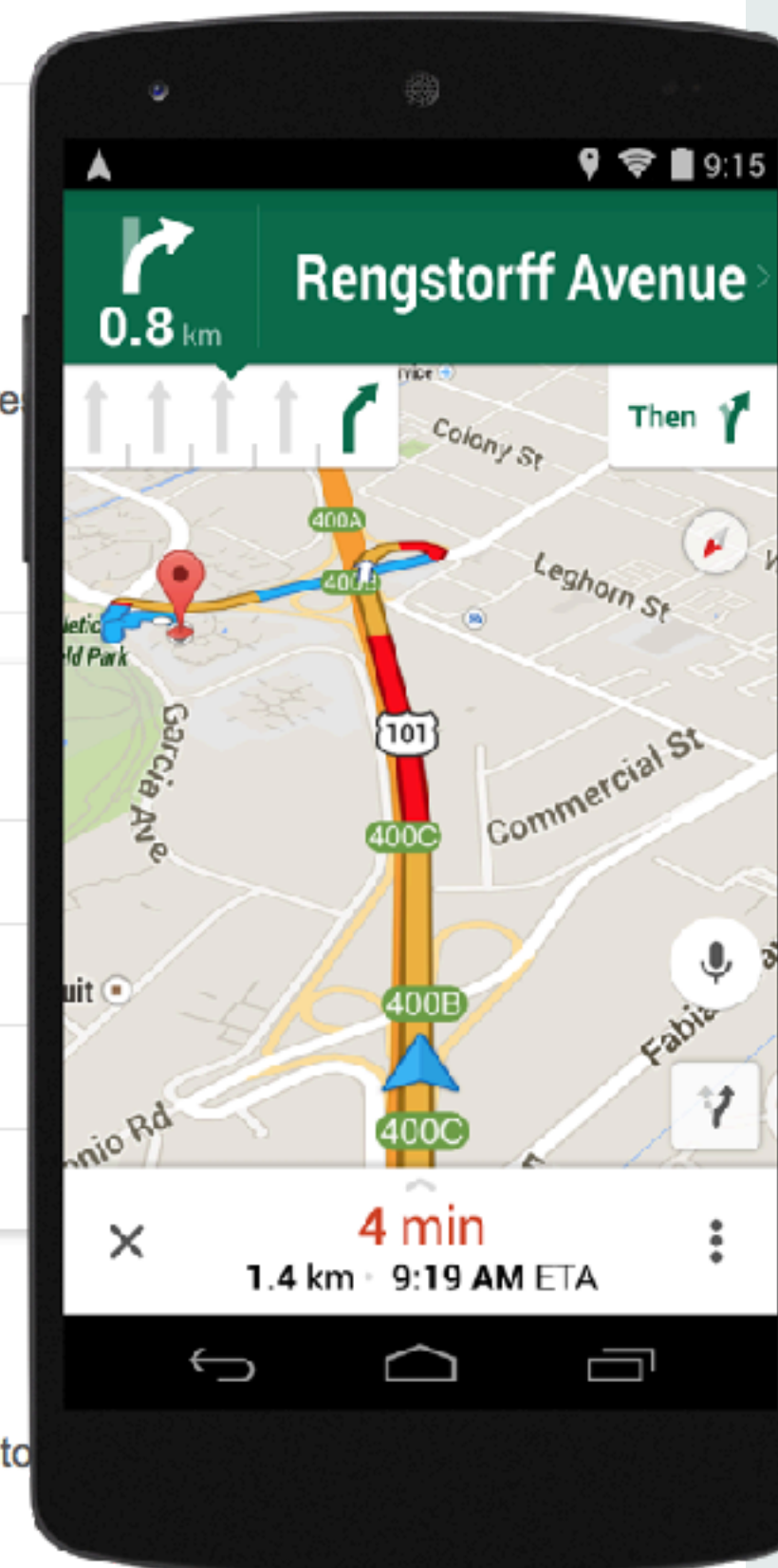
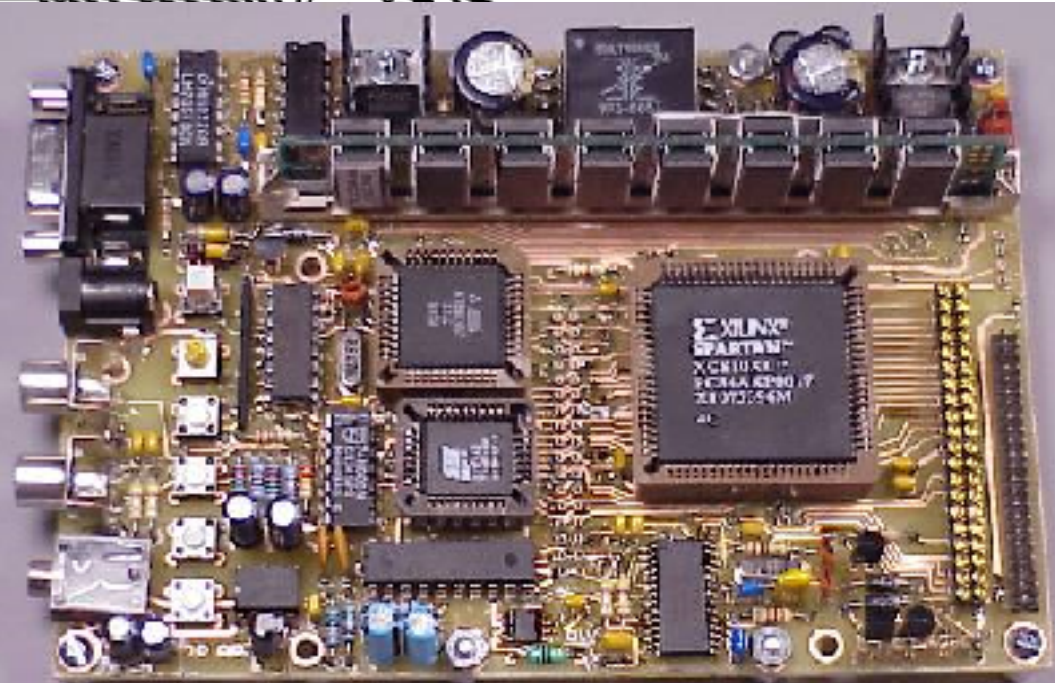
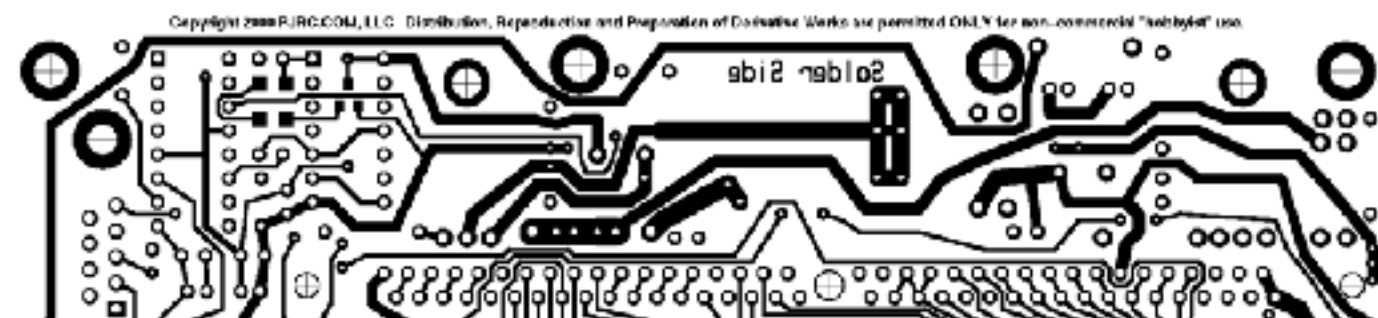
About 431,000,000 results (0.86 seconds)

[PageRank - Wikipedia](#)

<https://en.wikipedia.org/wiki/PageRank> - Wikipedia

PageRank is an algorithm used by Google Search to rank websites in their search engine results. PageRank was named after Larry Page, one of the founders of ...

[Description](#) · [History](#) · [Algorithm](#) · [Variations](#)



Follow Mark to get his public posts in your News Feed.

83,820,410 Followers

Intro

Making the world more open and connected.

- Founder and CEO at Facebook
- Works at Chan Zuckerberg Initiative
- Studied Computer Science at Harvard University

Mark Zuckerberg

October 28 at 1:26pm

Happy birthday, Bill! Thanks for your friendship and here's to of changing the world.



**facebook**

December 2010

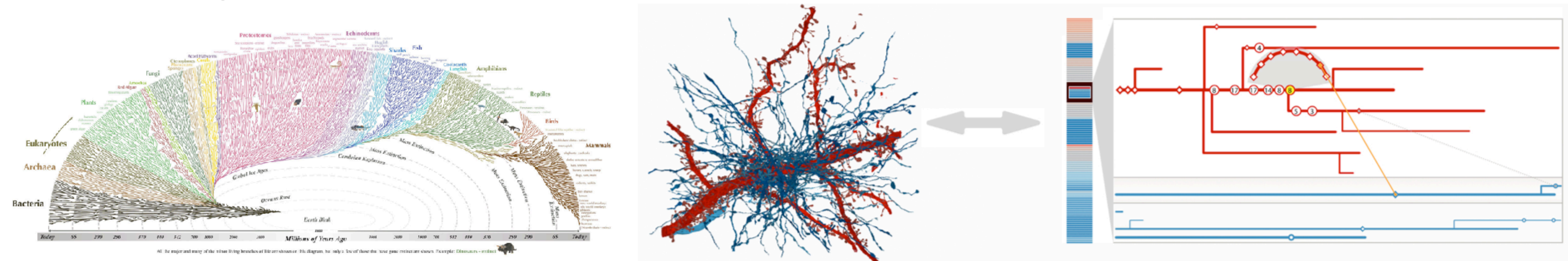
# Biological Networks

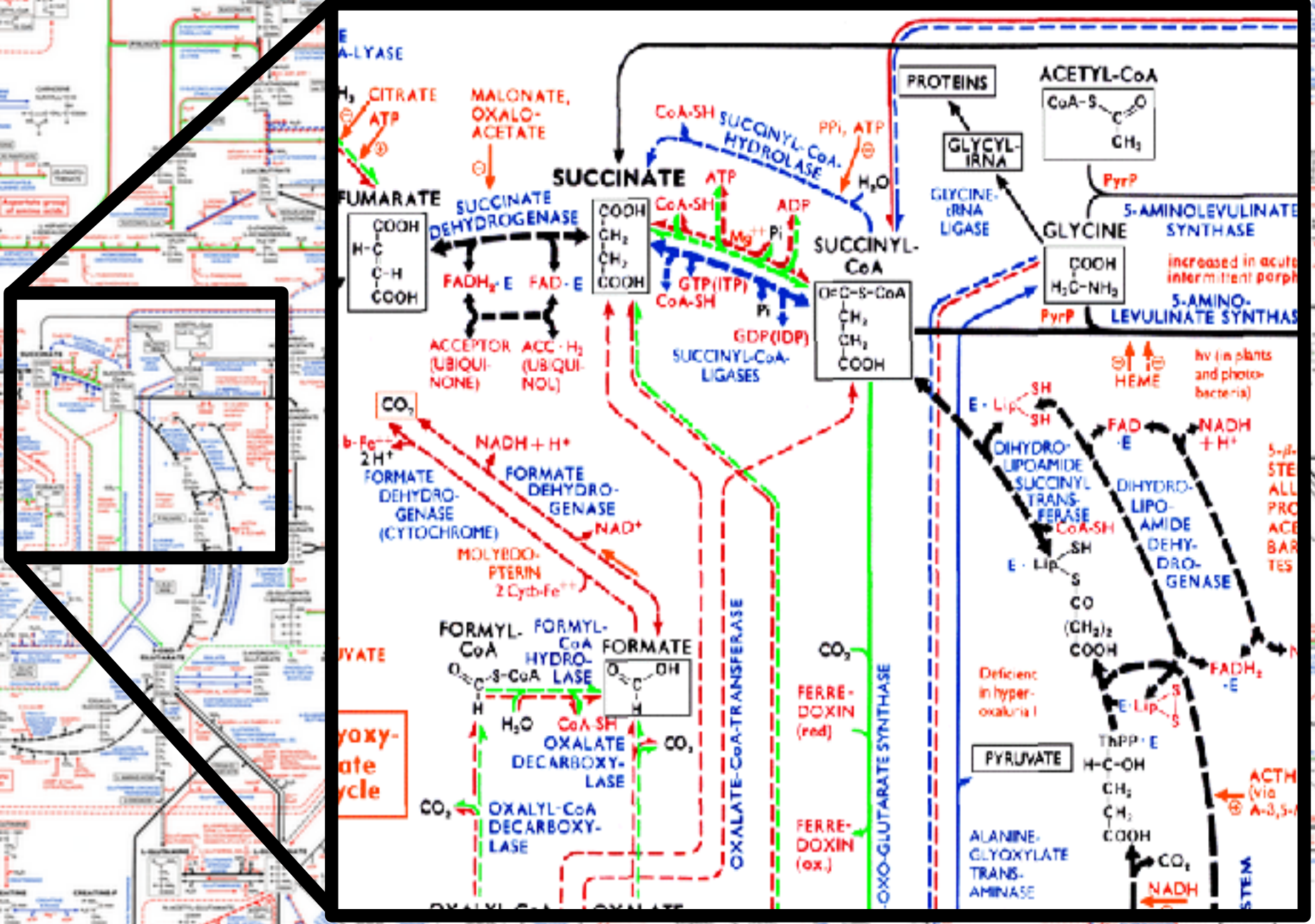
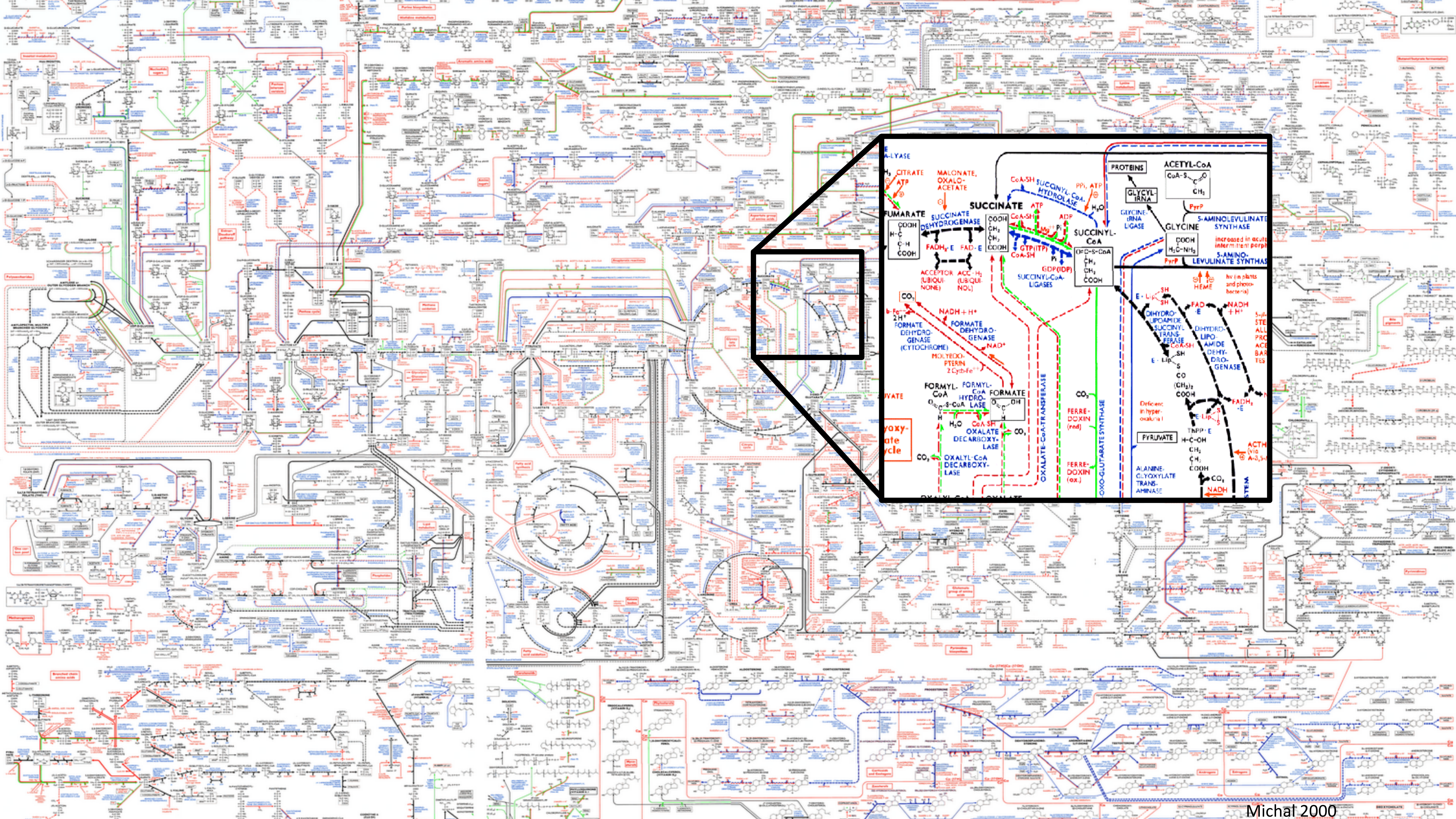
Interaction between genes, proteins and chemical products

The brain: connections between neurons

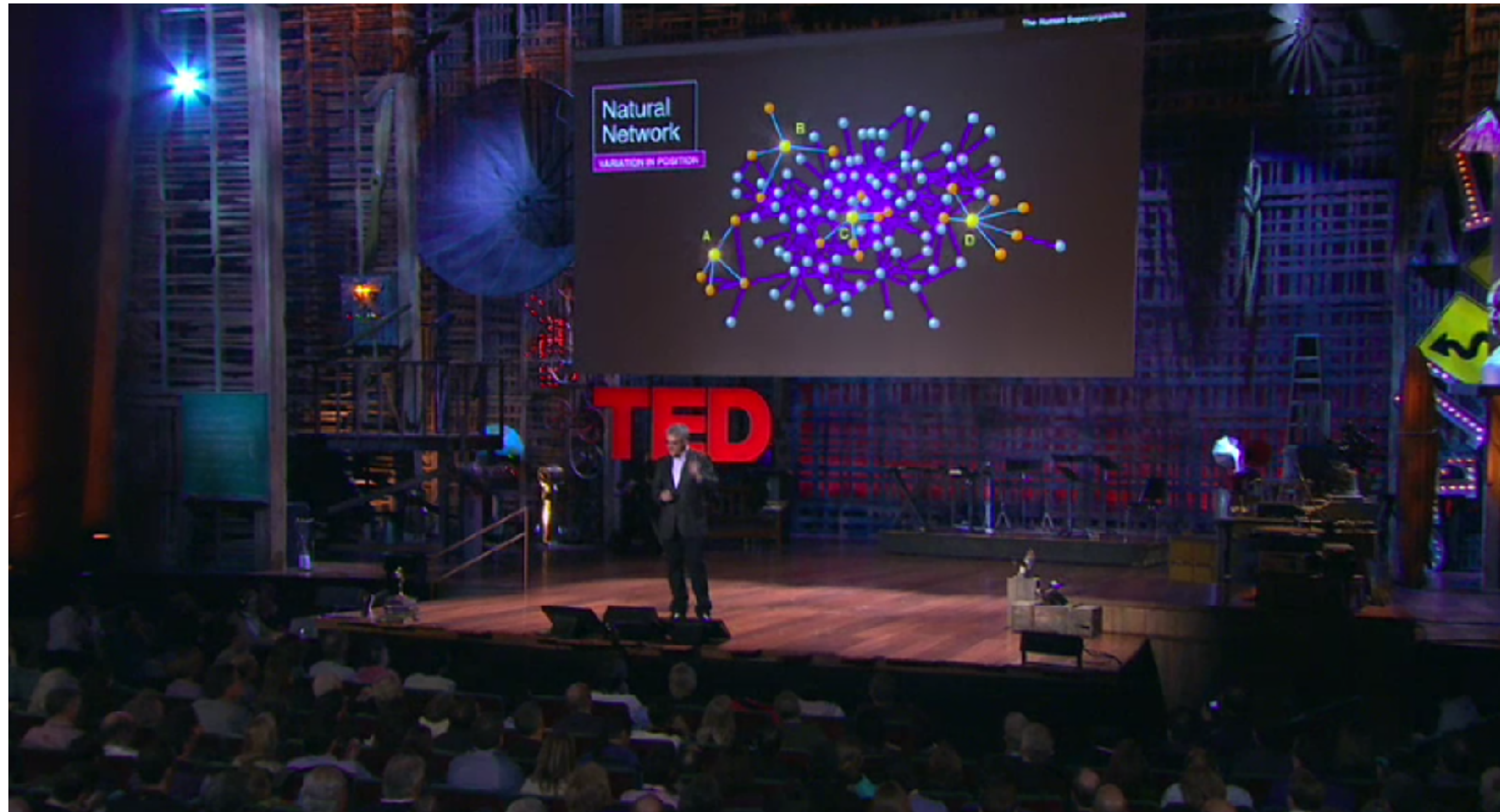
Your ancestry: the relations between you and your family

Phylogeny: the evolutionary relationships of life





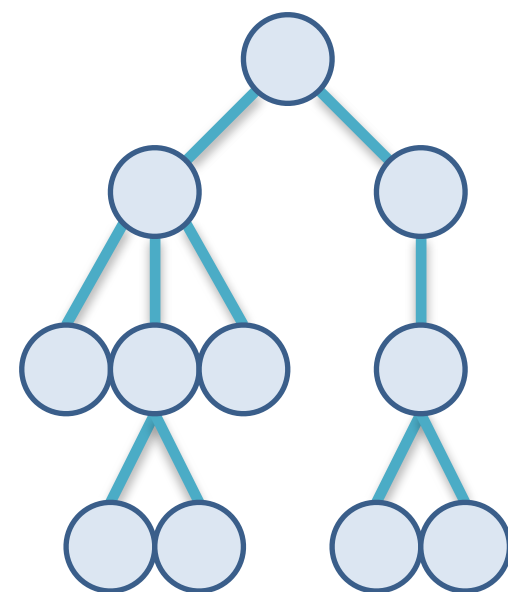
# Graph Analysis Case Study



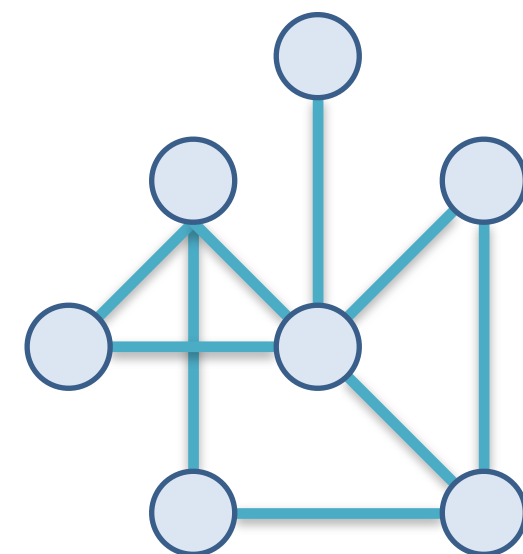
# Graph Theory Fundamentals

See also “Network Science”, Barabasi  
<http://barabasi.com/networksciencebook/chapter/2>

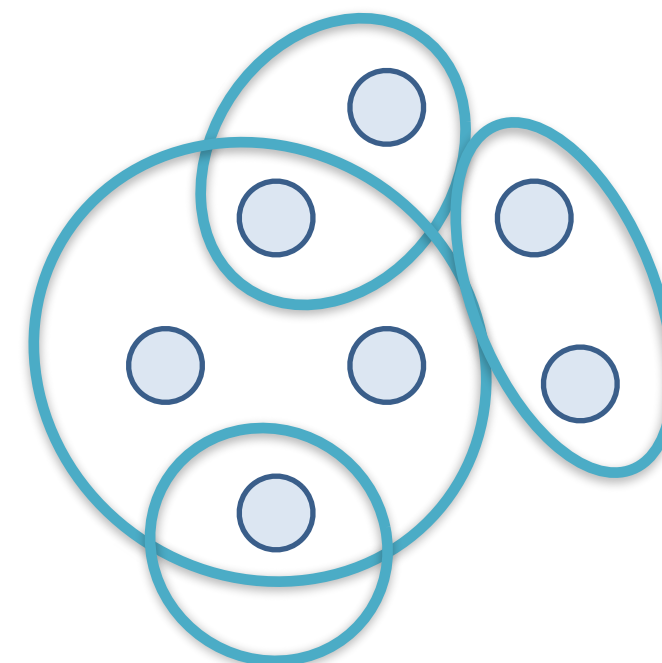
Tree



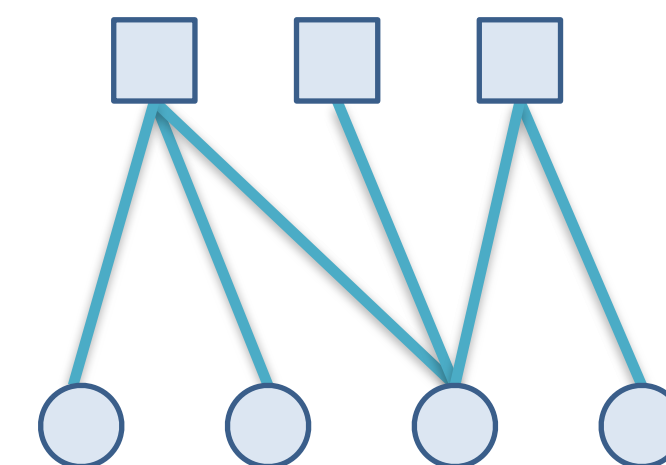
Network



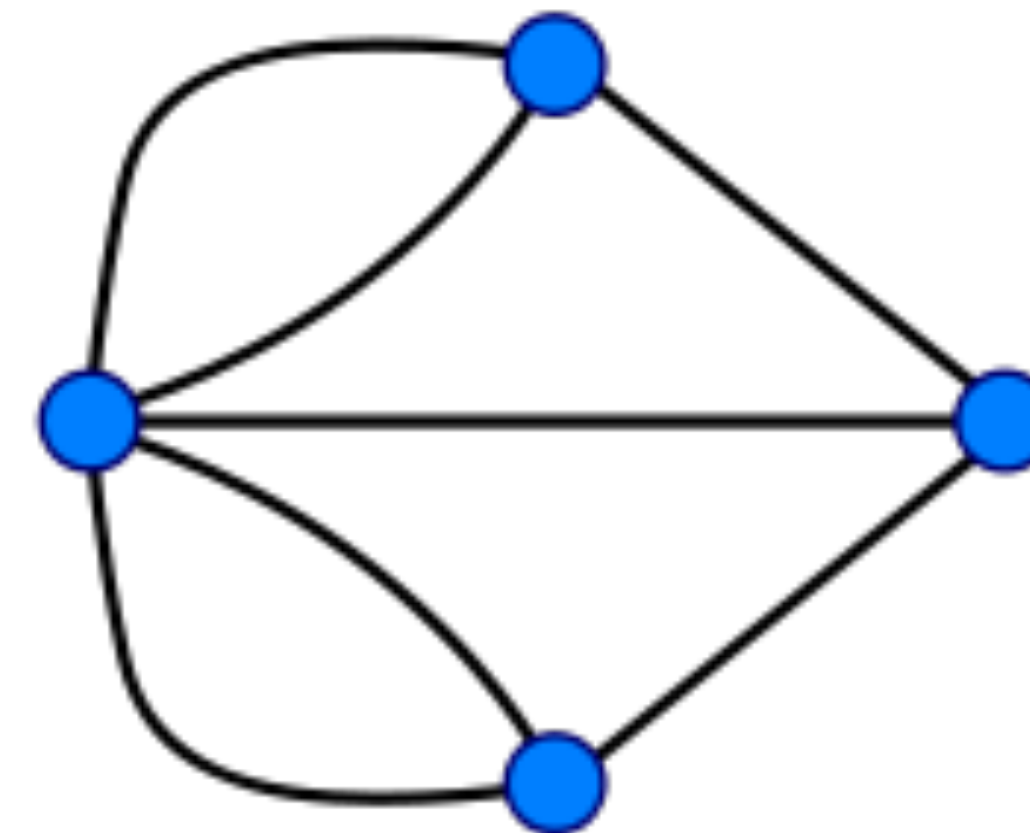
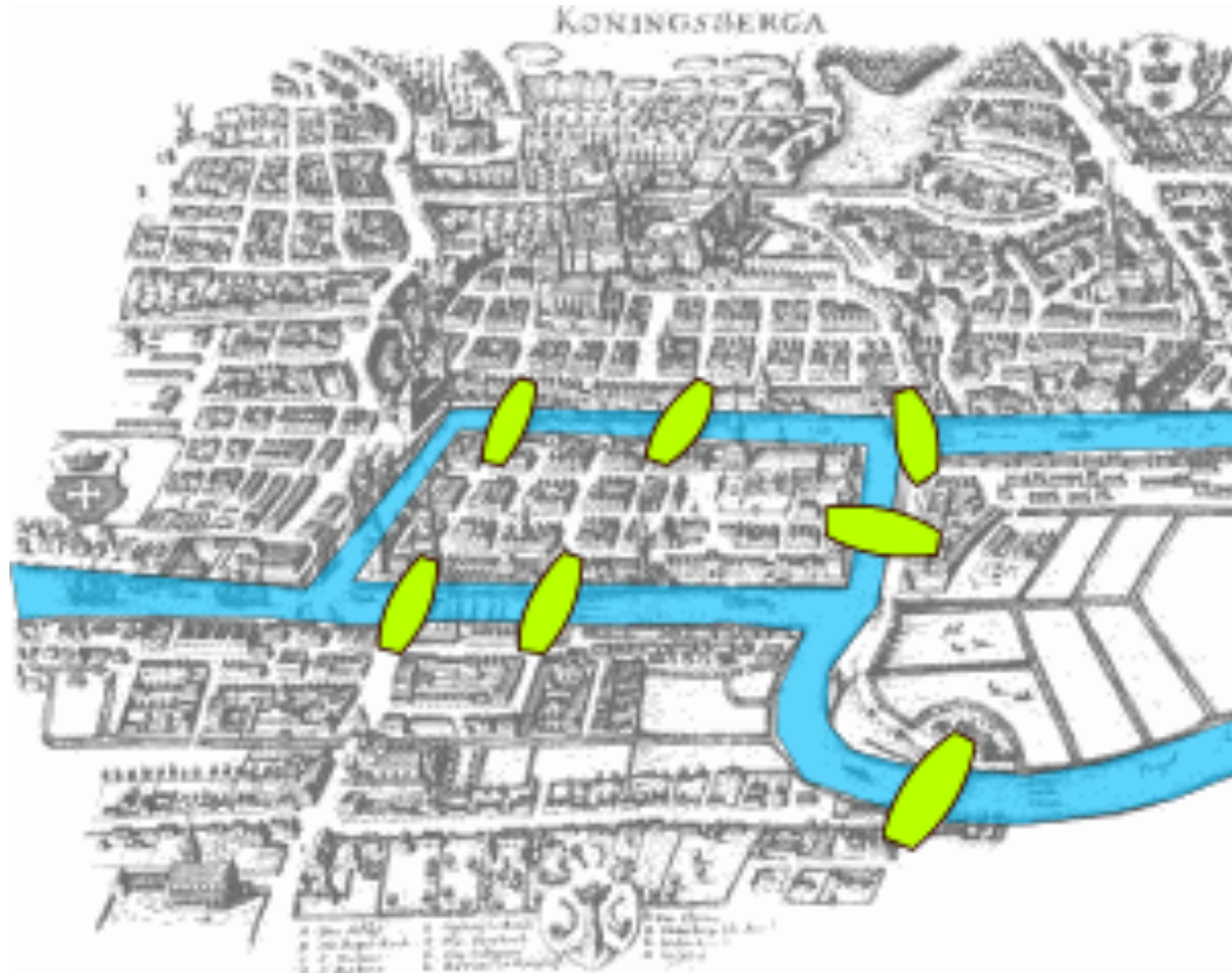
Hypergraph



Bipartite Graph



# Königsberg Bridge Problem (1736)



Only possible with a graph with at most two nodes with an odd number of links.  
This graph has four nodes with odd number of links.

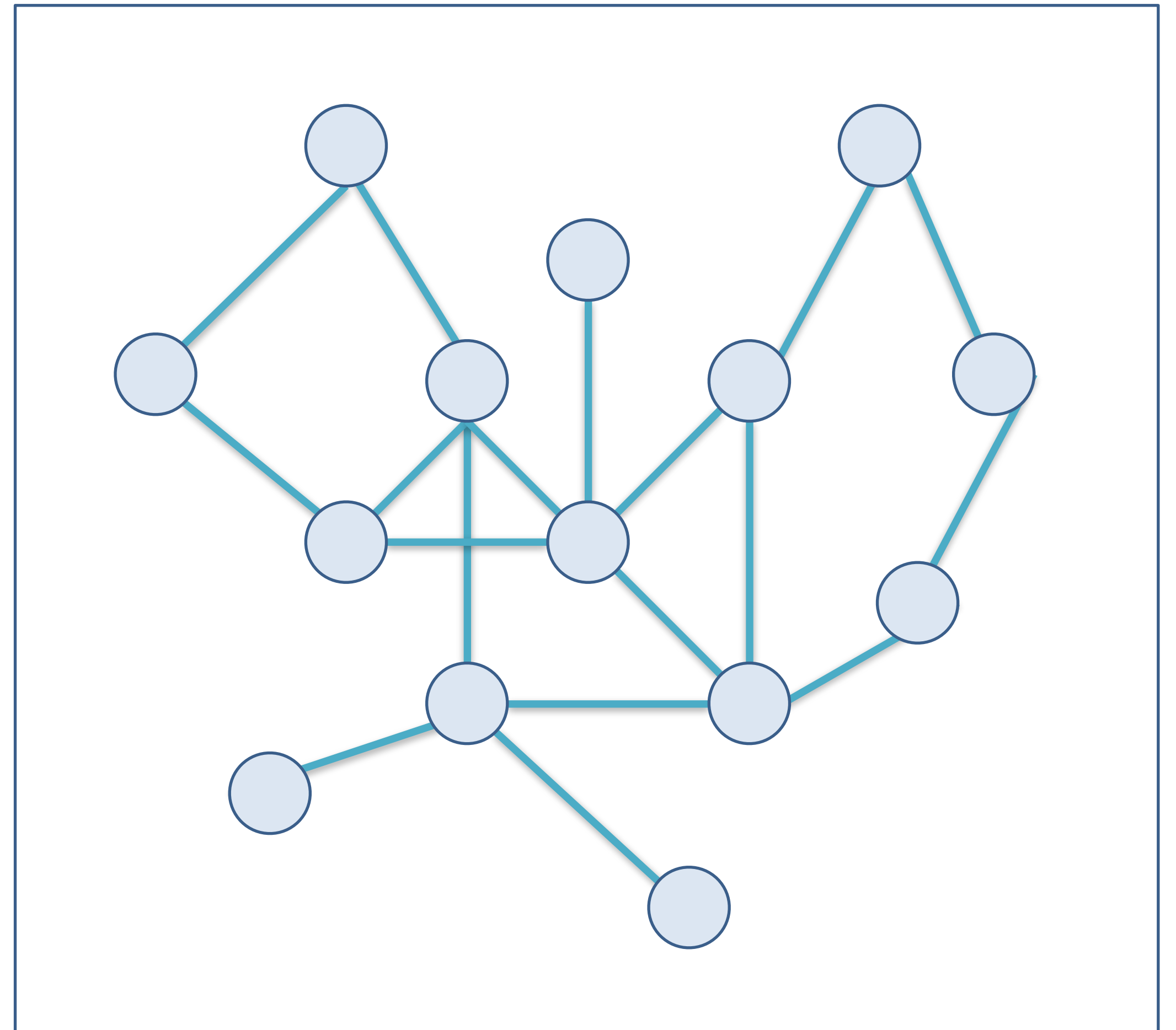


# Graph Terms

A graph  $G(V,E)$  consists of a set of **vertices V** (also called nodes) and a

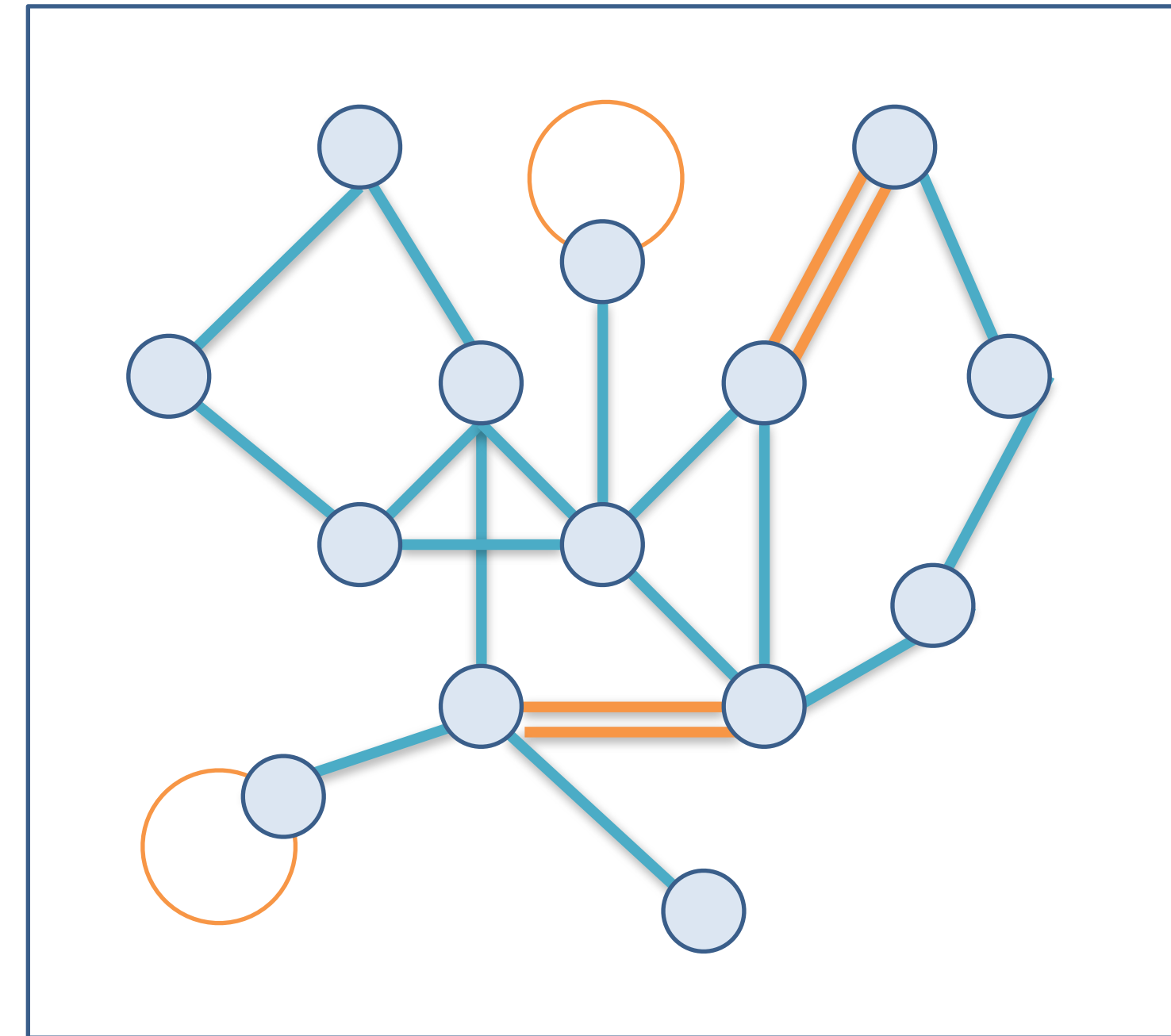
set of **edges E** (also called links) connecting these vertices.

**Graph** and **Network** are often used interchangeably



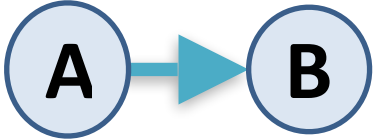
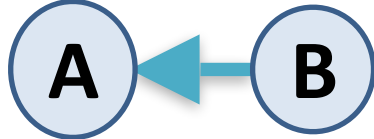
# Graph Term: Simple Graph

A simple graph  $G(V,E)$  is a graph which contains **no multi-edges** and **no loops**



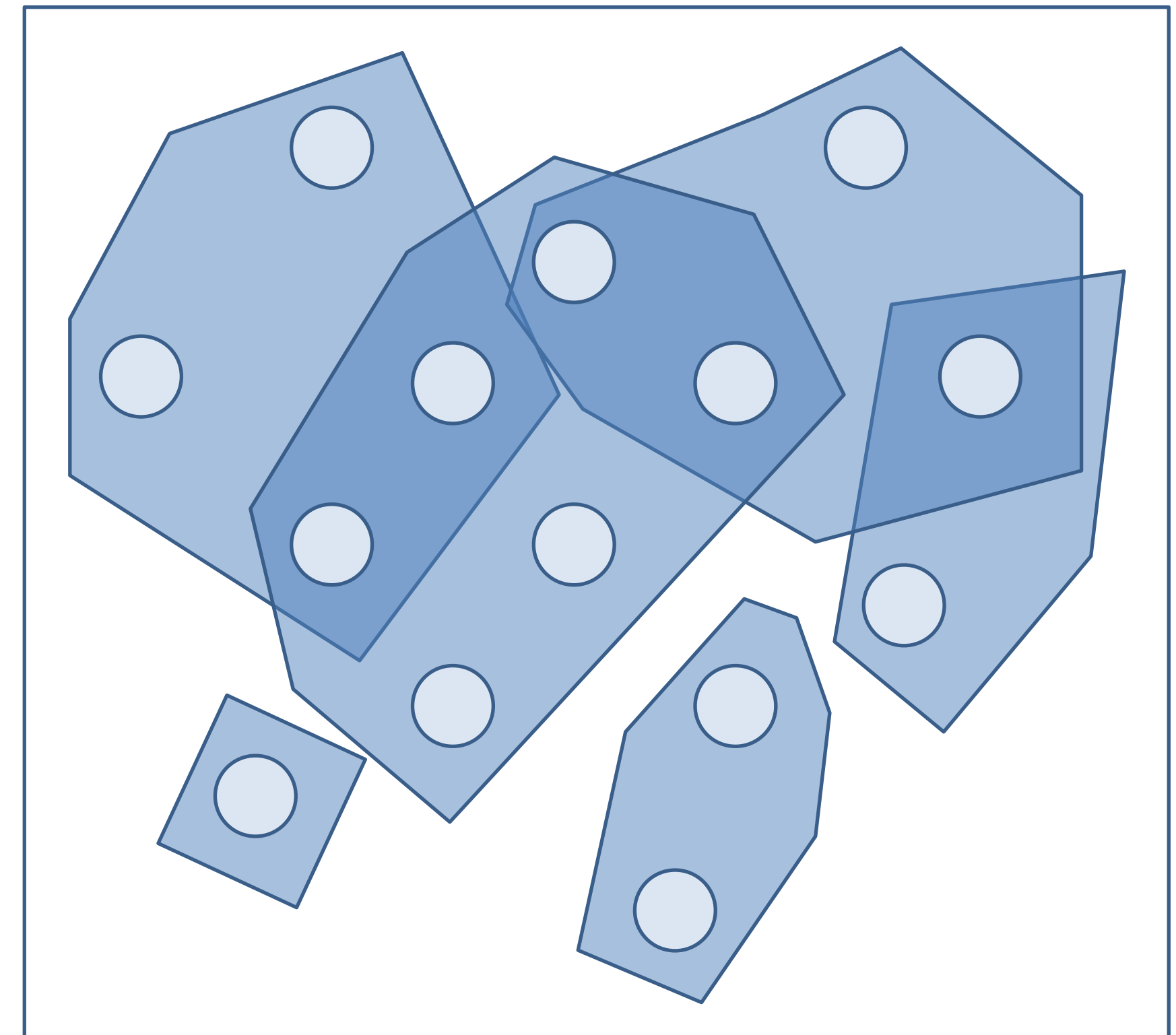
Not a simple graph!  
→ A *general graph*

# Graph Term: Directed Graph

A directed graph (digraph) is a graph that discerns between the edges  and .

# Graph Terms: Hypergraph

A hypergraph is a graph with edges connecting any number of vertices.



Hypergraph Example

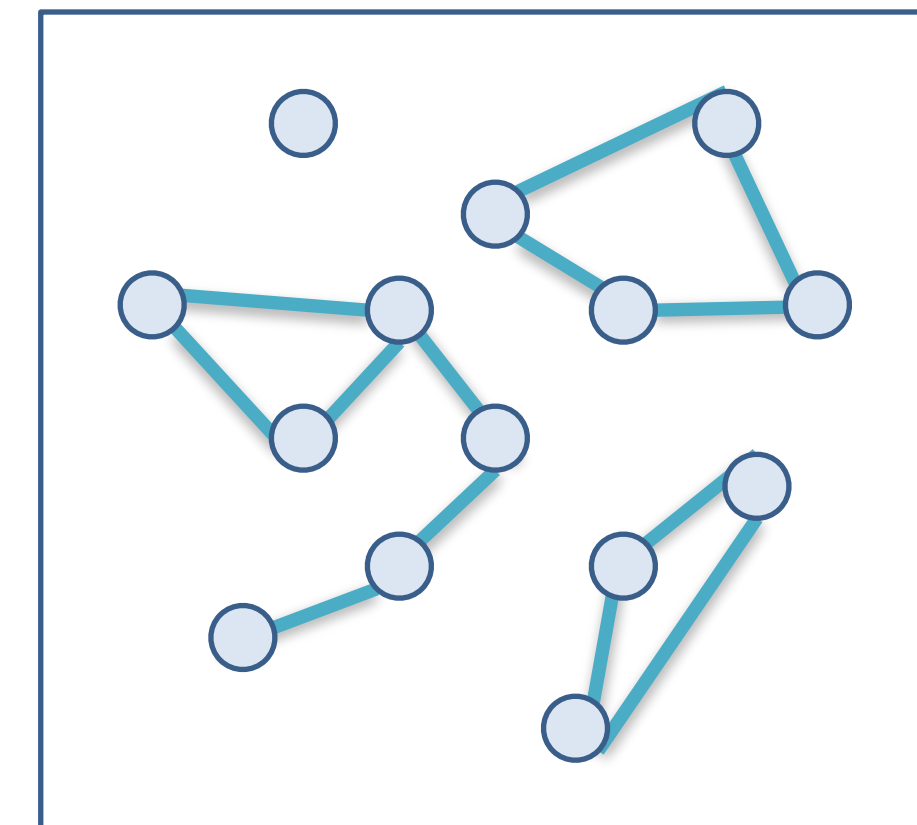
# Unconnected Graphs, Articulation Points

## *Unconnected graph*

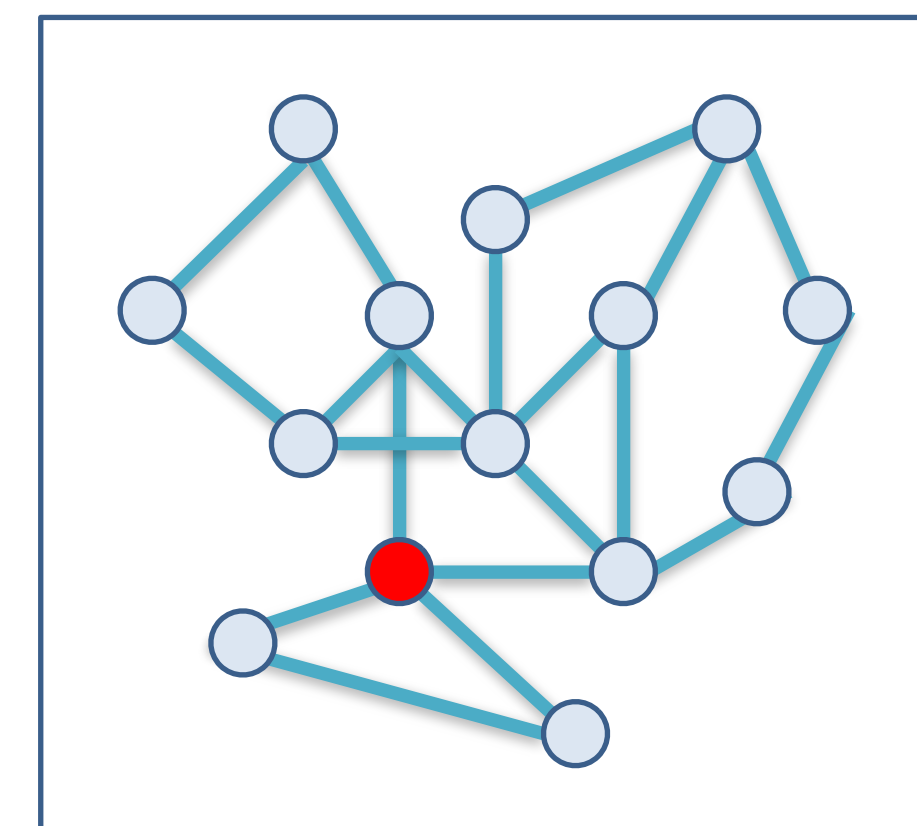
An edge traversal starting from a given vertex cannot reach any other vertex.

## *Articulation point*

Vertices, which if deleted from the graph, would break up the graph in multiple sub-graphs.



Unconnected Graph

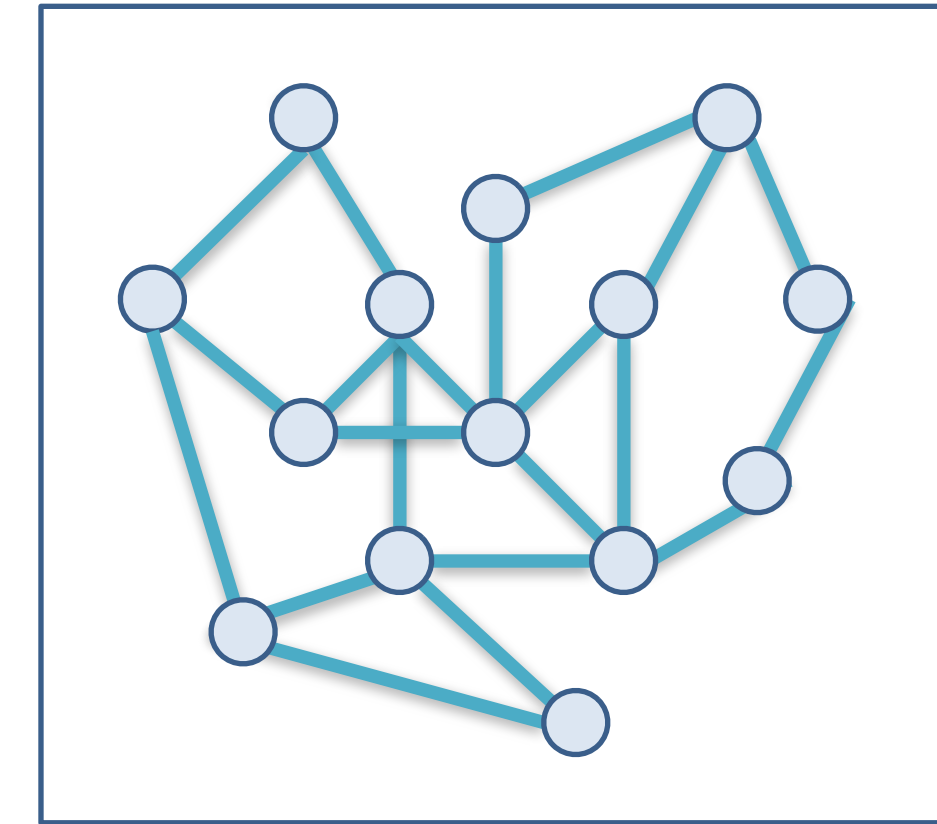


Articulation Point (red)

# Biconnected, Bipartite Graphs

## *Biconnected graph*

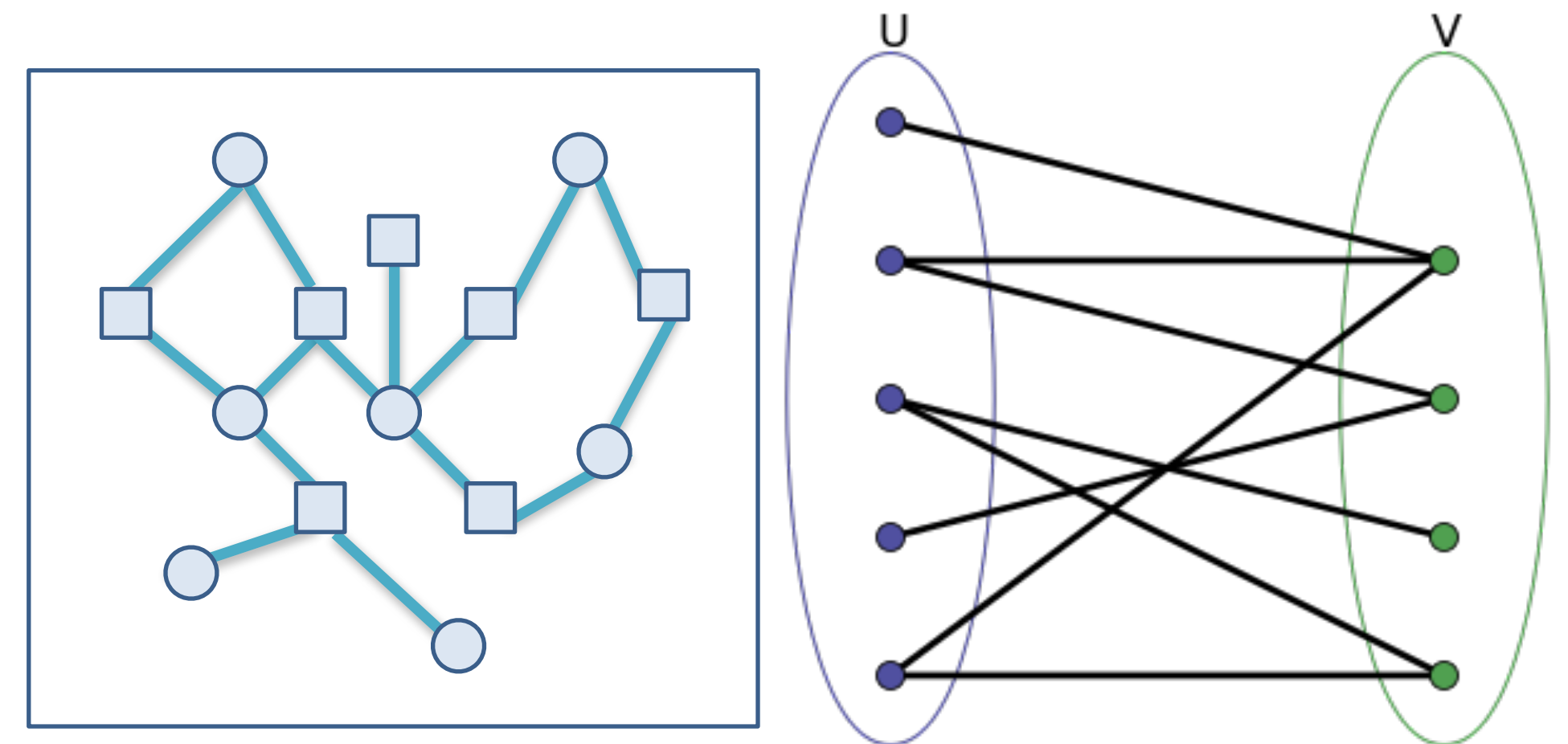
A graph without articulation points.



Biconnected Graph

## *Bipartite graph*

The vertices can be partitioned in two independent sets.



Bipartite Graph

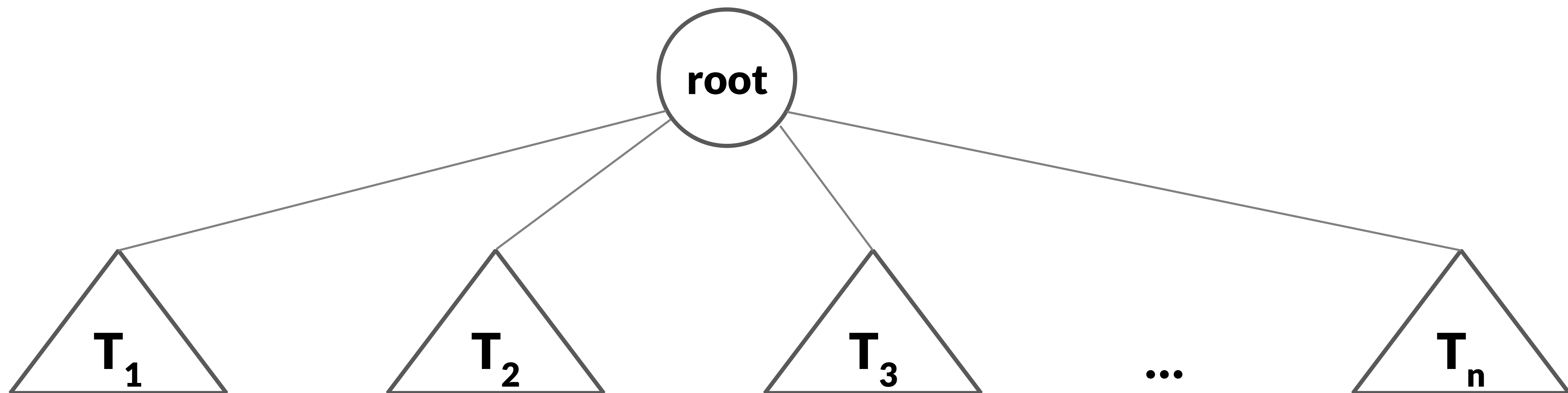
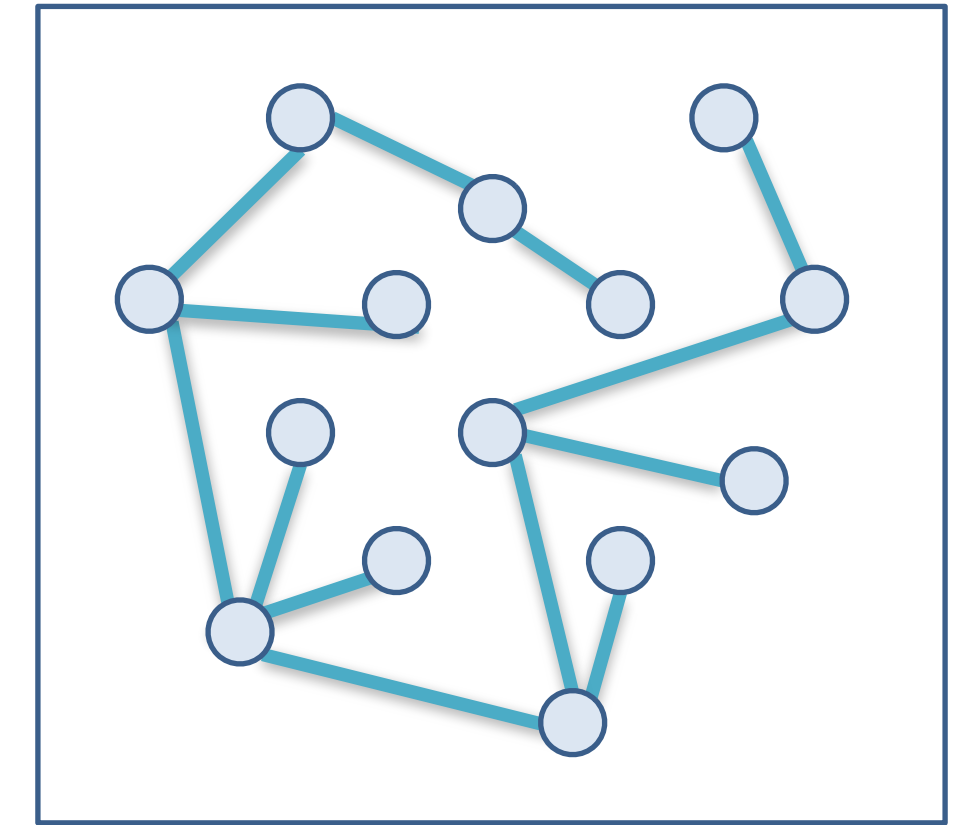
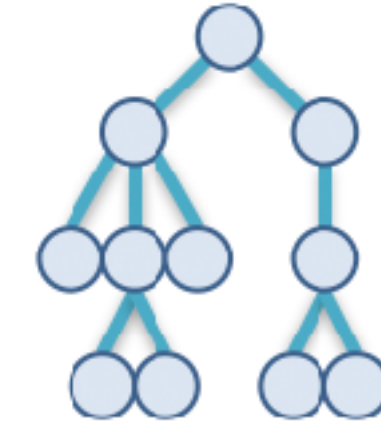
# Tree

**A graph with no cycles - or:**

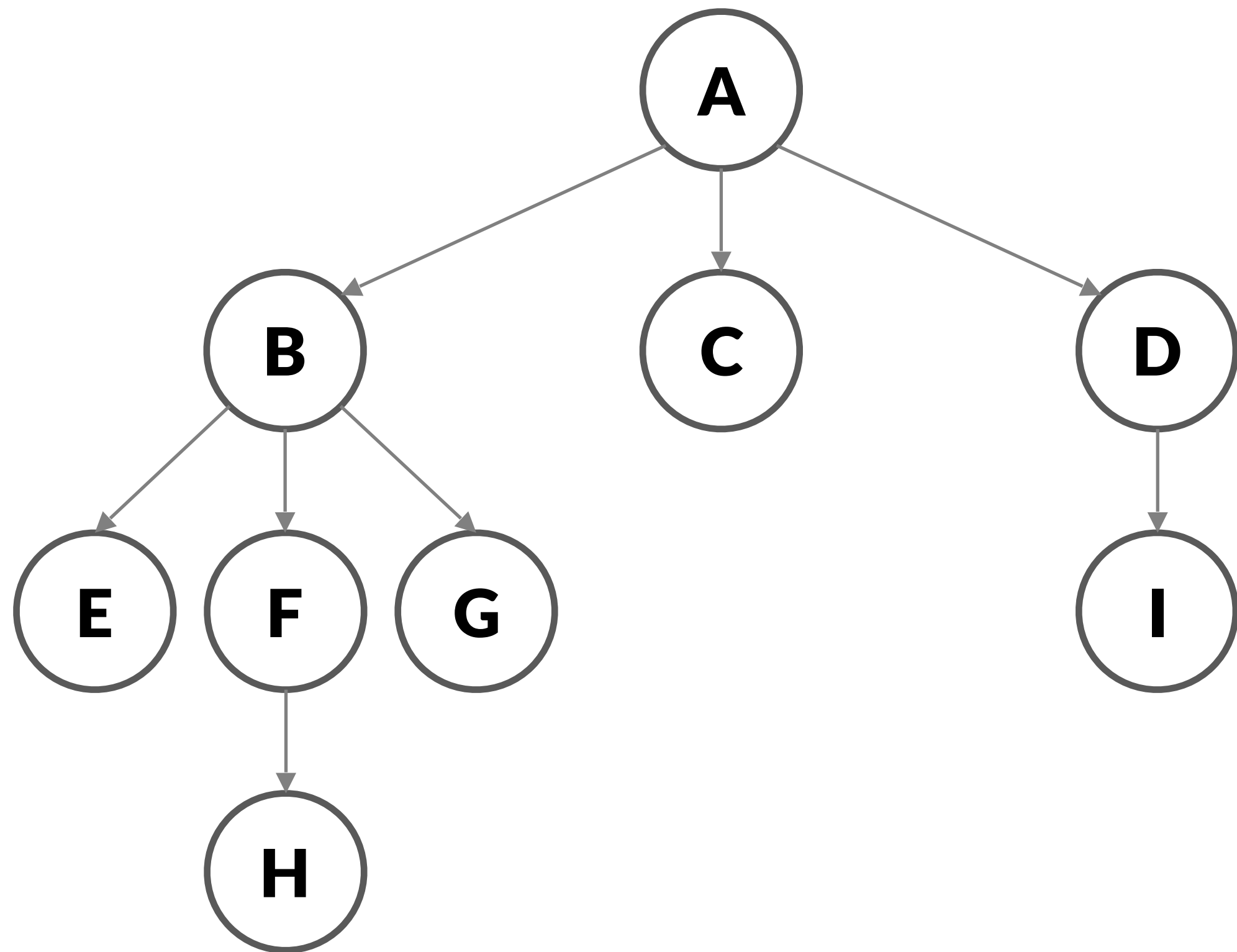
**A collection of nodes**

**contains a root node and 0-n subtrees**

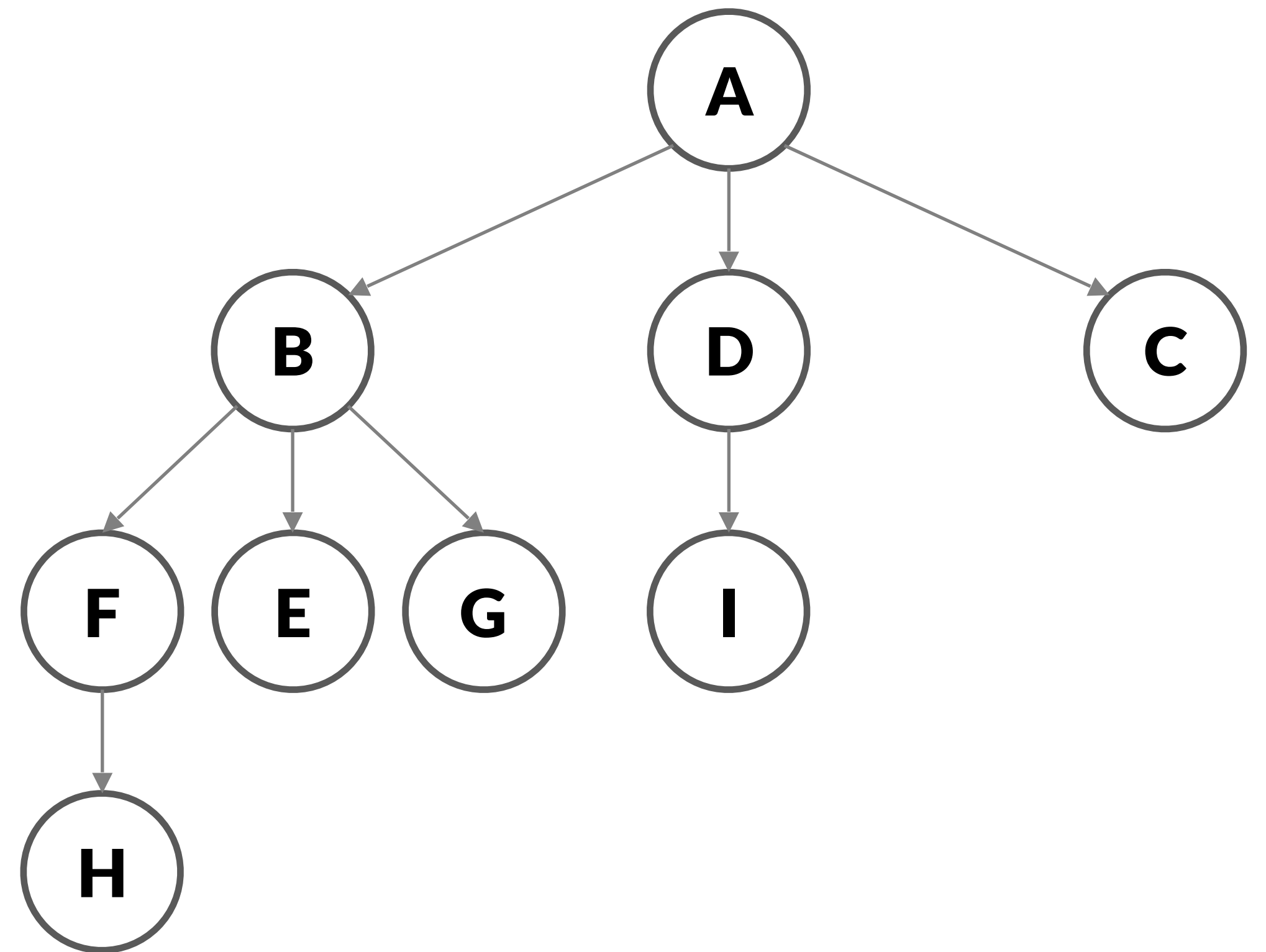
**subtrees are connected to root by an edge**



# Ordered Tree



≠

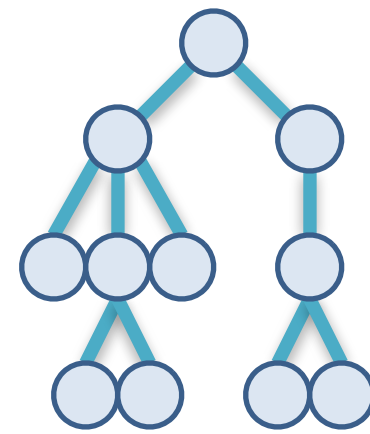




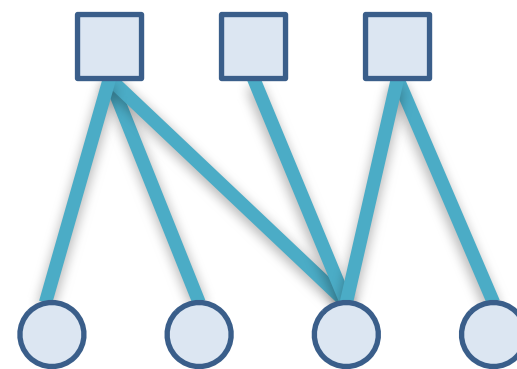
# Different Kinds of Graphs

Over 1000 different graph classes

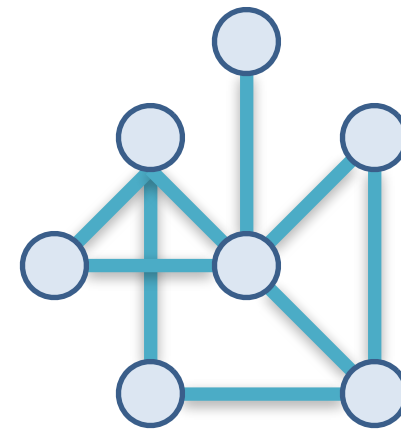
Tree



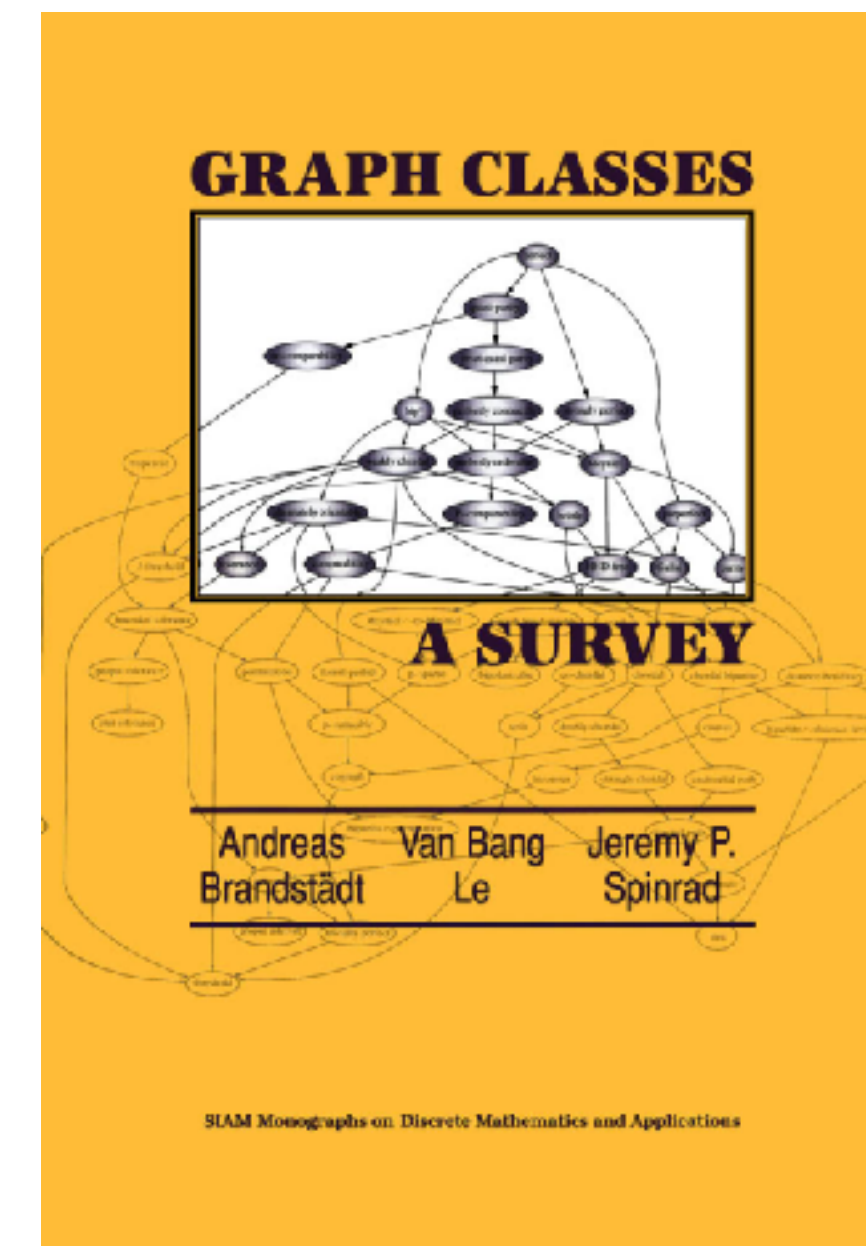
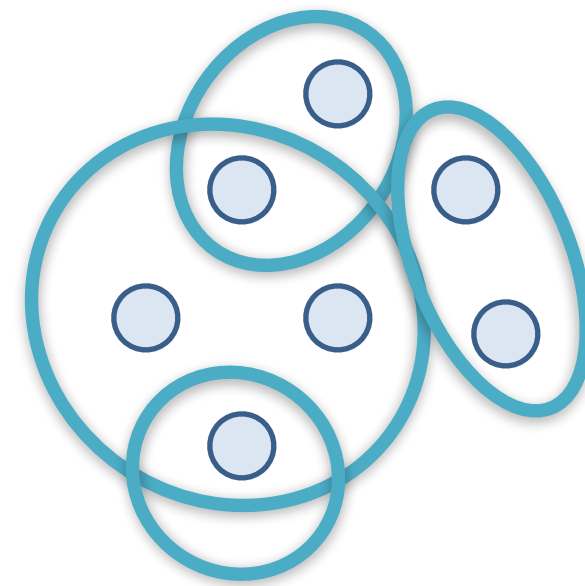
Bipartite Graph



Network



Hypergraph



A. Brandstädt et al. 1999

# Degree

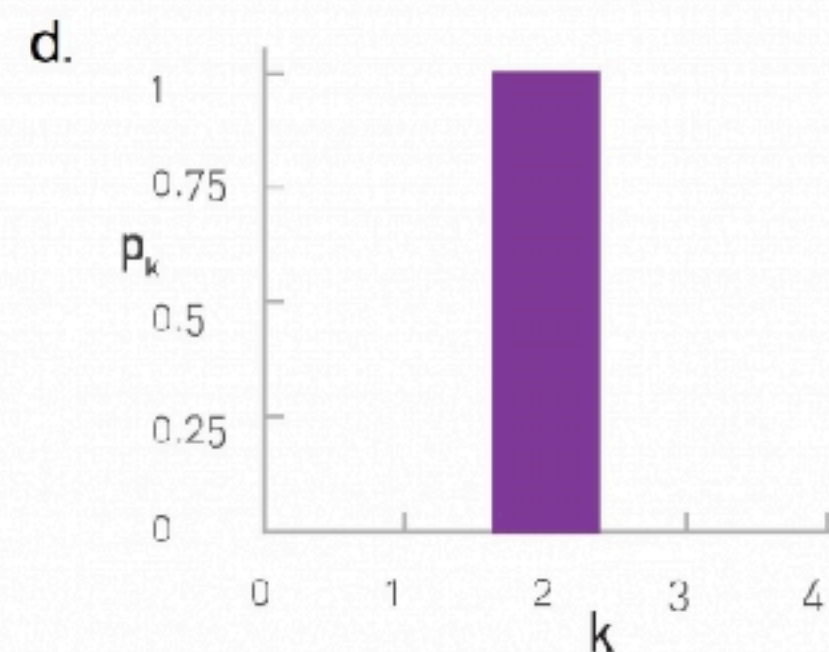
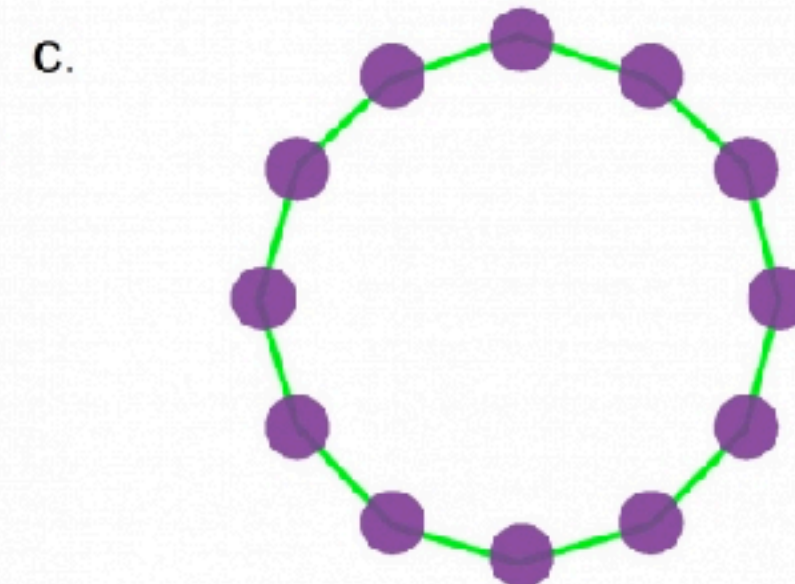
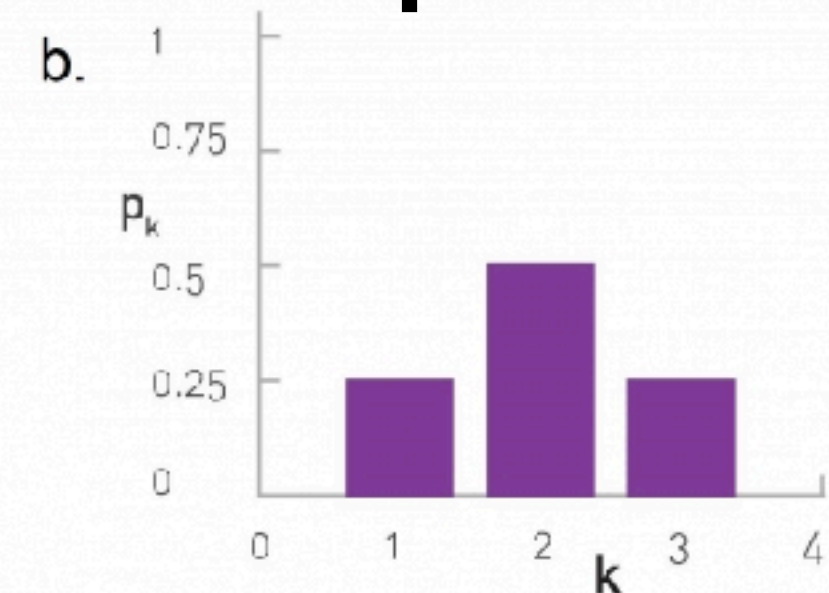
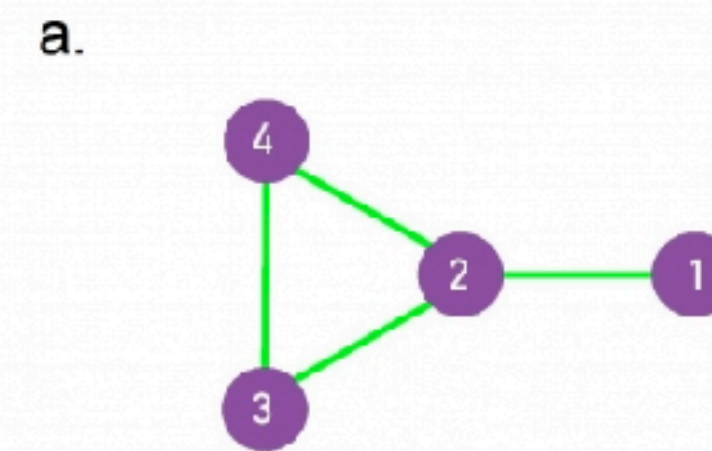
## Node degree $\deg(x)$

The number of edges being incident to this node. For directed graphs indeg/outdeg are considered separately.

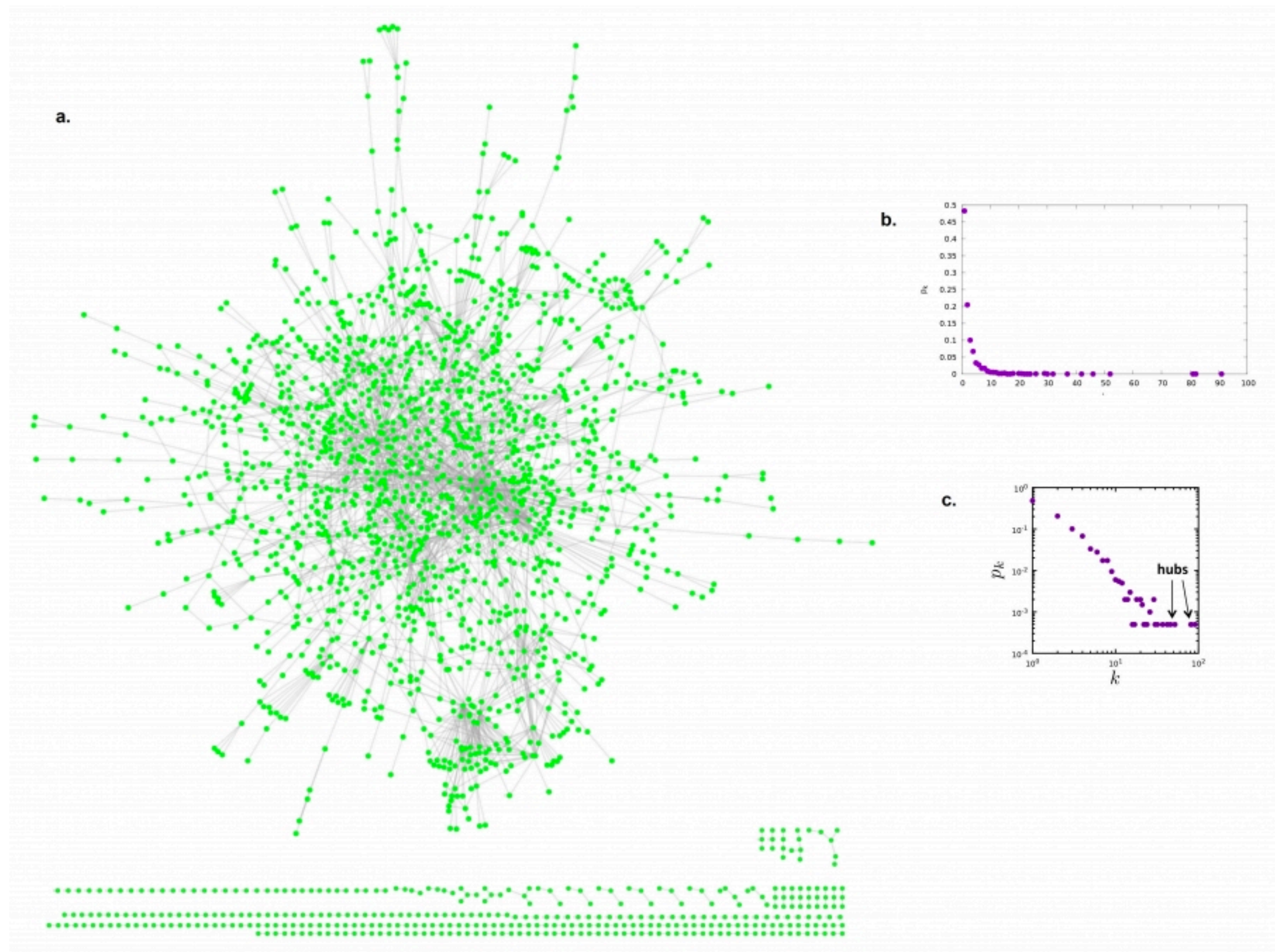
## Average degree

$$\langle k \rangle = \frac{1}{N} \sum_{i=1}^N k_i = \frac{2L}{N}$$

## Degree distribution



# Degree Distribution of a real Network

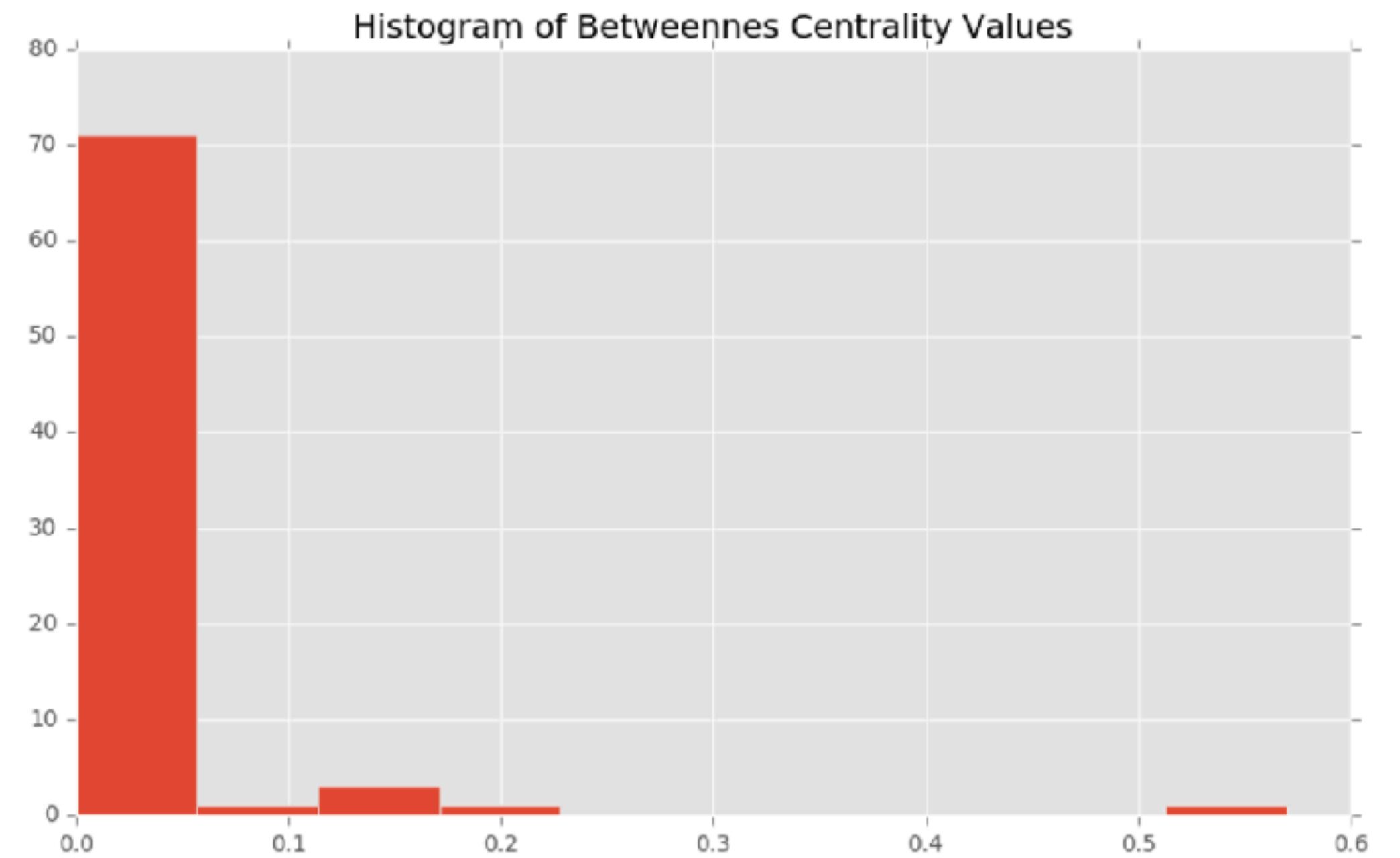
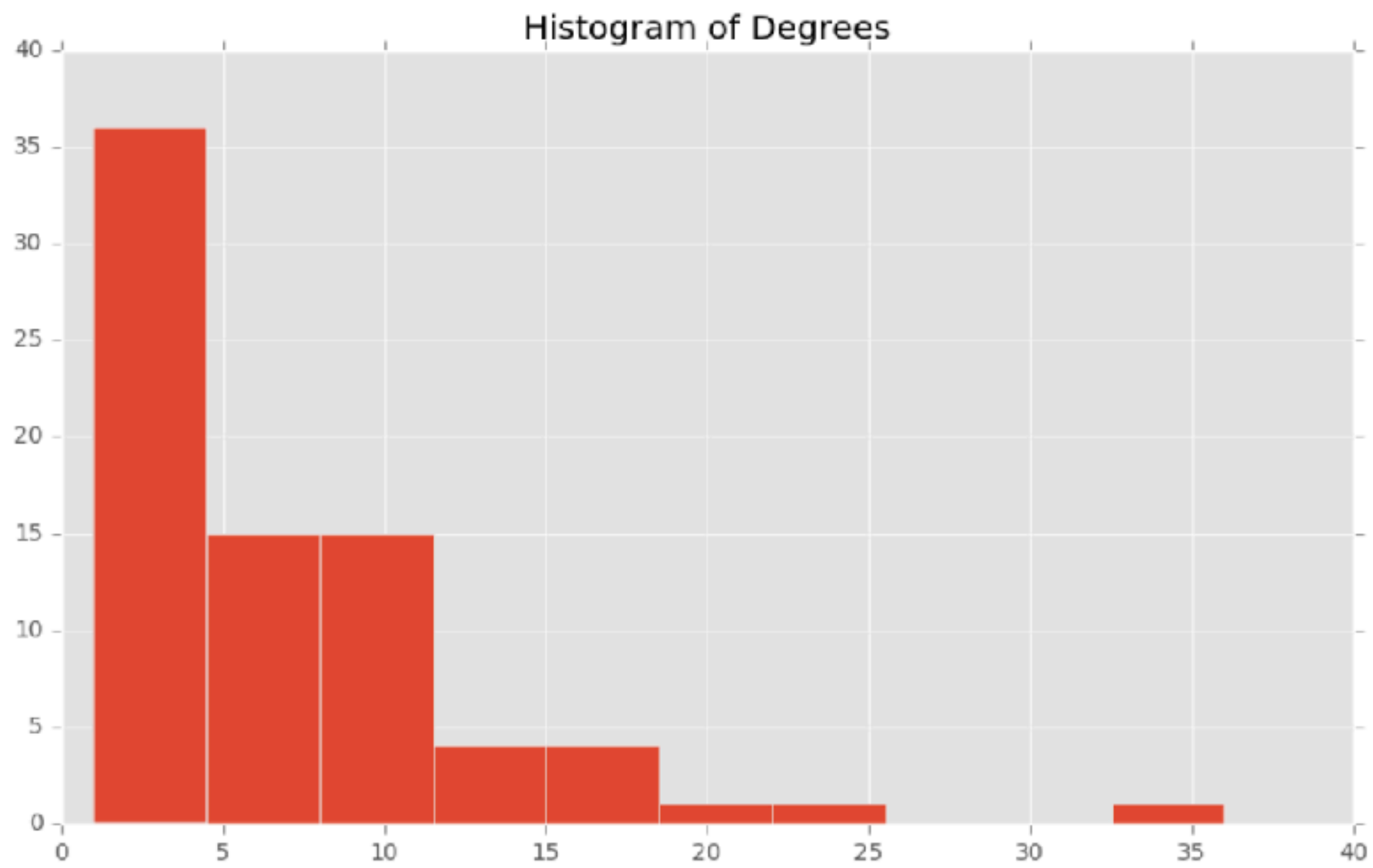


Protein Interaction Network





# Degree vs BC



# Paths & Distances

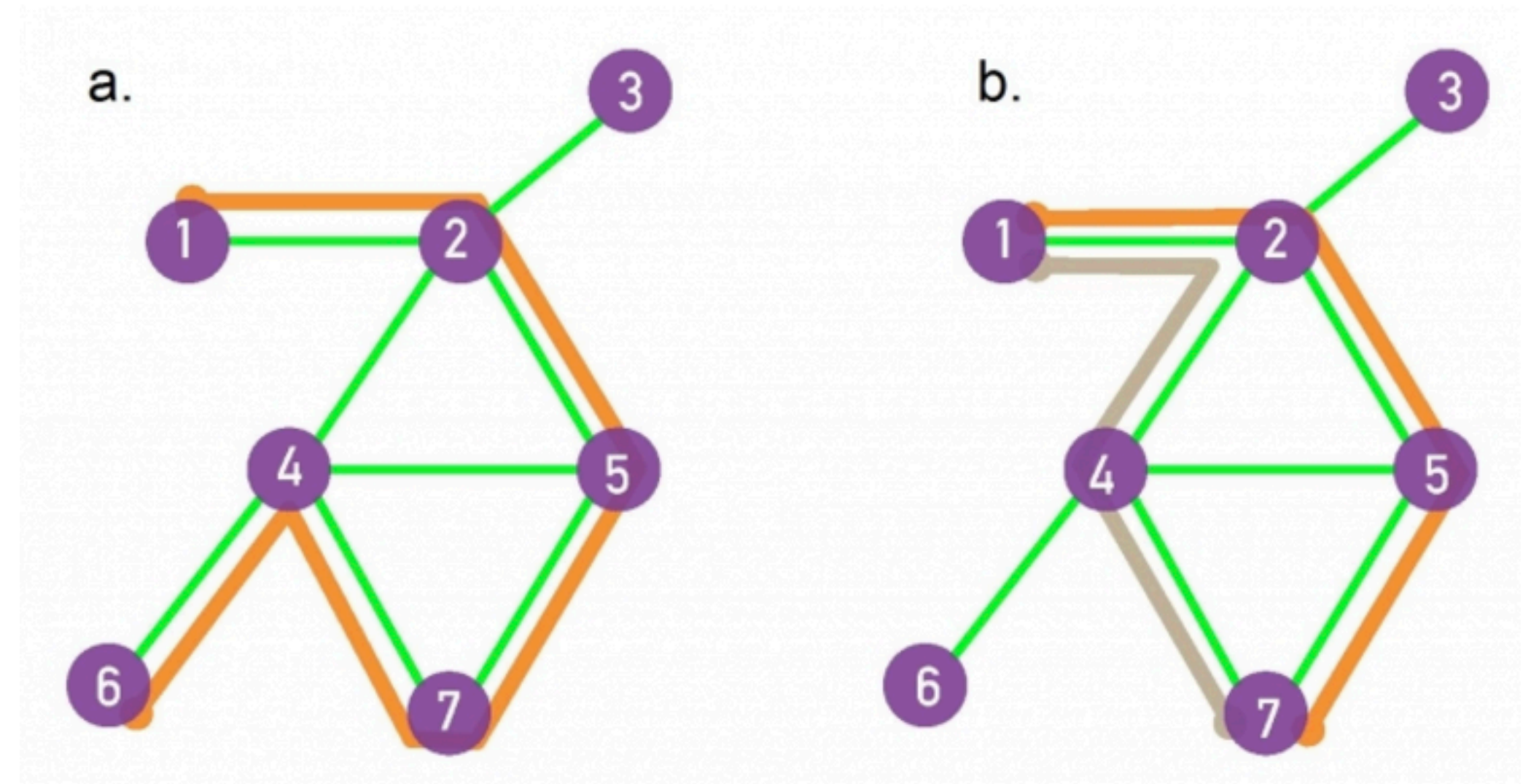
Path is **route along links**

Path length is the **number of links** contained

Shortest paths connects nodes  $i$  and  $j$  with the smallest number of links

**Diameter of graph  $G$**

The longest shortest path within  $G$ .



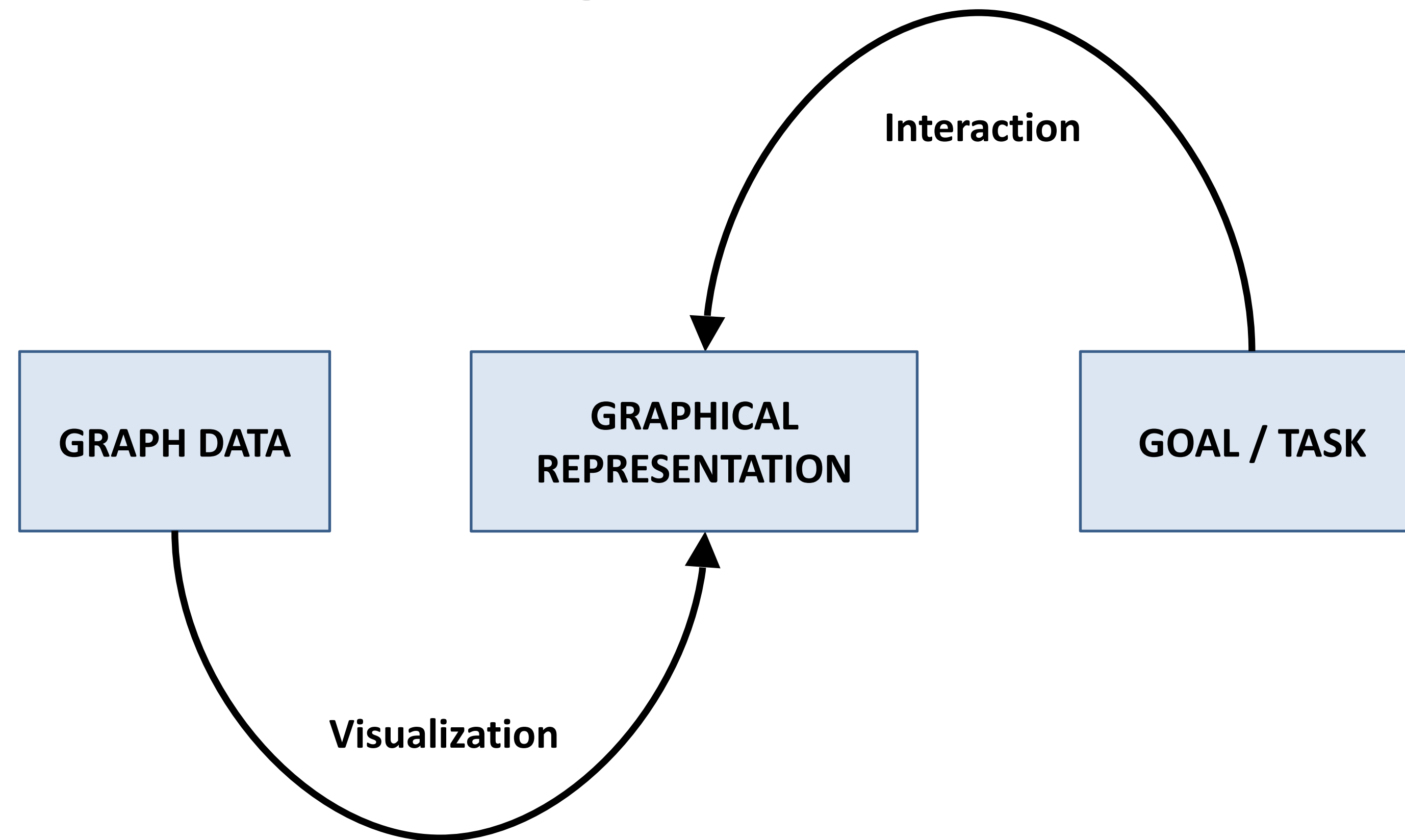
A path from 1 to 6

Shortest paths (two) from 1 to 7.

# Graph and Tree Visualization



# Setting the Stage



How to decide which **representation** to use for which **type of graph** in order to achieve which kind of **goal**?

# Different Kinds of Tasks/Goals

Two principal types of tasks: **attribute-based (ABT)** and **topology-based (TBT)**

**Localize** – find a single or multiple nodes/edges that fulfill a given property

- ABT: Find the edge(s) with the maximum edge weight.
- TBT: Find all adjacent nodes of a given node.

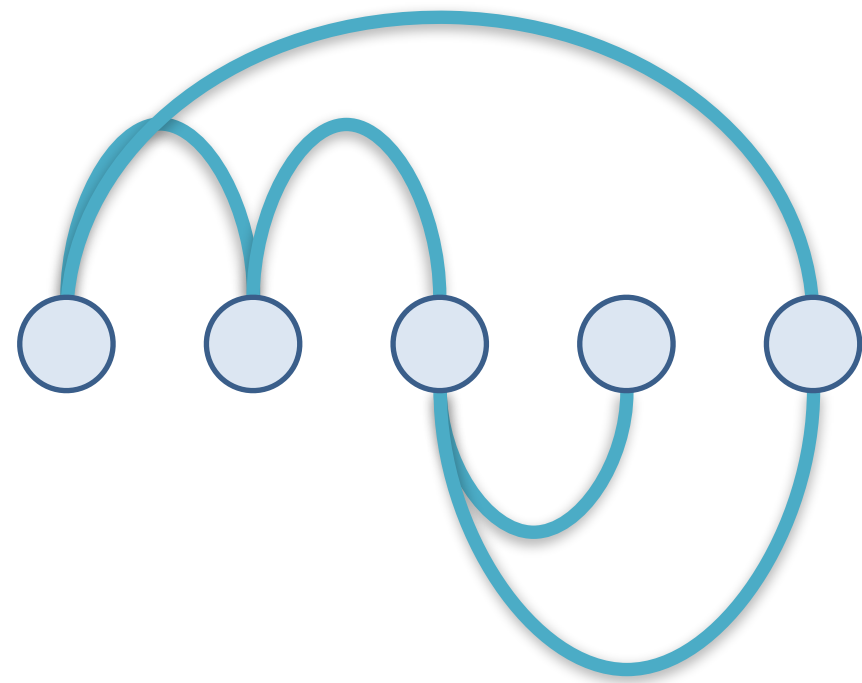
**Quantify** – count or estimate a numerical property of the graph

- ABT: Give the number of all nodes.
- TBT: Give the indegree (the number of incoming edges) of a node.

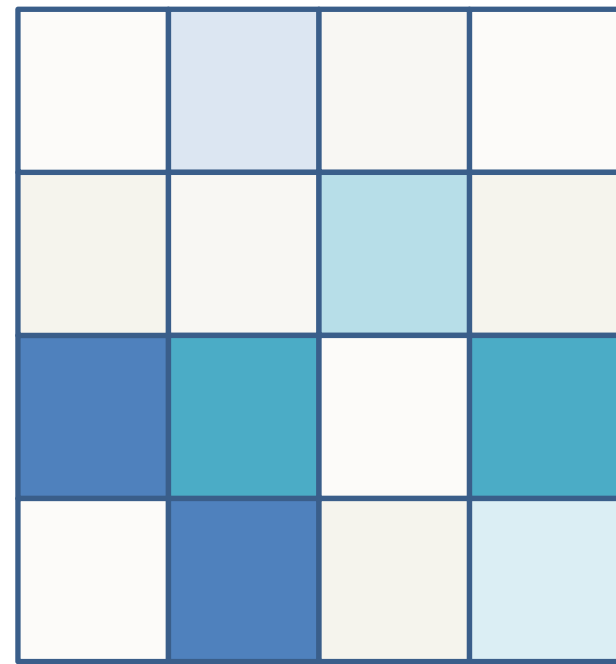
**Sort/Order** – enumerate the nodes/edges according to a given criterion

- ABT: Sort all edges according to their weight.
- TBT: Traverse the graph starting from a given node.

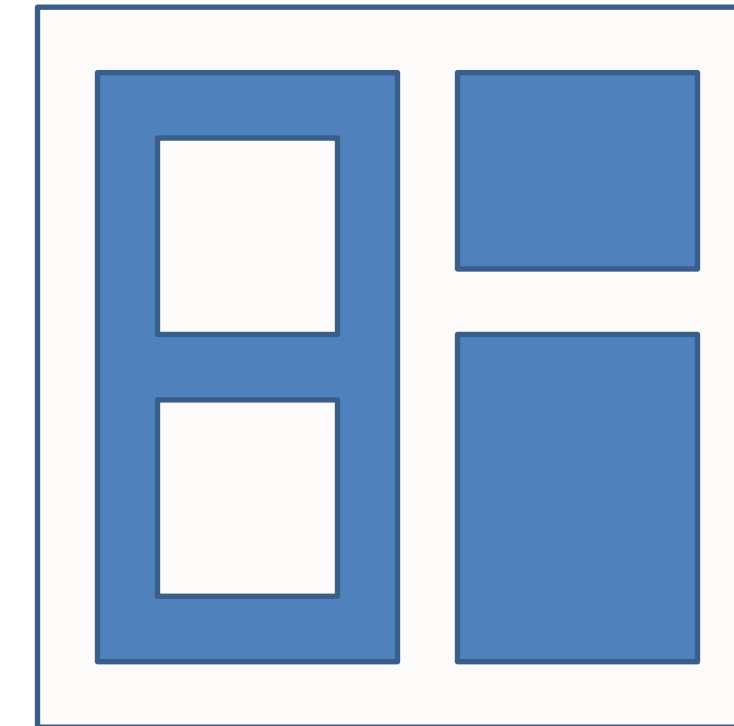
# Three Types of Graph Representations



Explicit  
(Node-Link)



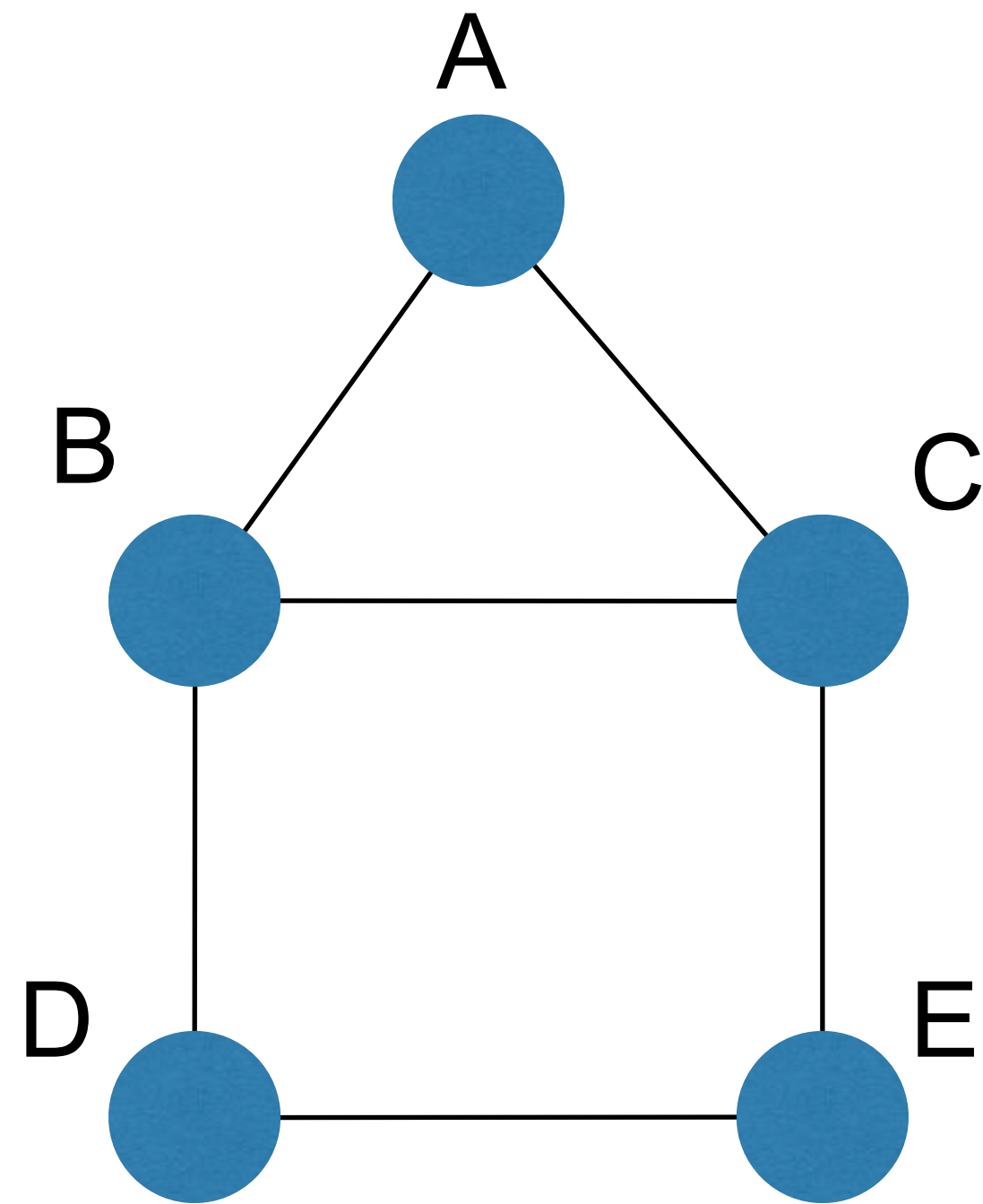
Matrix



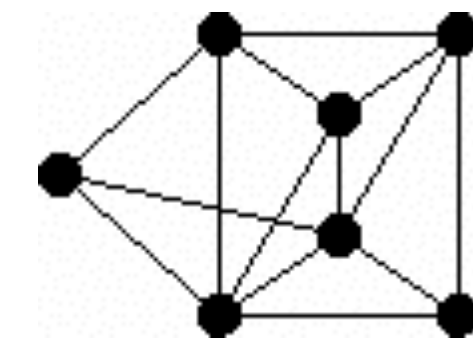
Implicit

# Explicit Graph Representations

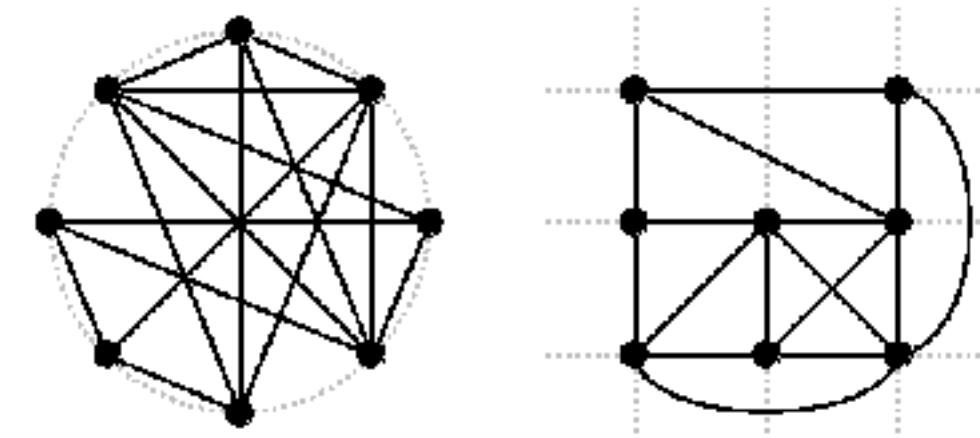
Node-link diagrams: vertex = point, edge = line/arc



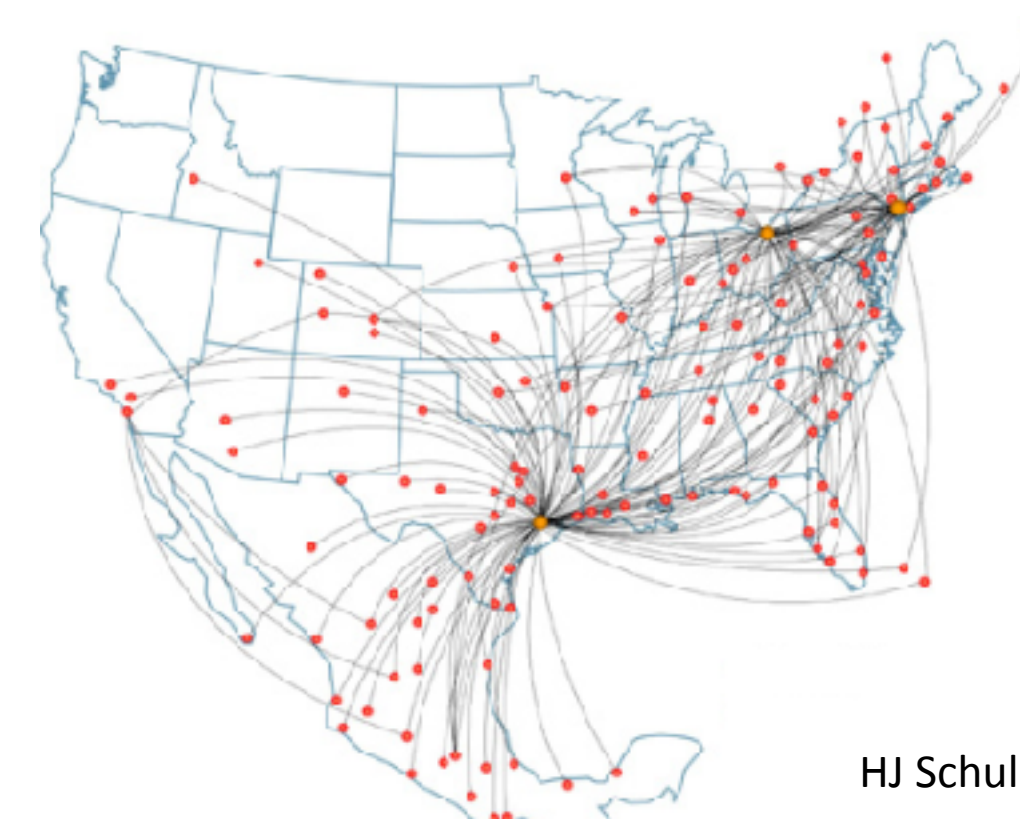
Free



Styled



Fixed



# Criteria for Good Node-Link Layout

Minimized **edge crossings**

Minimized **distance** of neighboring nodes

Minimized **drawing area**

Uniform edge **length**

Minimized edge **bends**

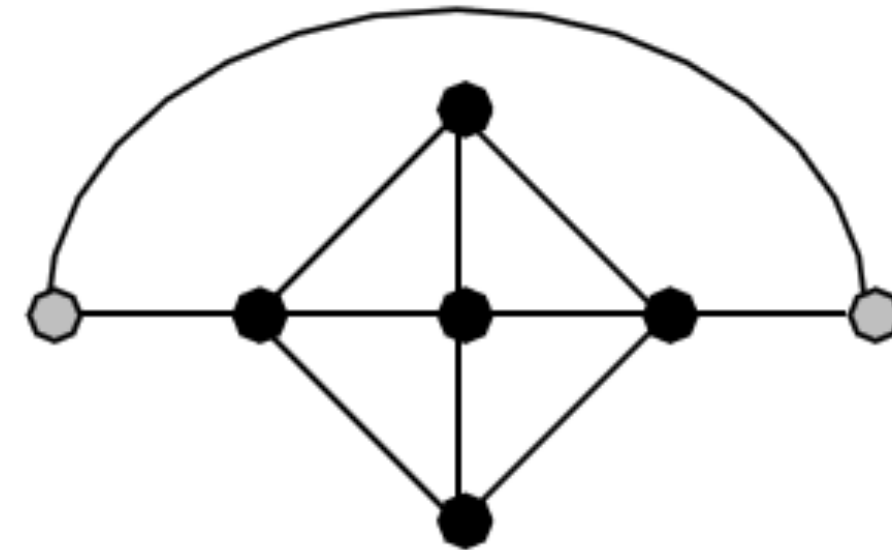
Maximized **angular distance** between different edges

Aspect ratio about 1 (not too long and not too wide)

**Symmetry**: similar graph structures should look similar

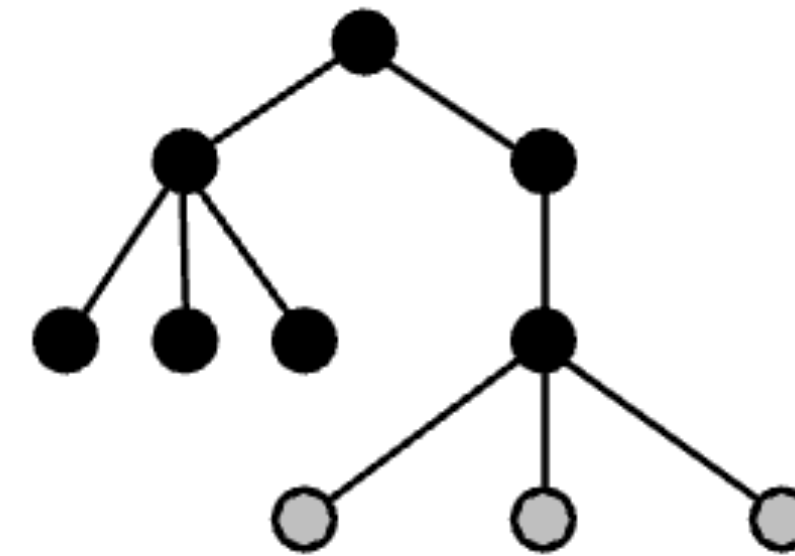
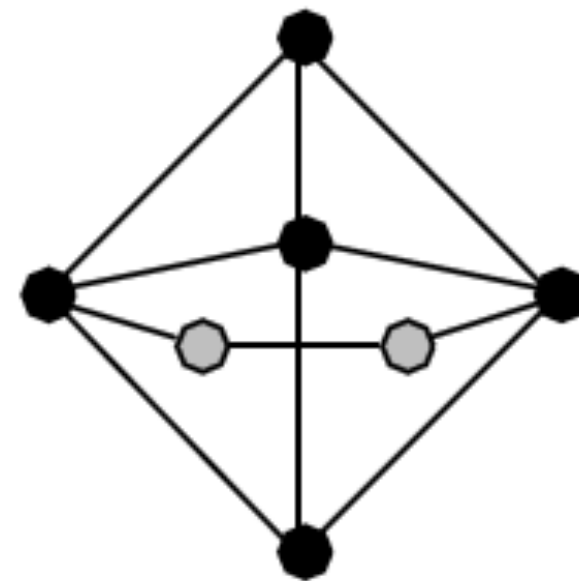
# Conflicting Criteria

Minimum number  
of edge crossings



vs.

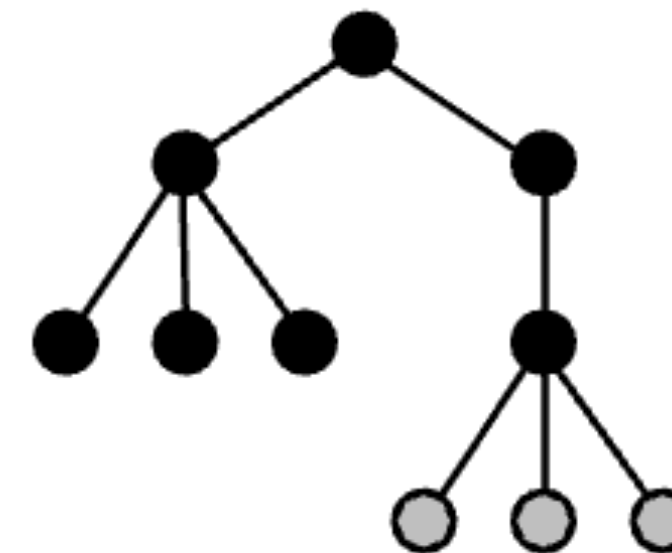
Uniform edge  
length



Space utilization

vs.

Symmetry



# Force Directed Layouts

Physics model:  
edges = springs,  
vertices = repulsive magnets

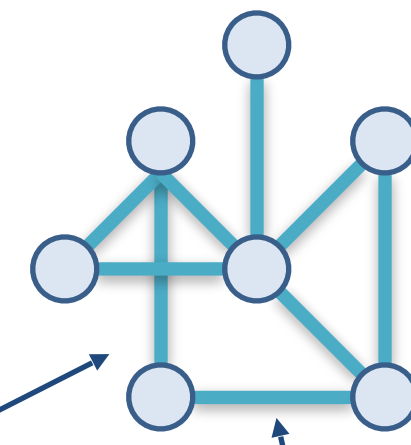
in practice: damping,  
center of gravity

Computationally  
expensive:  $O(n^3)$

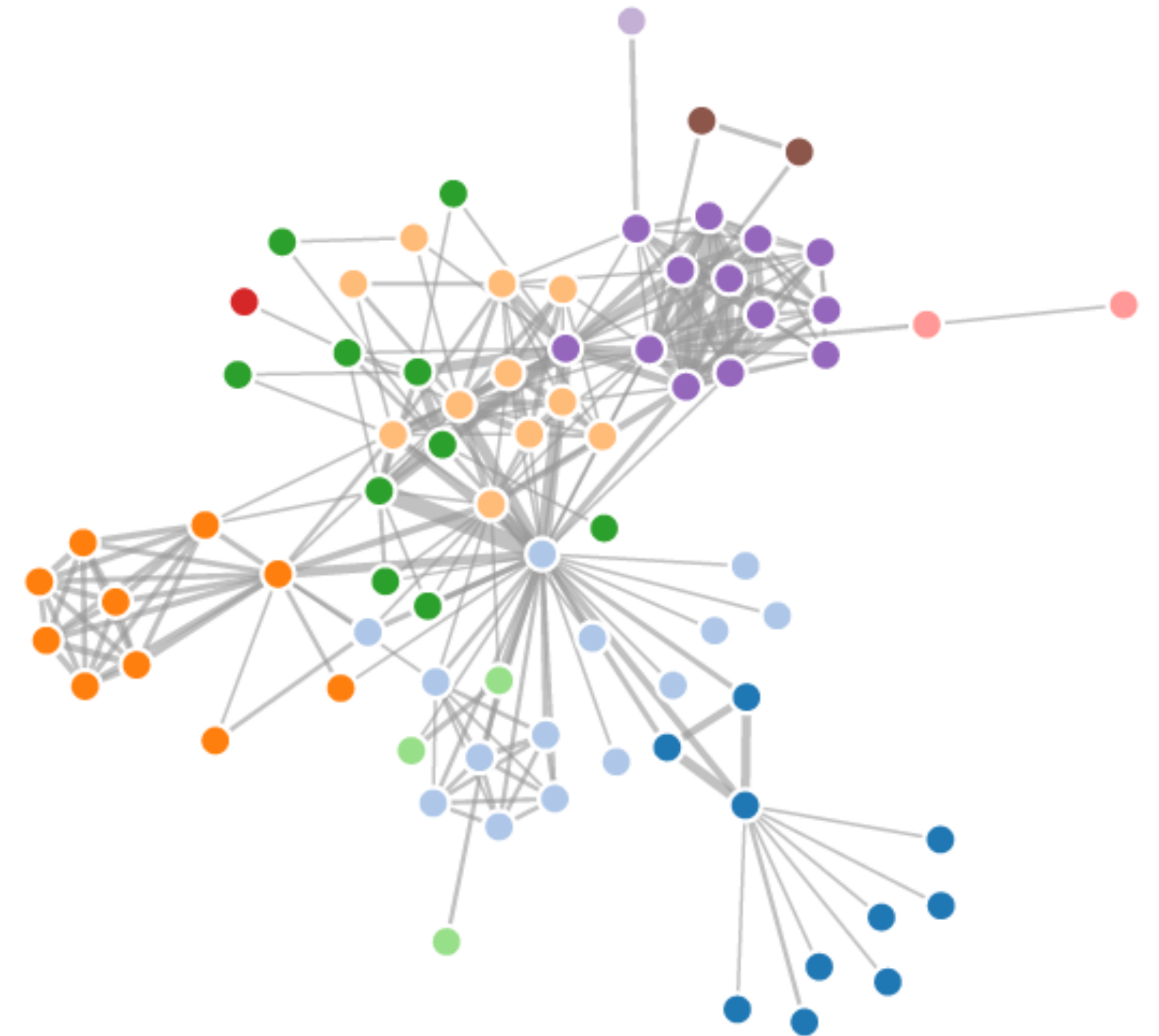
Limit (interactive):  $\sim 1000$  nodes

<http://bl.ocks.org/steveharoz/8c3e2524079a8c440df60c1ab72b5d03>

Expander  
(pushing nodes apart)



Spring Coil  
(pulling nodes together)





**Giant Hairball**



# Explicit Representations

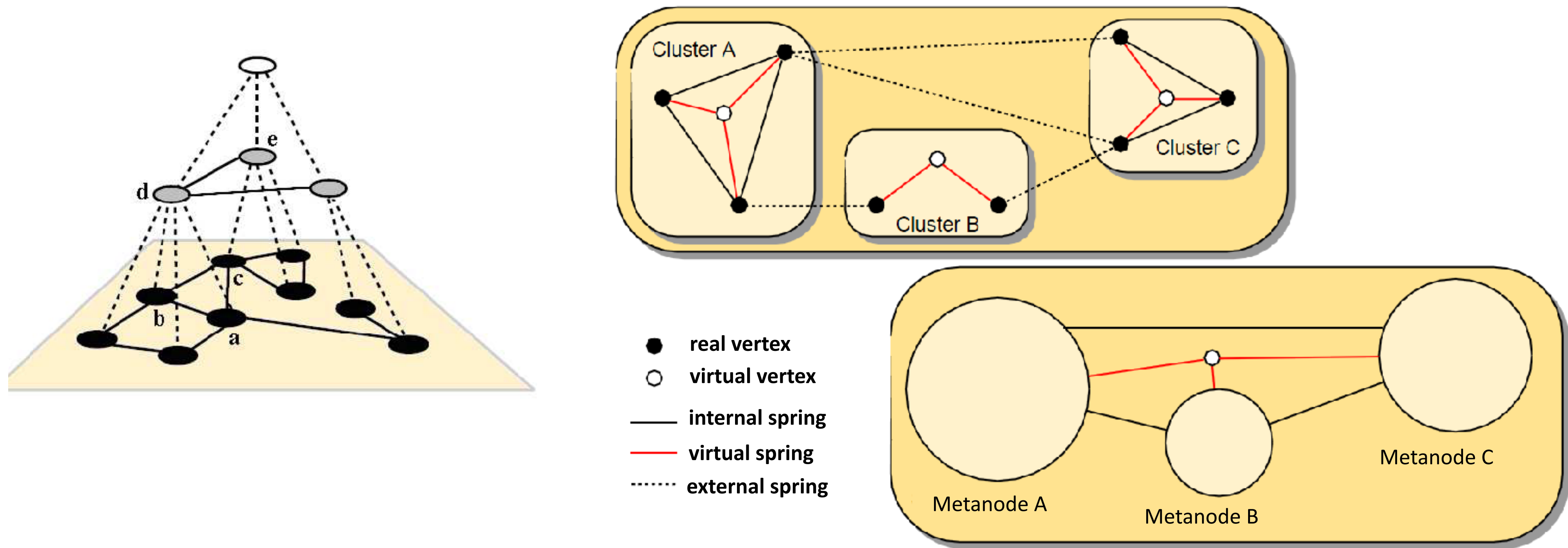
Problem #1: computing an optimal layout lies in NP

Solution approach: formulate the layout problem as an optimization problem

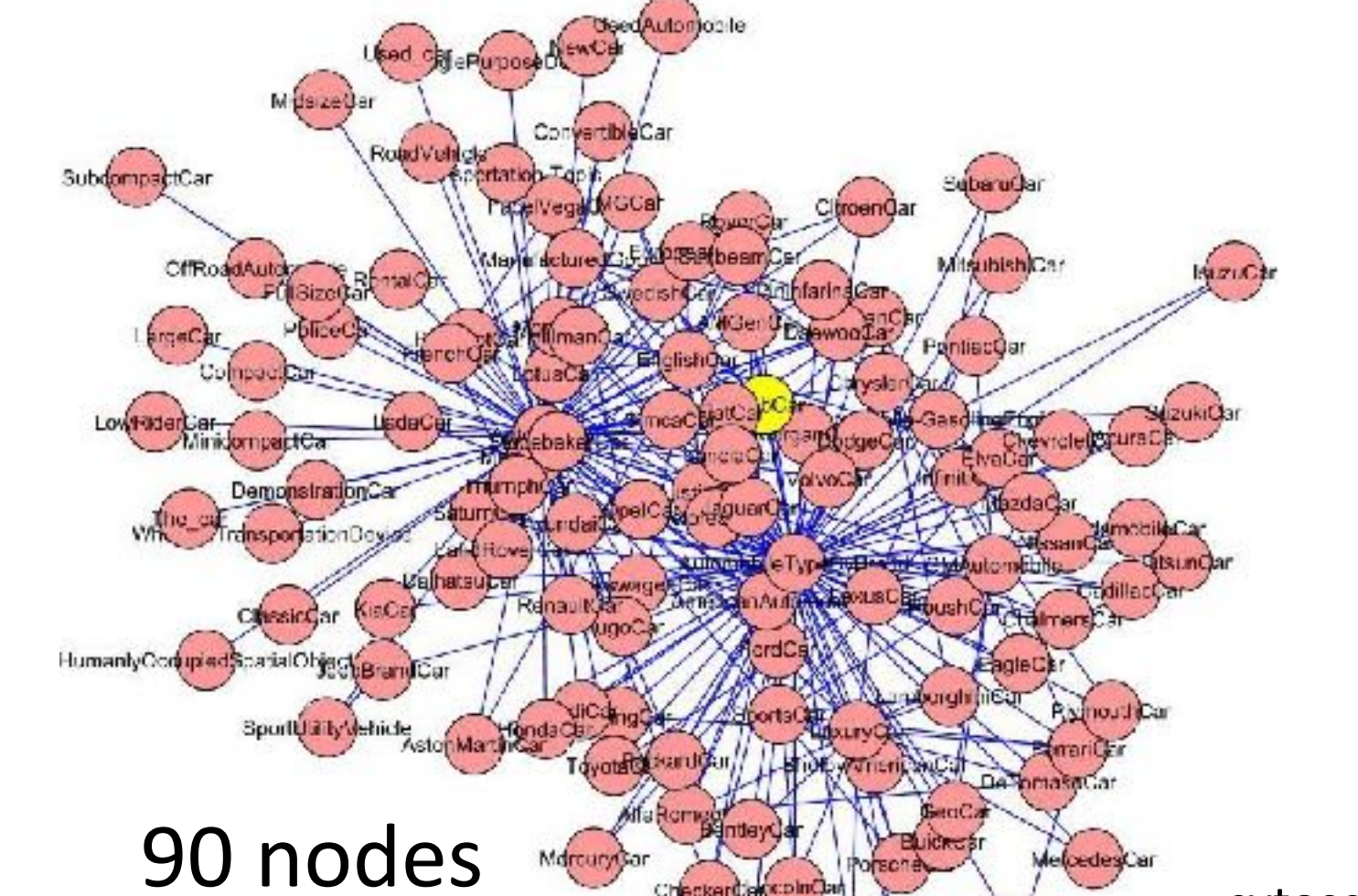
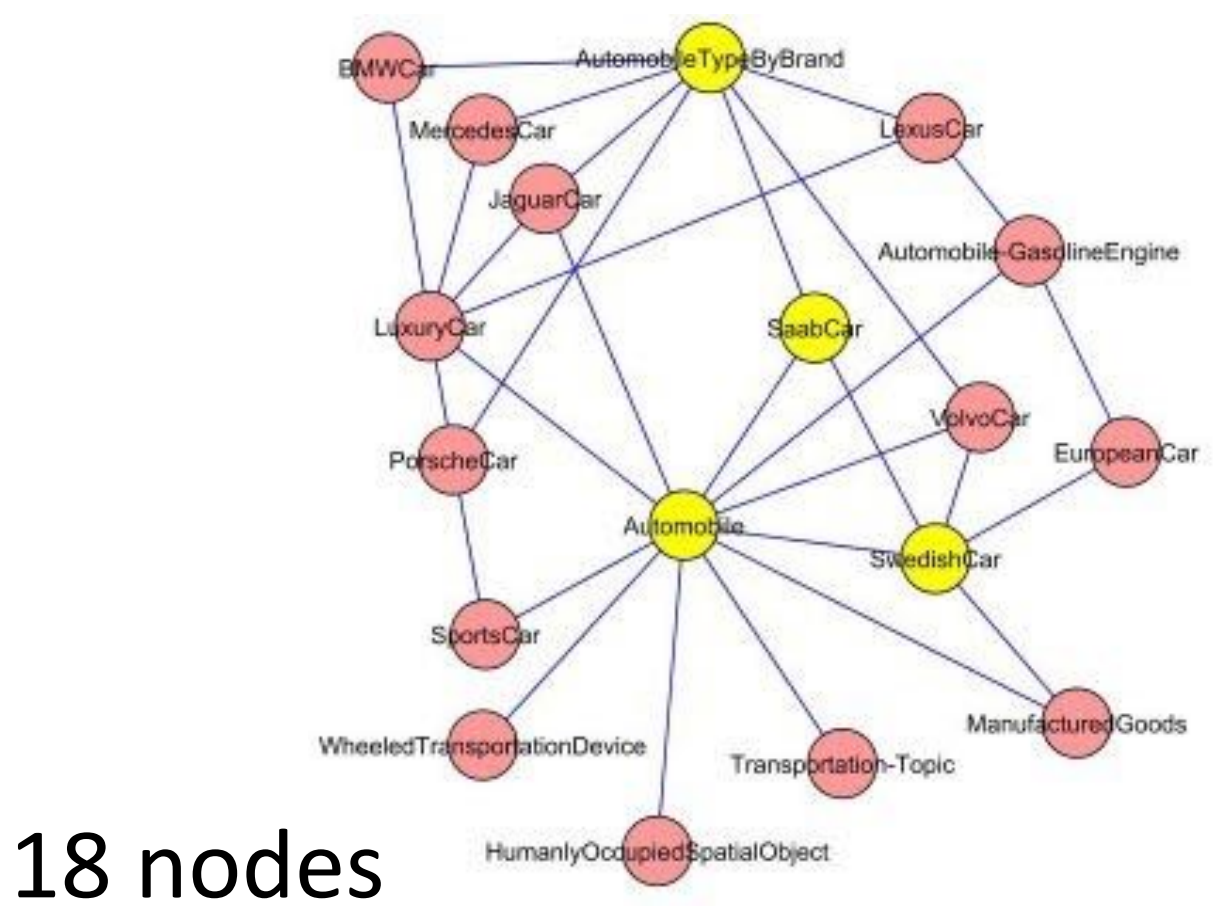
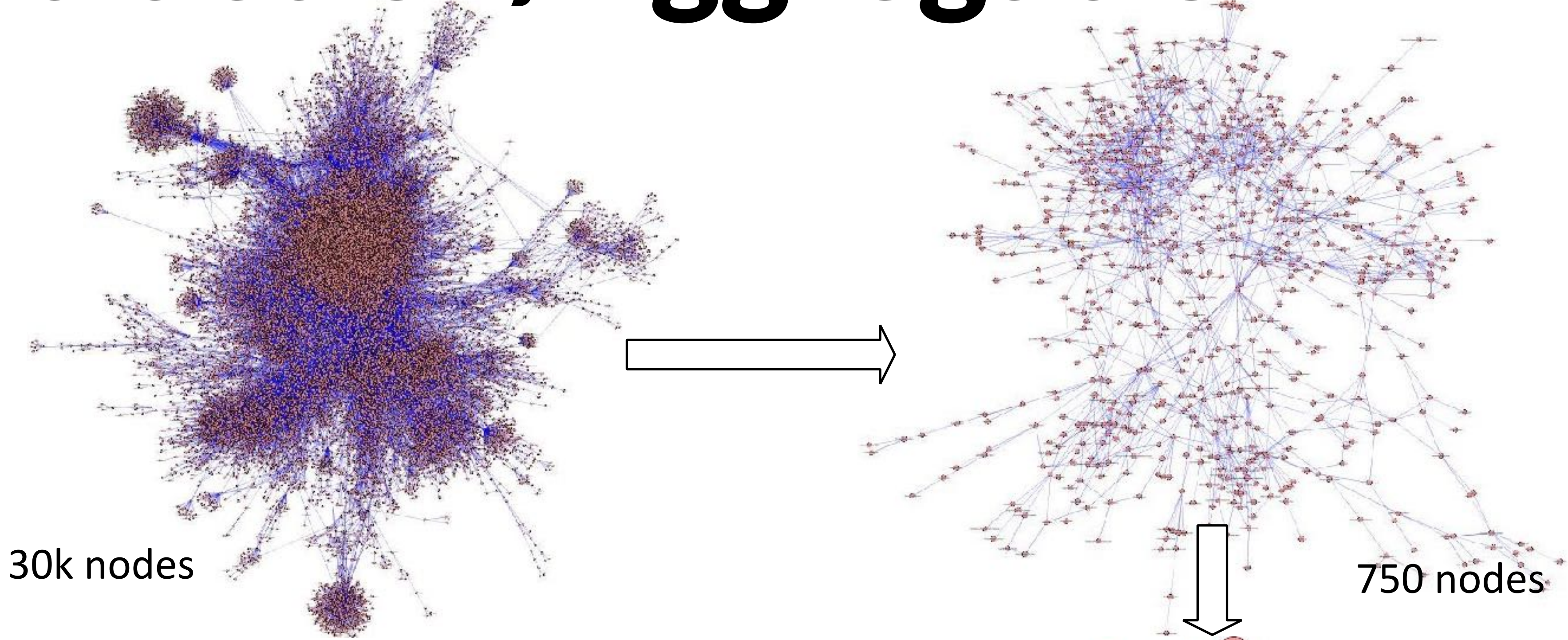
BUT: naïve runtime complexity is still  $O(n^2)$ !

in each optimization step, all vertices have to be checked against all other vertices

# Address Computational Scalability: Multilevel Approaches



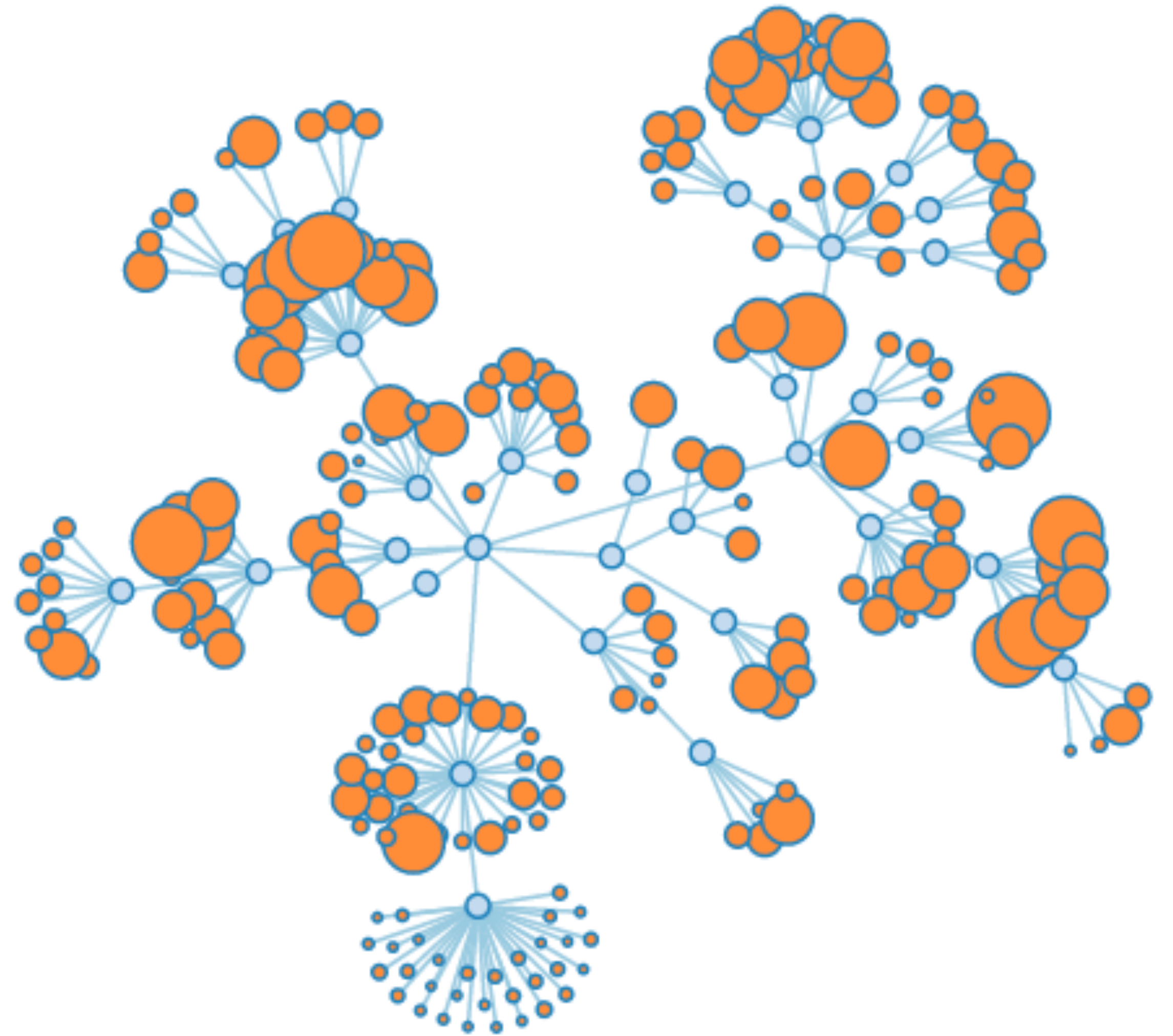
# Abstraction/Aggregation



# Collapsible Force Layout

Supernodes: aggregate of nodes

manual or algorithmic  
clustering

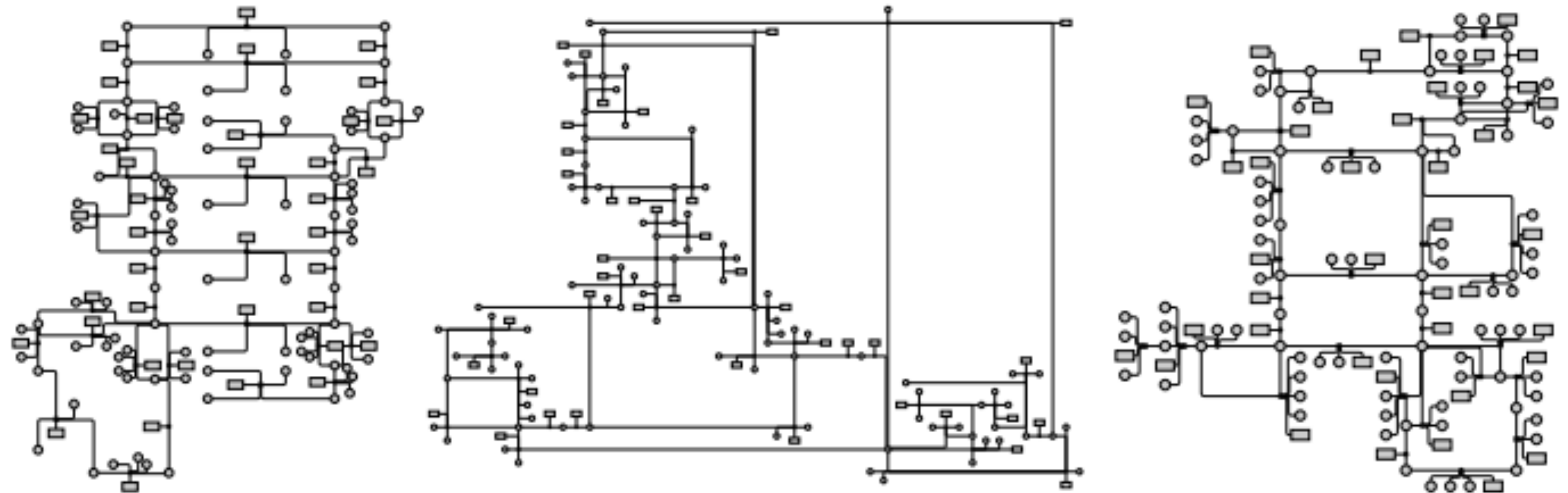


# HOLA: Human-like Orthogonal Layout

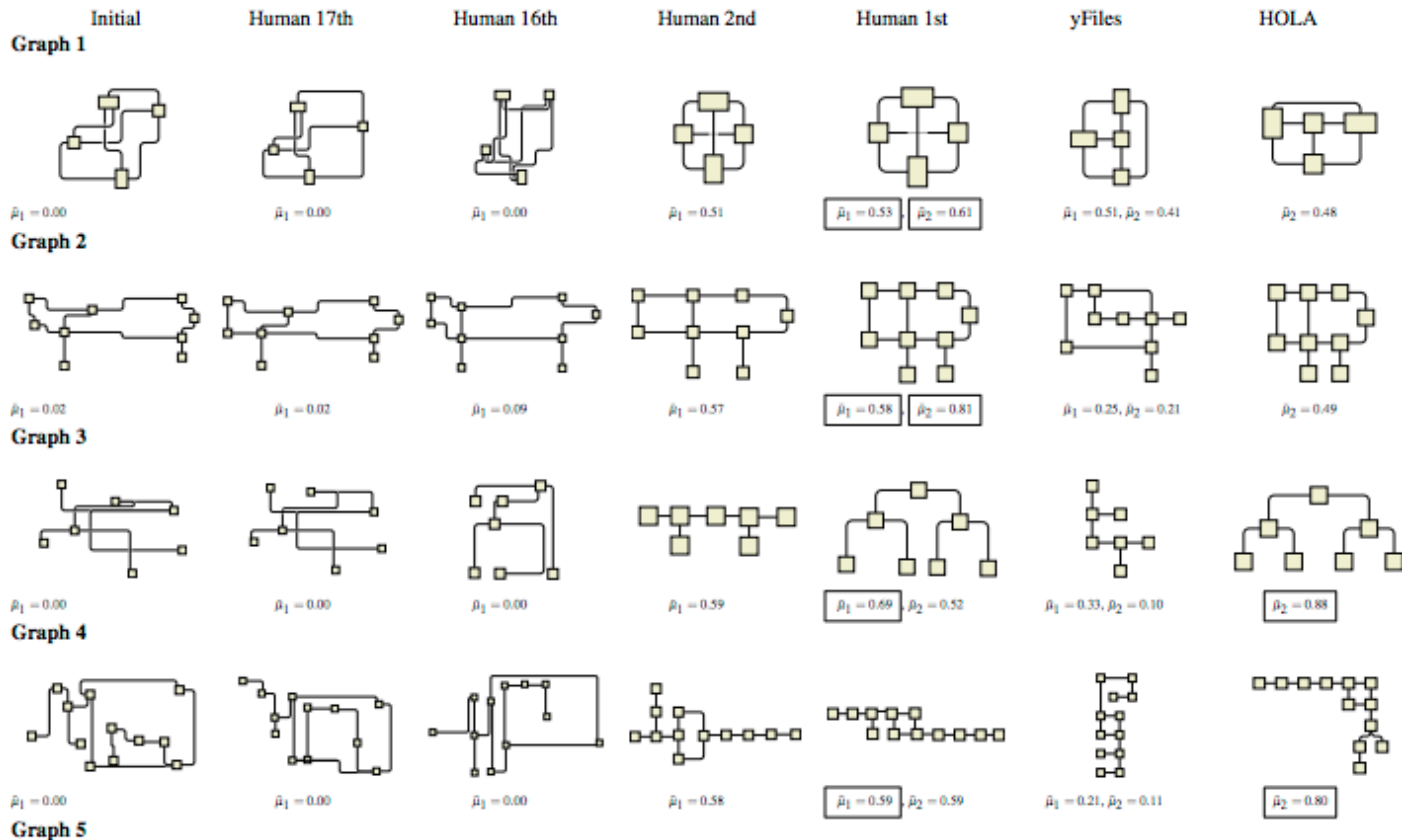
Study how humans lay-out a graph

Try to emulate layout

Left: human, middle: conventional algo, right new algo



[Kieffer et al, InfoVis 2015]

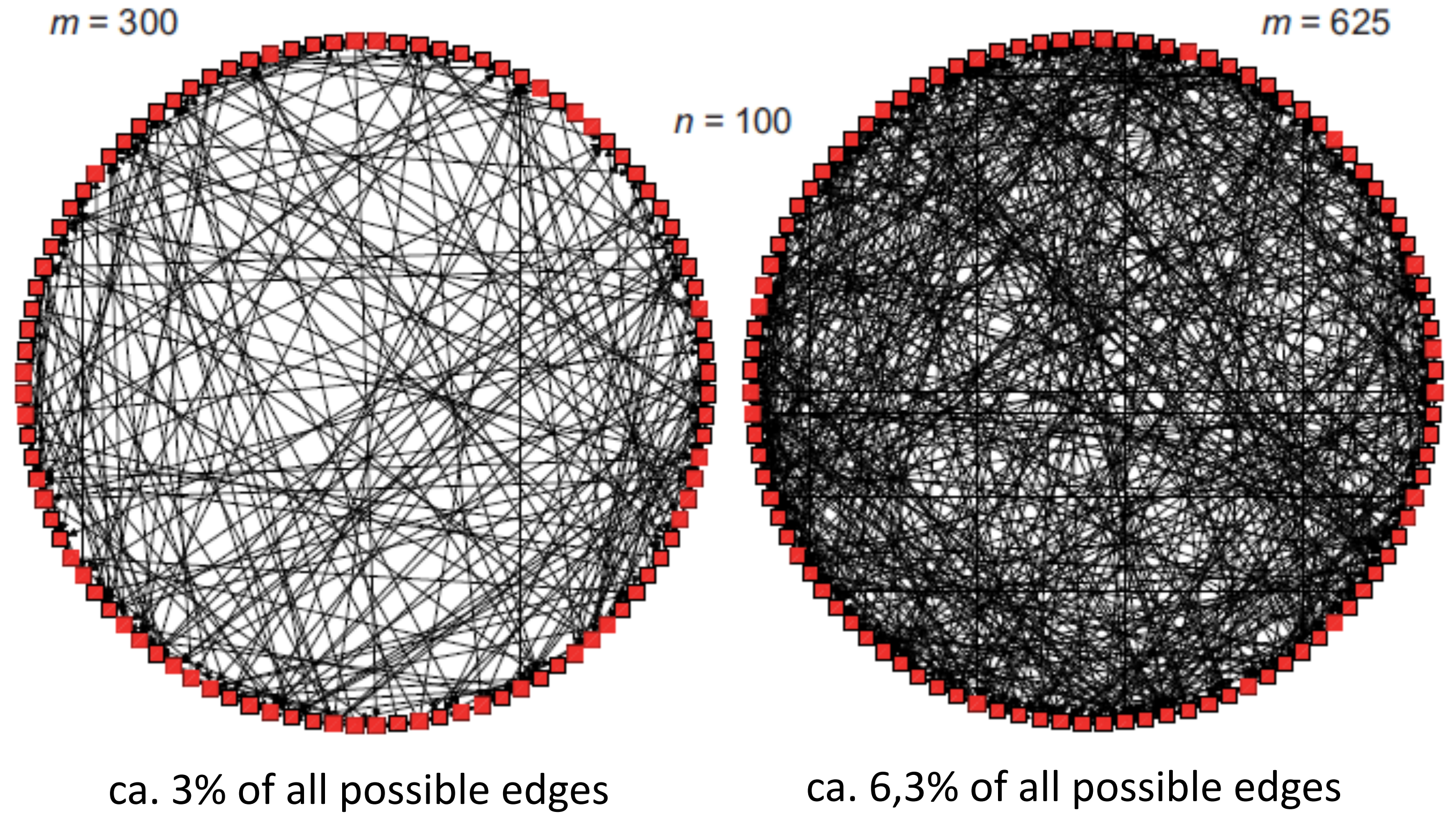


# Styled / Restricted Layouts

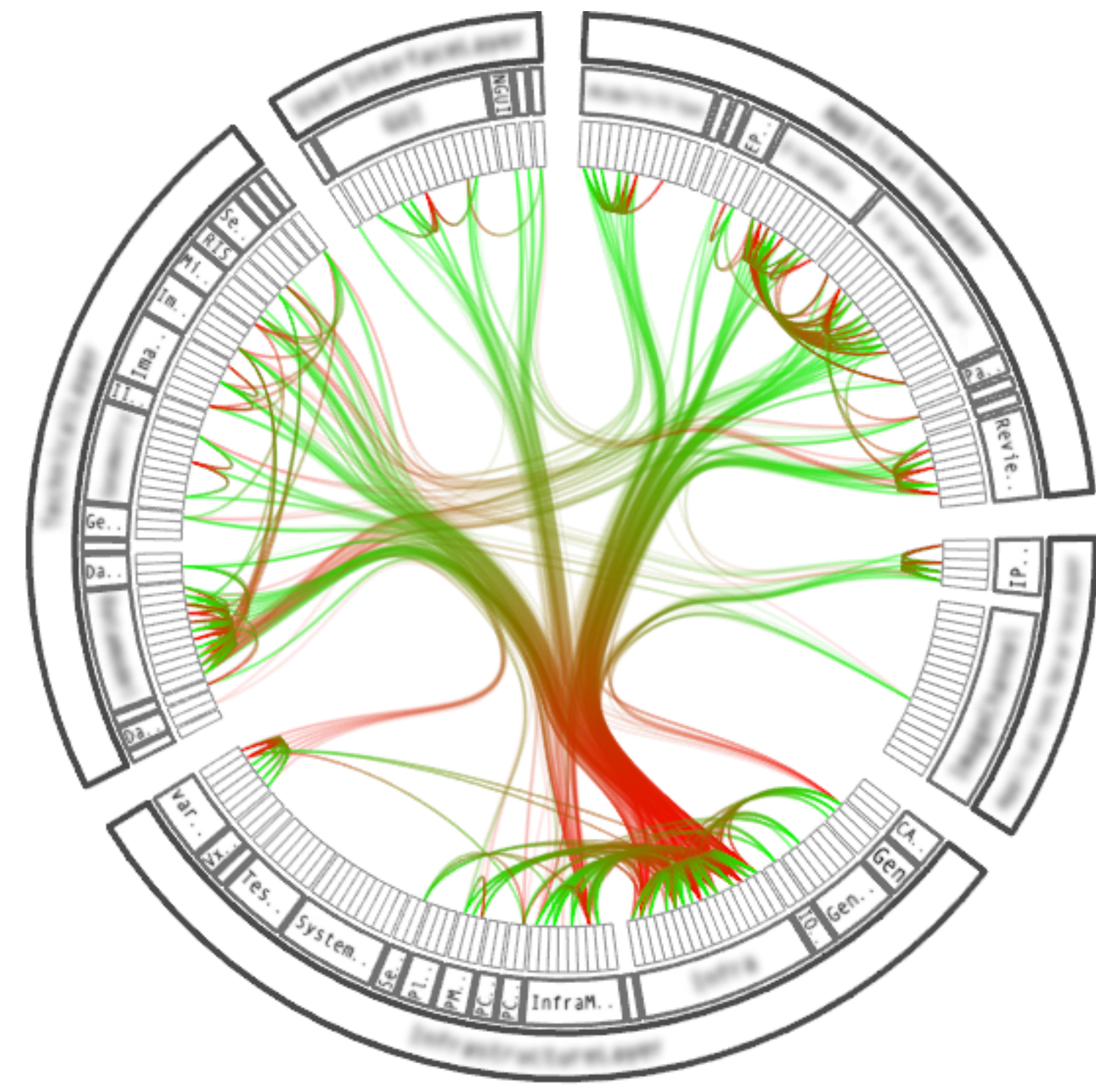
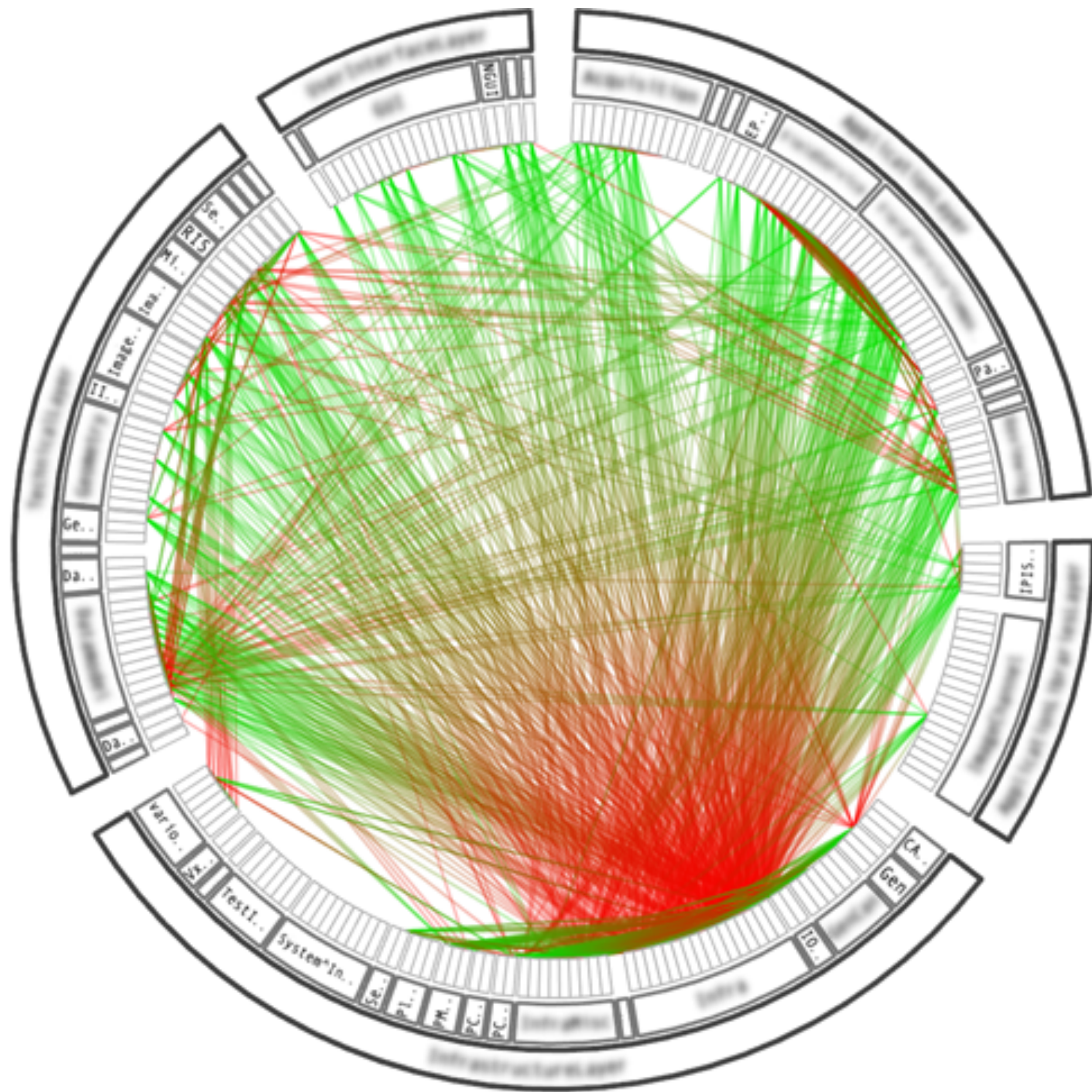
Circular Layout

Node ordering

Edge Clutter

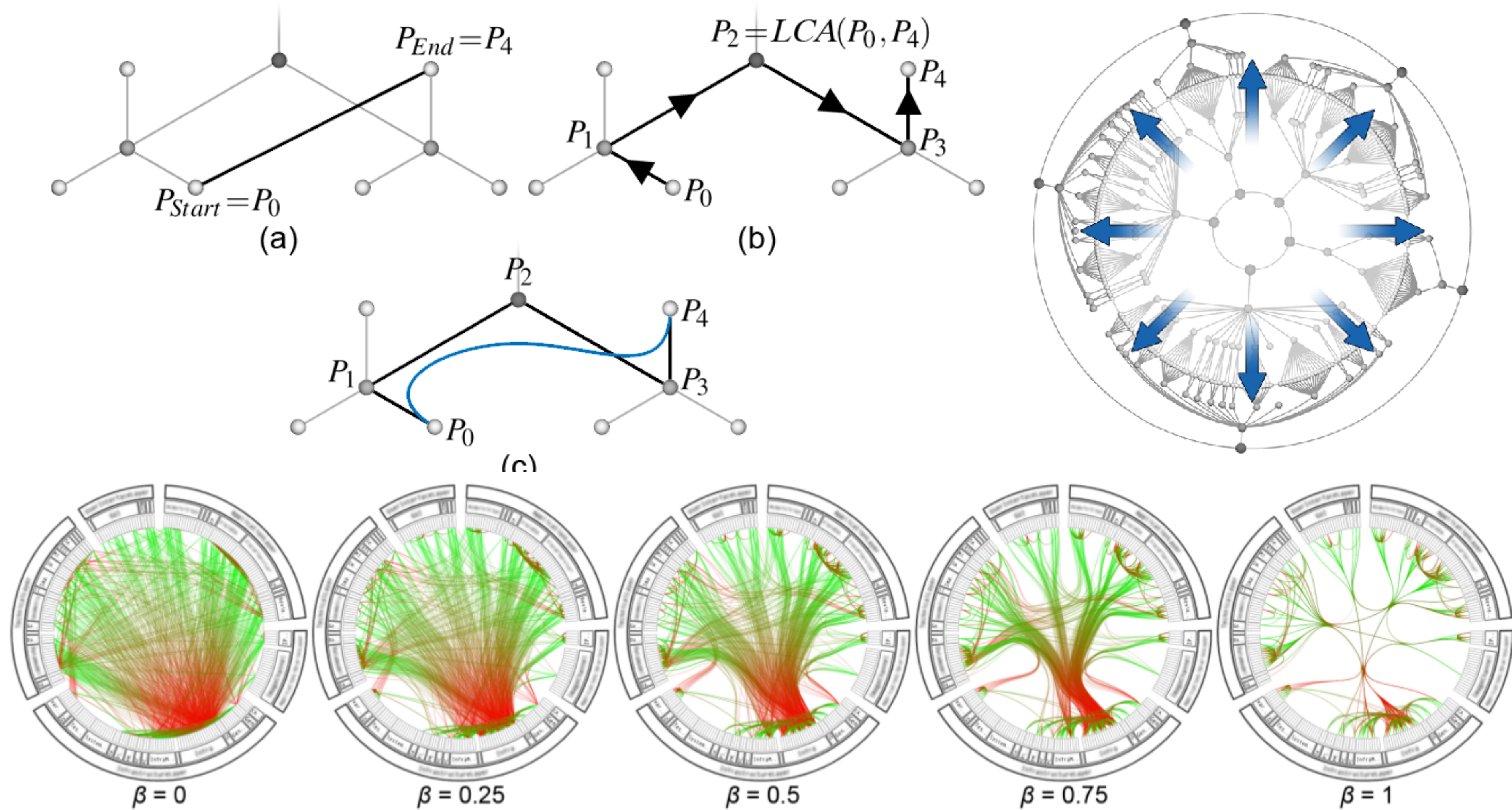


# Reduce Clutter: Edge Bundling



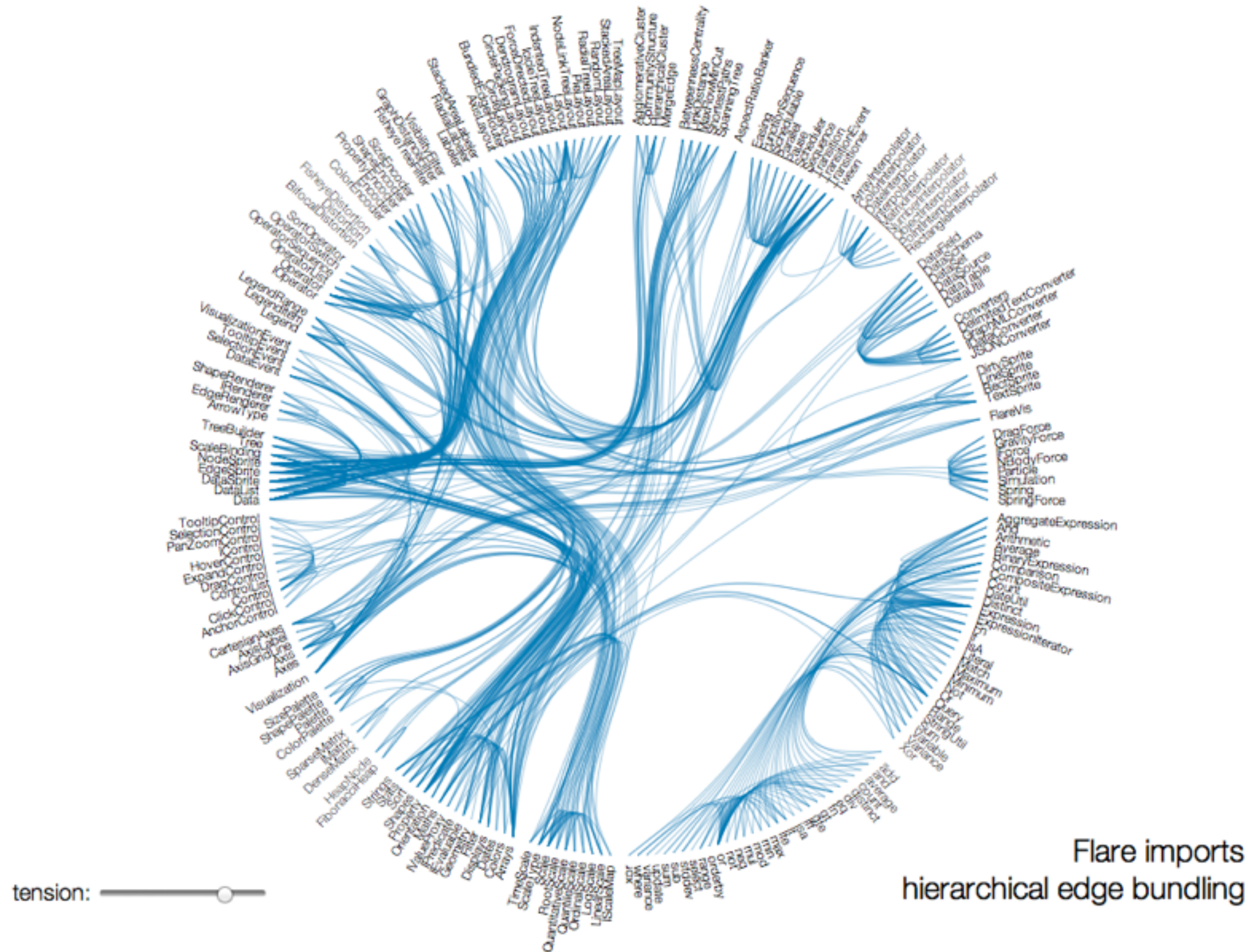


# Hierarchical Edge Bundling



Bundling Strength

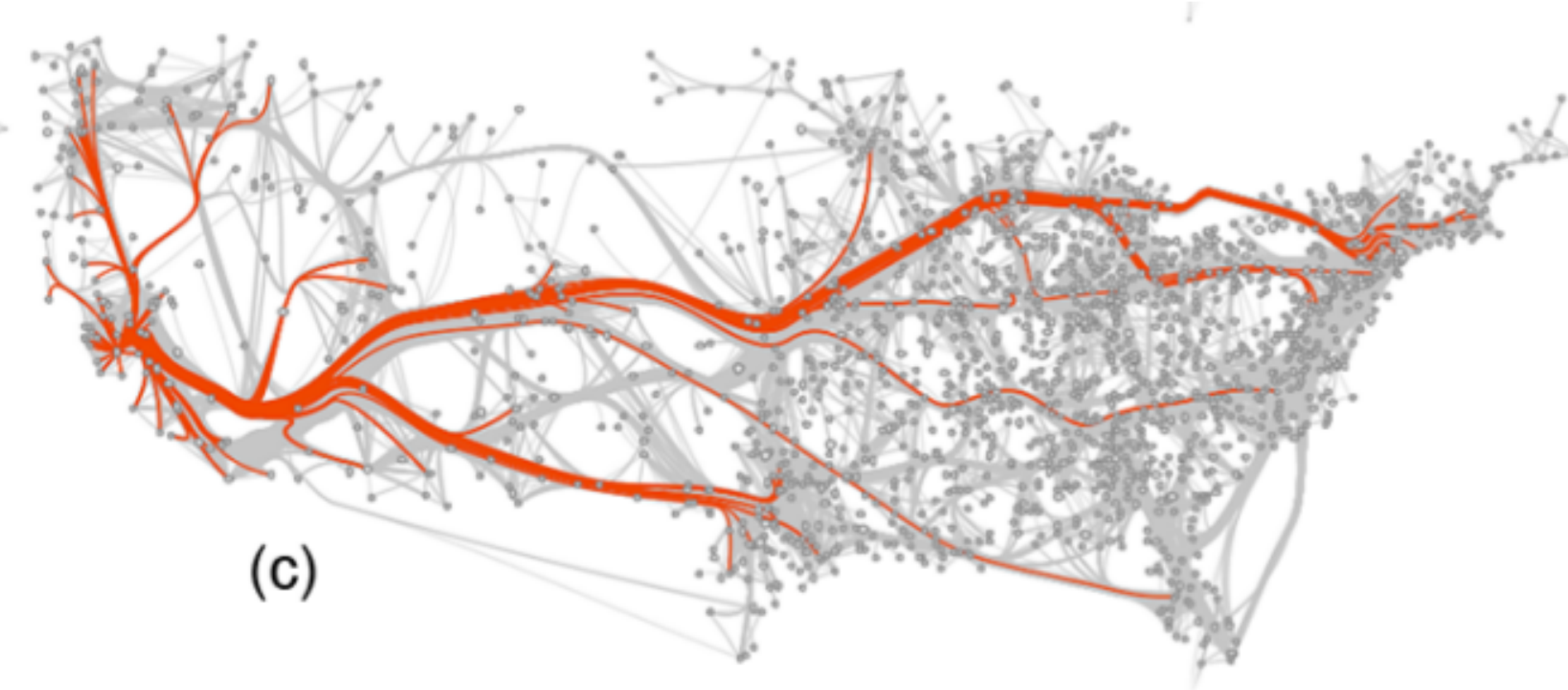
# Bundling Strength



# Fixed Layouts

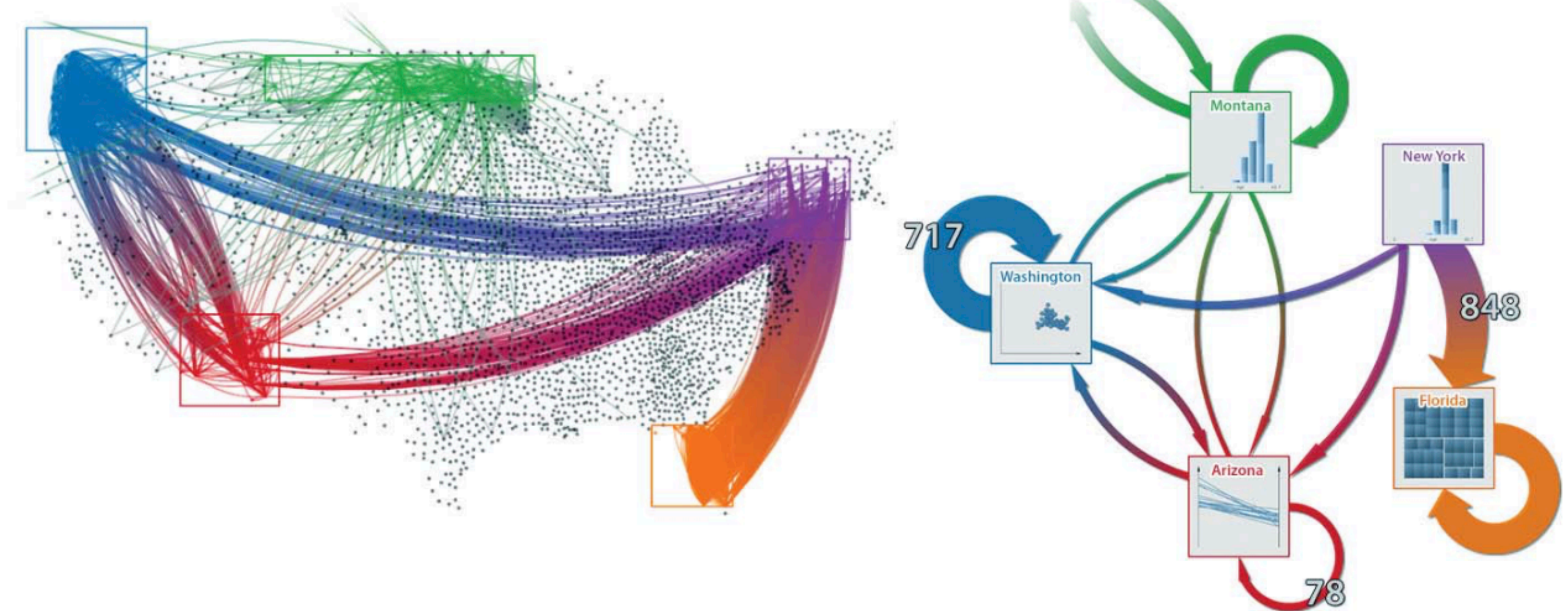
Can't vary position of nodes

Edge routing important





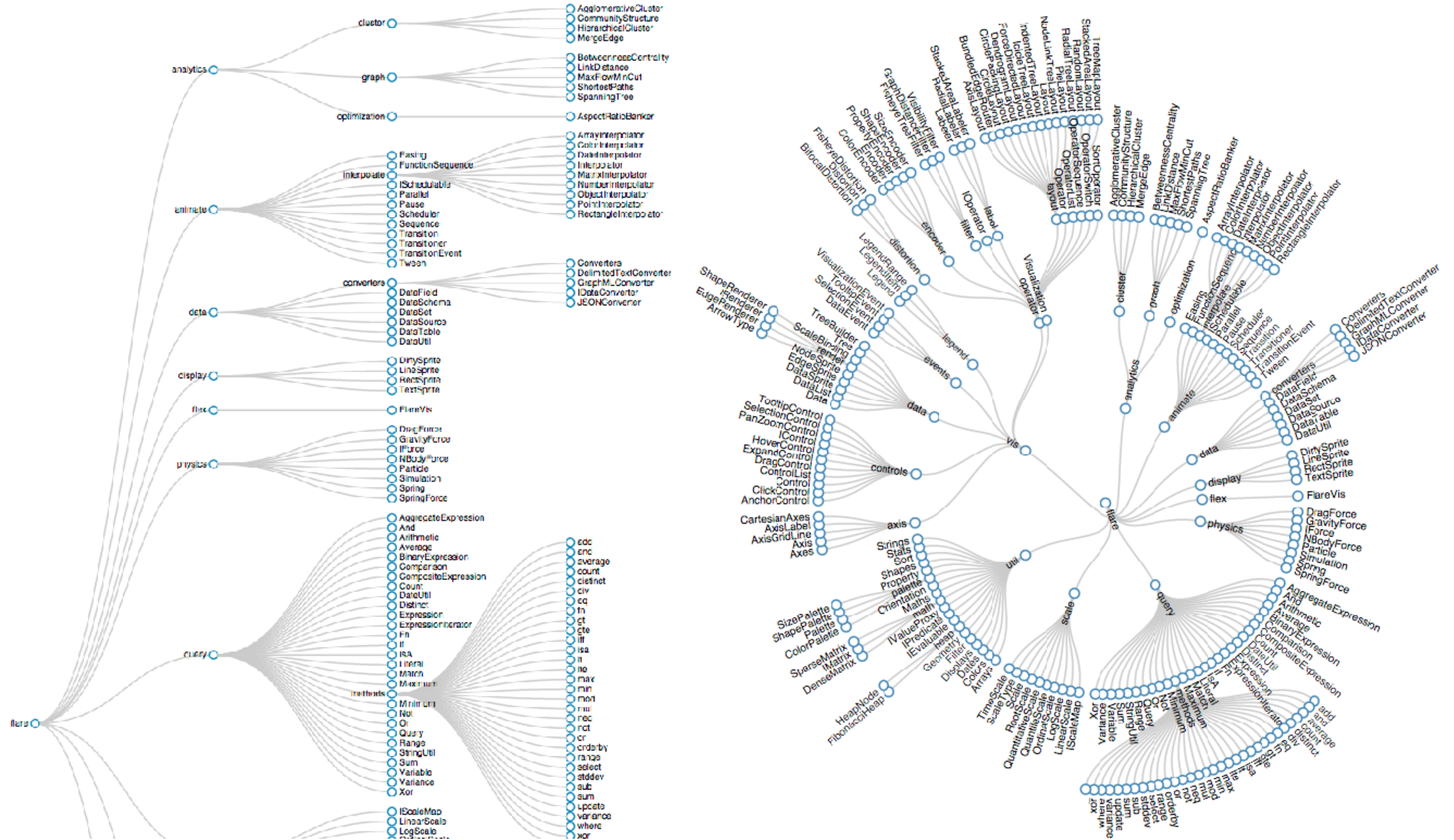
# Aggregation



# Explicit Tree Visualization

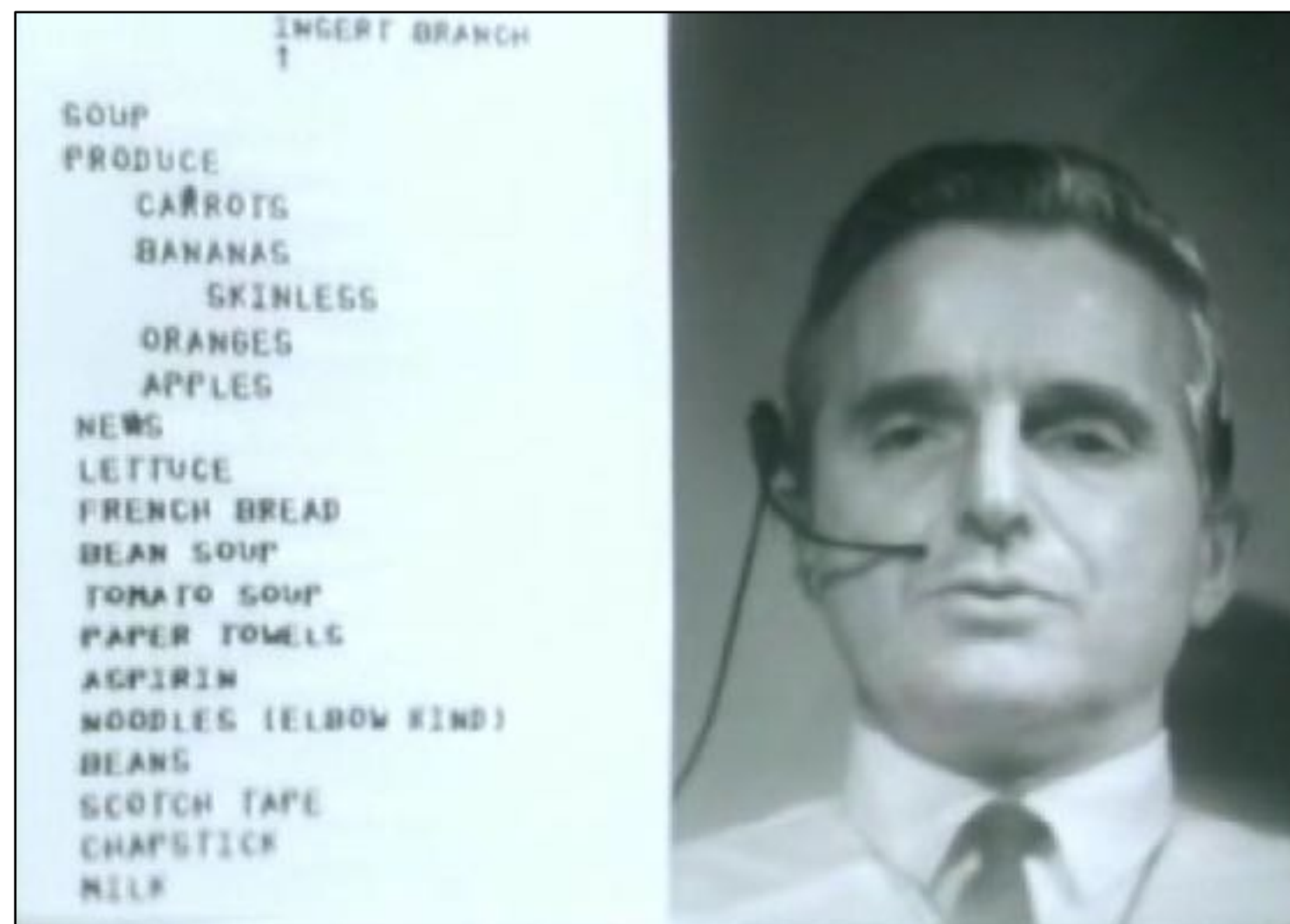
Reingold-Tilford layout

<http://billmill.org/pymag-trees/>

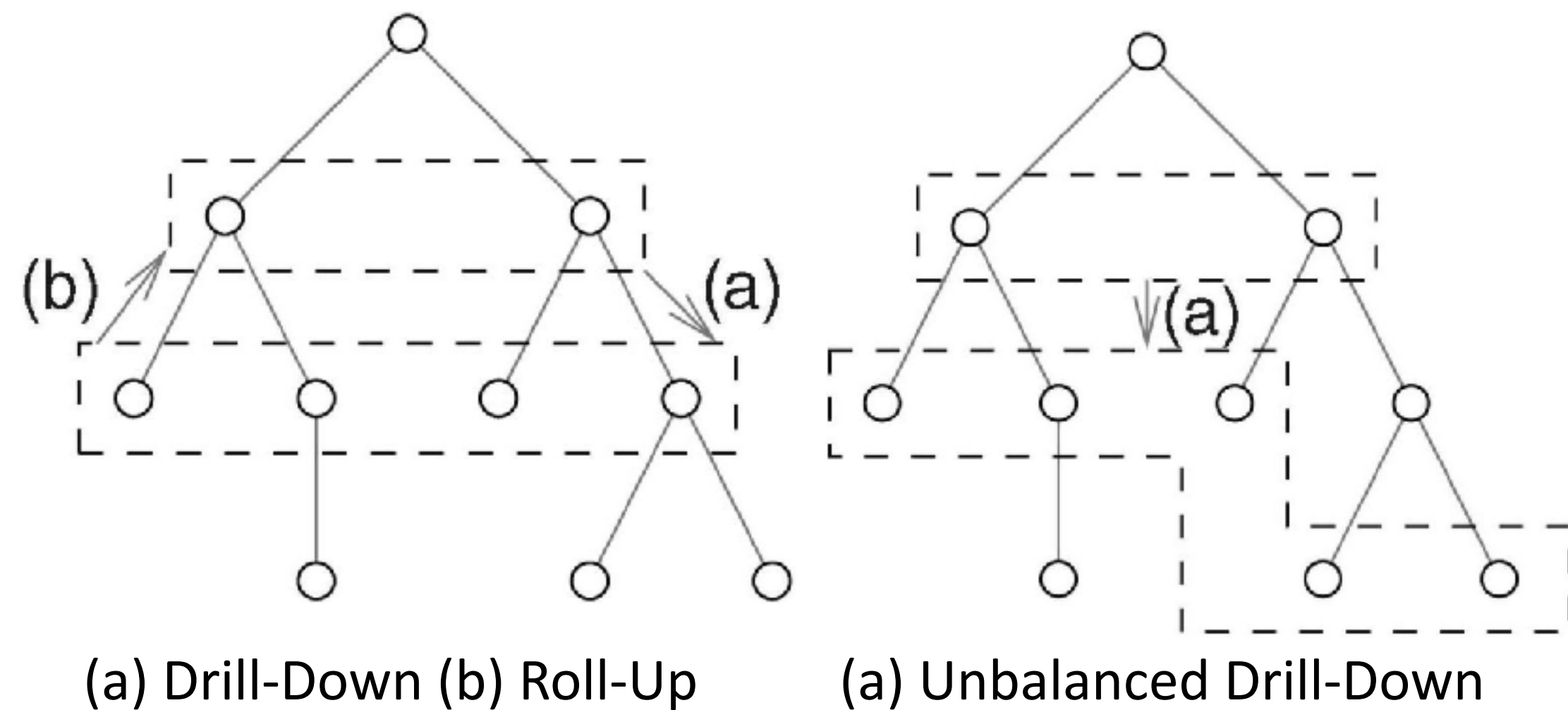


# Manipulating Aggregation Levels

First interactive tree manipulation



Douglas Engelbart 1968 - <http://www.1968demo.org>



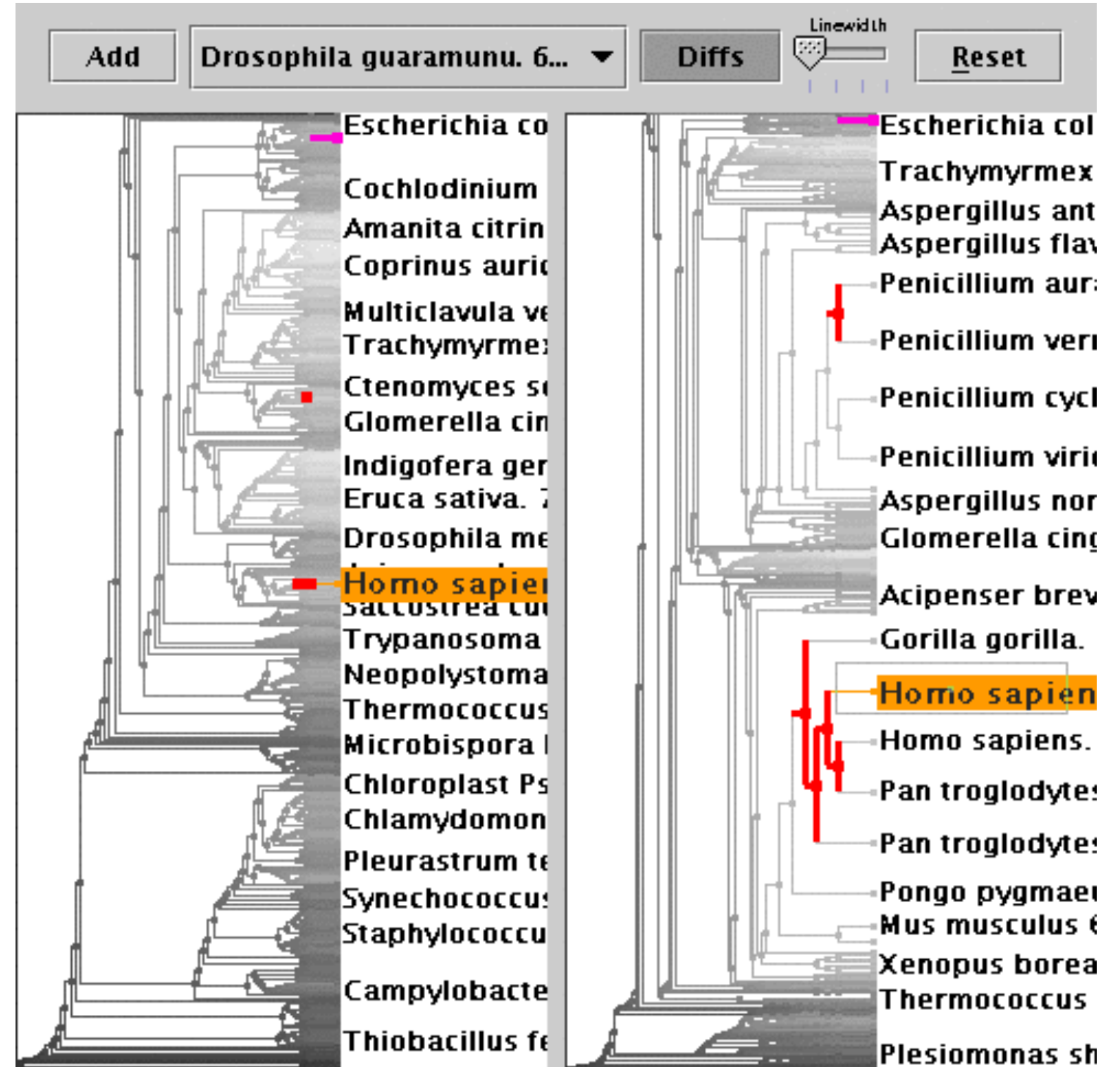
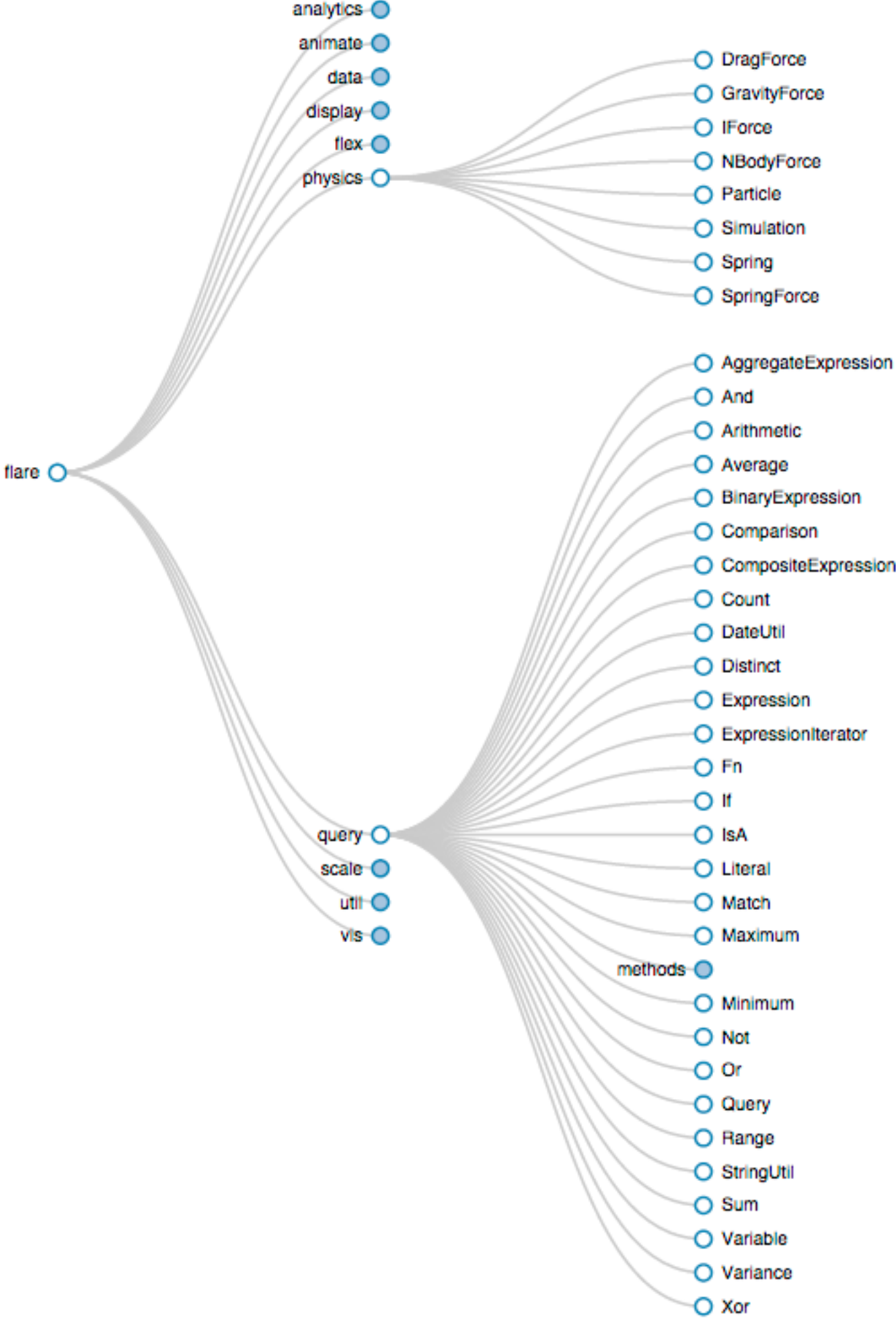
(a) Drill-Down (b) Roll-Up

(a) Unbalanced Drill-Down

“The mother of all demos“

<https://www.youtube.com/watch?v=yJDv-zdhzMY>

# Tree Interaction, Tree Comparison





# Explicit Representations

## Pros:

is able to depict all graph classes

can be customized by weighing the layout constraints

very well suited for TBTs, if also a suitable layout is chosen

## Cons:

computation of an optimal graph layout is in NP

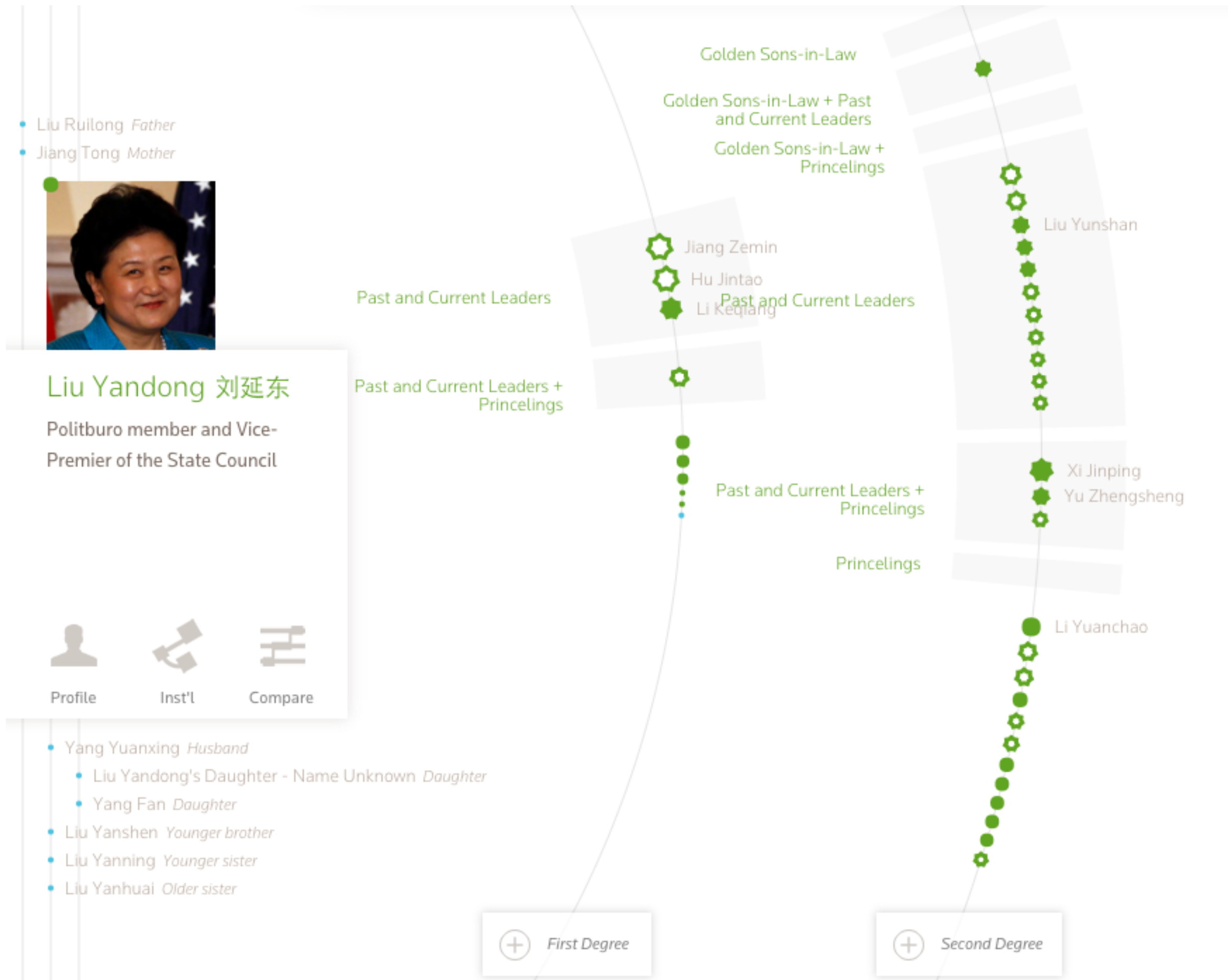
(even just achieving minimal edge crossings is already in NP)

even heuristics are still slow/complex (e.g., naïve spring embedder is in  $O(n^2)$ )

has a tendency to clutter (edge clutter, “hairball”)

# Design Critique

# Connected China



<https://goo.gl/YXkWYX>

<http://china.fathom.info/>

# Multivariate Graphs

# Networks and Attributes

Attributes can influence topology

Path can be slow / blocked

best route when driving depends on traffic

biological network depends on many factors

# Challenge: Data Scale & Heterogeneity

Large **number of values**

Large datasets have more than 500 experiments

Multiple **groups/conditions**

Different **types** of data

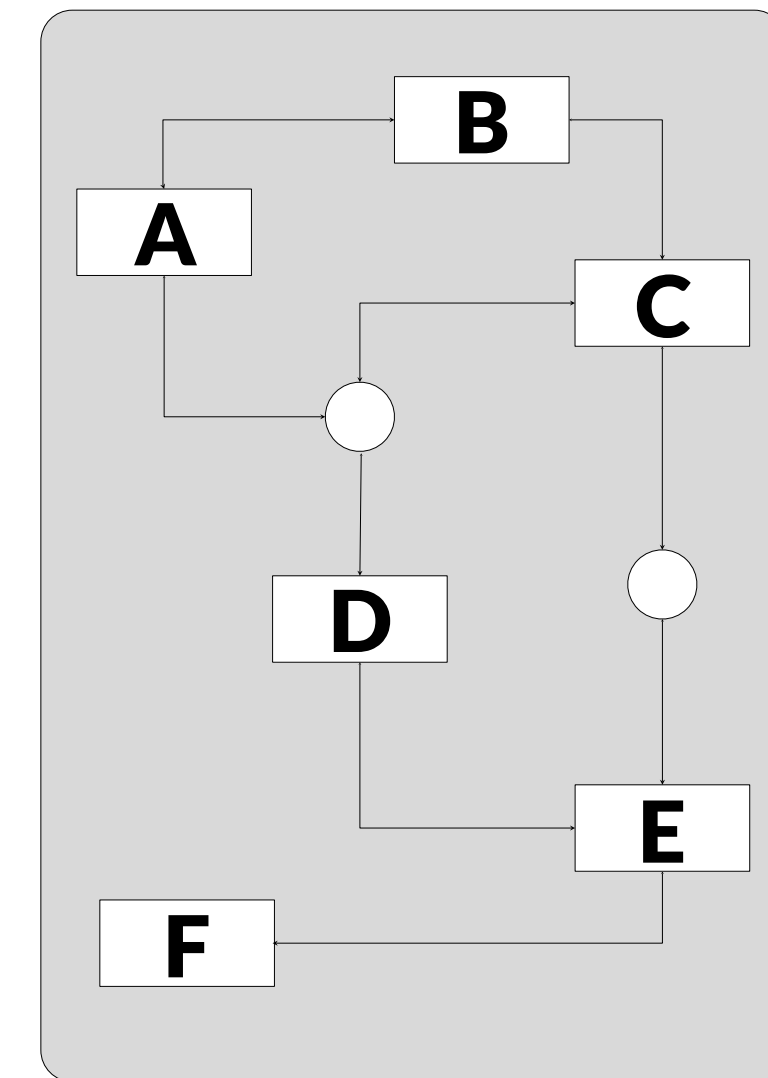
# Challenge: Supporting Multiple Tasks

Two central tasks:

Explore **topology** of network

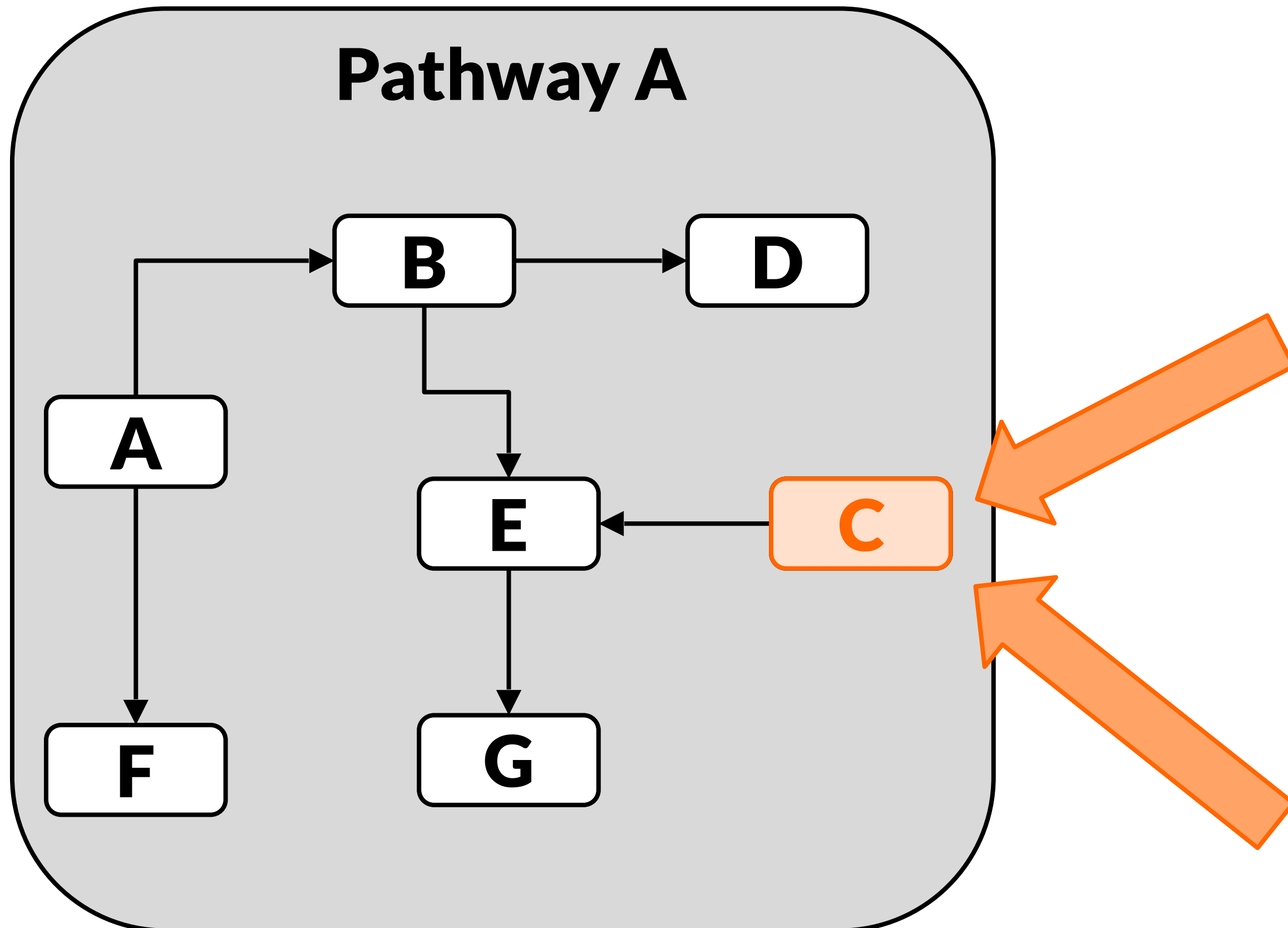
Explore the **attributes** of the nodes  
(experimental data)

Need to support both!



	Sample 1	Sample 2	Sample 3
Gene 1	1	1.1	0.4
Gene 2	2	0.5	1.2
Gene 3	1.4	0.2	0.5
Gene 4	0.3	0.5	0.7

# Many Node Attributes



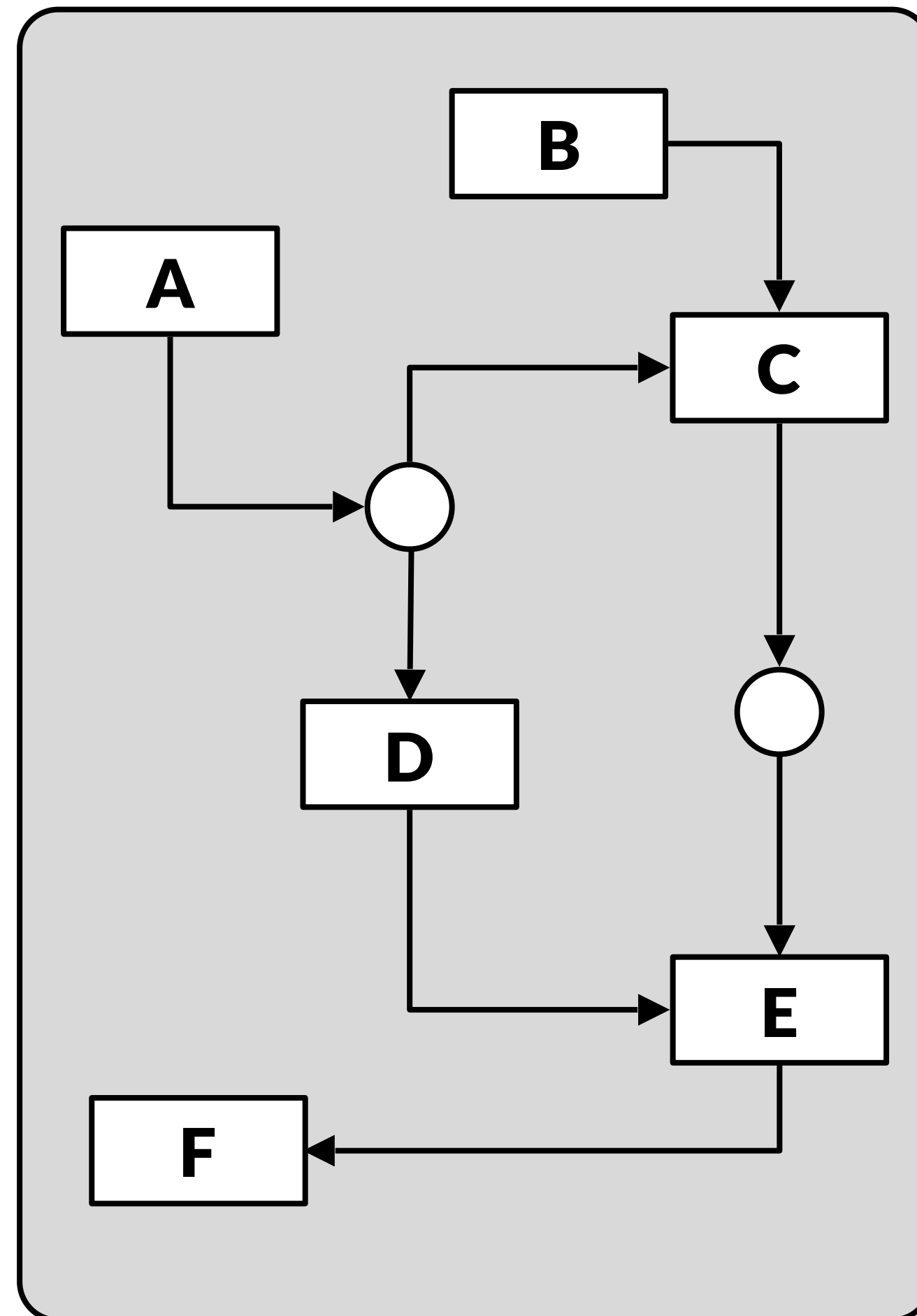
Node	Sample 1	Sample 2	Sample 3	...
A	0.55	0.95	0.83	...
B	0.12	0.42	0.16	...
C	0.33	0.65	0.38	...
...	...	...	...	...

Node	Sample 1	Sample 2	Sample 3	...
A	low	low	very high	...
B	normal	low	high	...
C	high	very low	normal	...
...	...	...	...	...

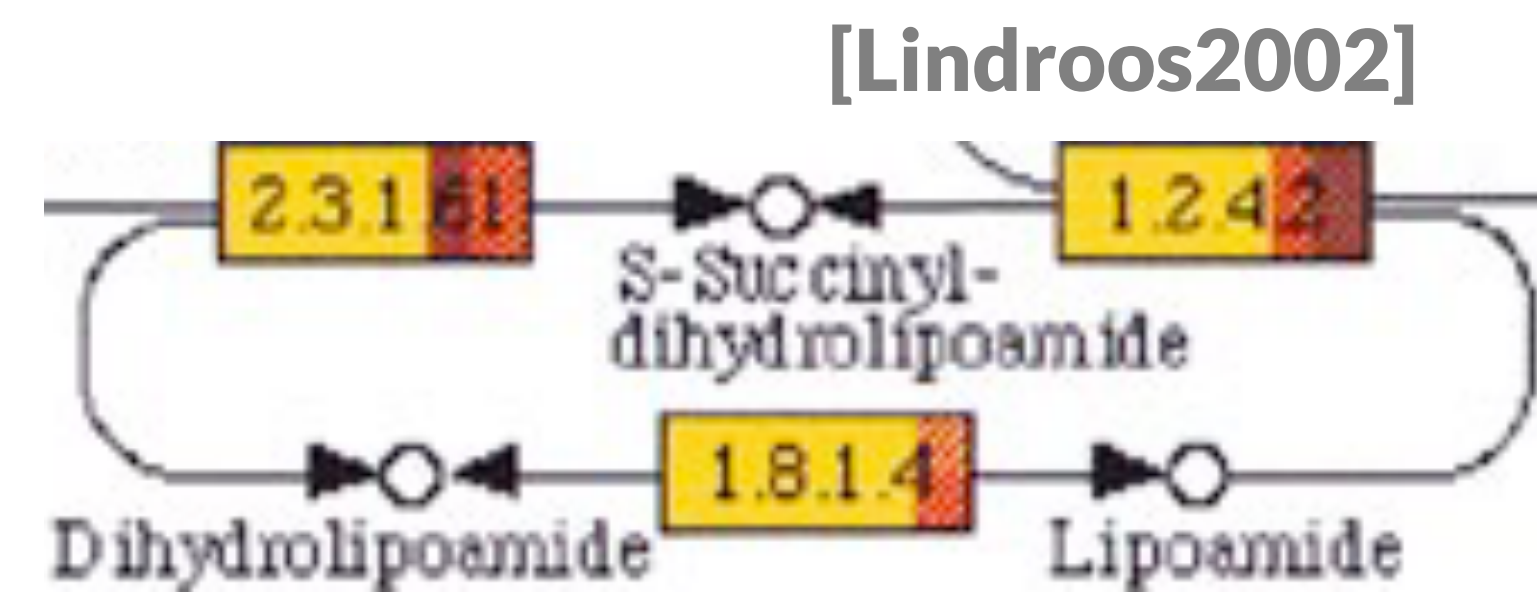
**How to visualize attribute data on networks?**



# Good Old Color Coding



<b>A</b>	<b>-3.4</b>	<b>4.2</b>	<b>5.1</b>	<b>4.2</b>
<b>B</b>	<b>2.8</b>	<b>1.8</b>	<b>1.3</b>	<b>1.1</b>
<b>C</b>	<b>3.1</b>	<b>-2.2</b>	<b>2.4</b>	<b>2.2</b>
<b>D</b>	<b>-3</b>	<b>-2.8</b>	<b>1.6</b>	<b>1.0</b>
<b>E</b>	<b>0.5</b>	<b>0.3</b>	<b>-1.1</b>	<b>1.3</b>
<b>F</b>	<b>0.3</b>	<b>0.3</b>	<b>1.8</b>	<b>-0.3</b>

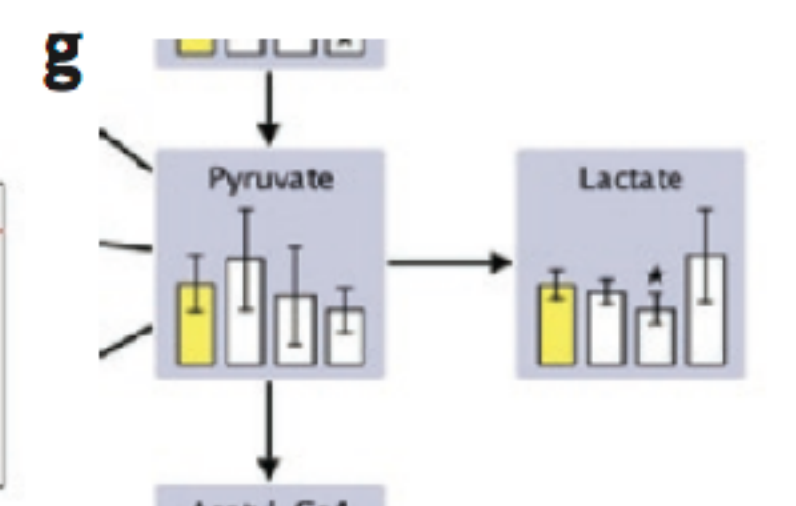
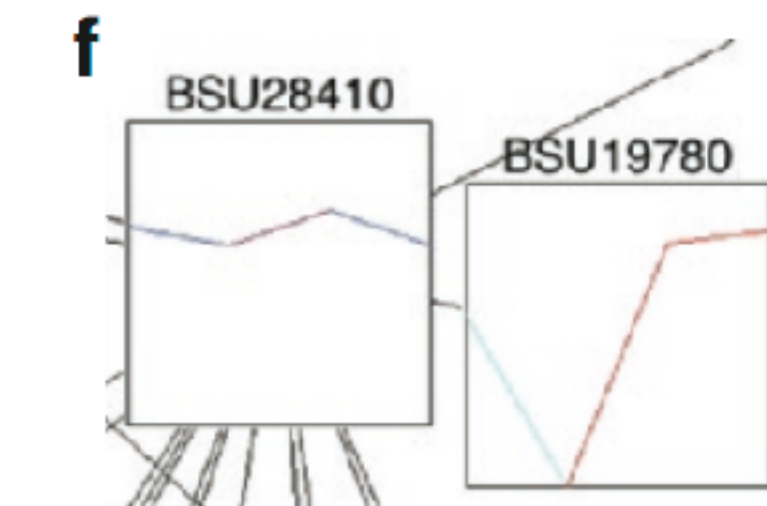
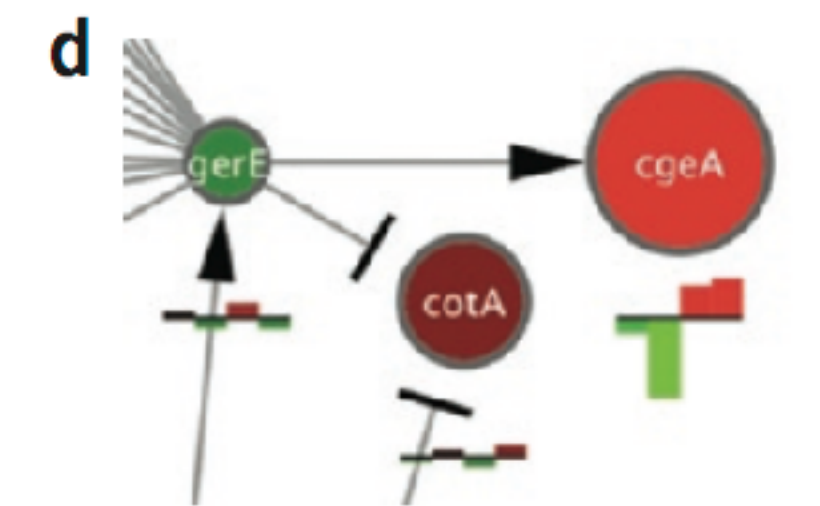
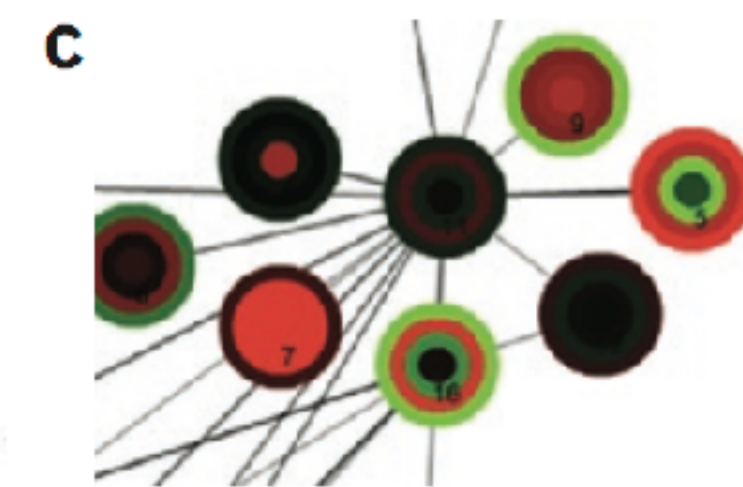
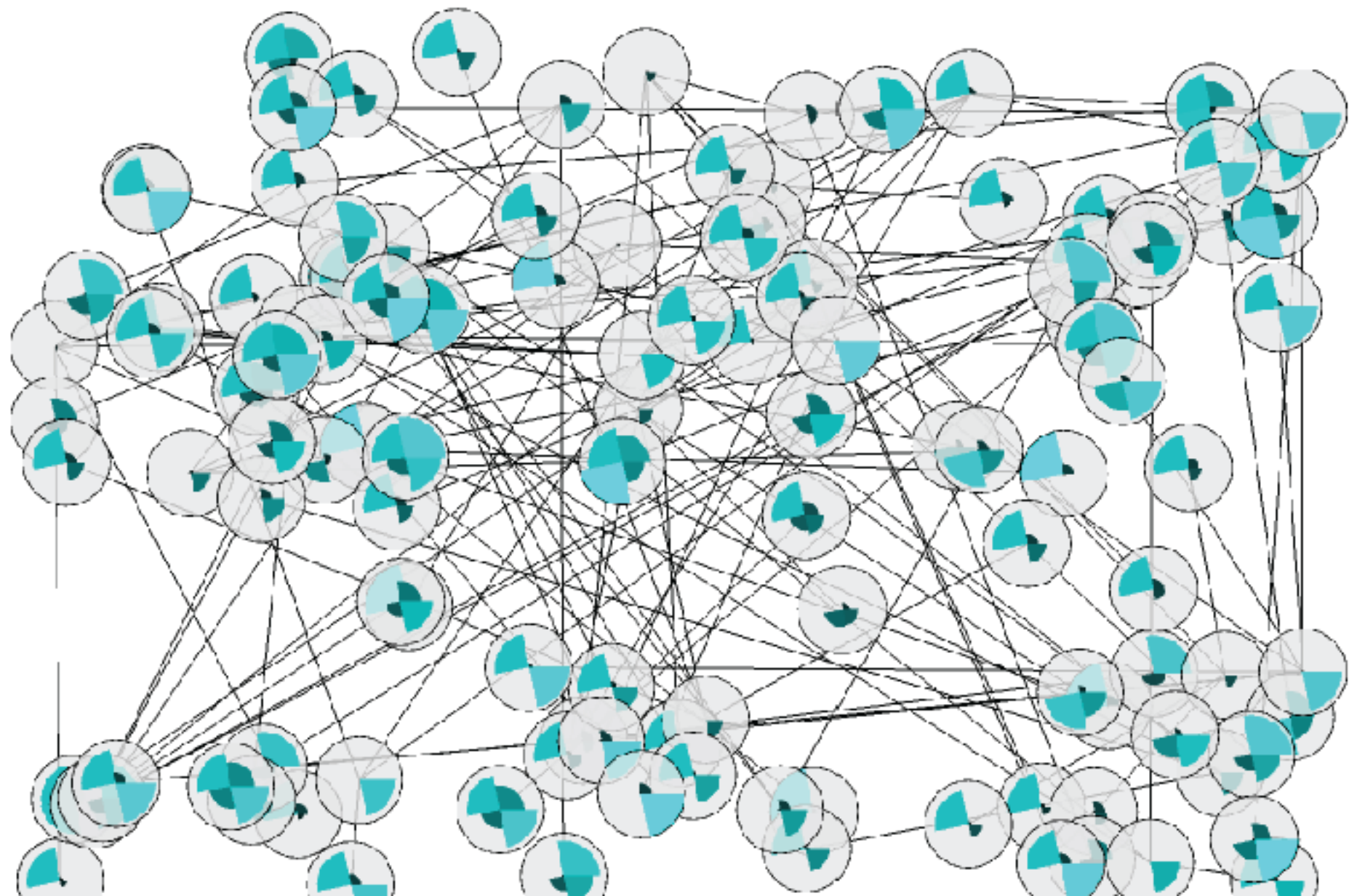


# Node Attributes

Coloring

Glyphs

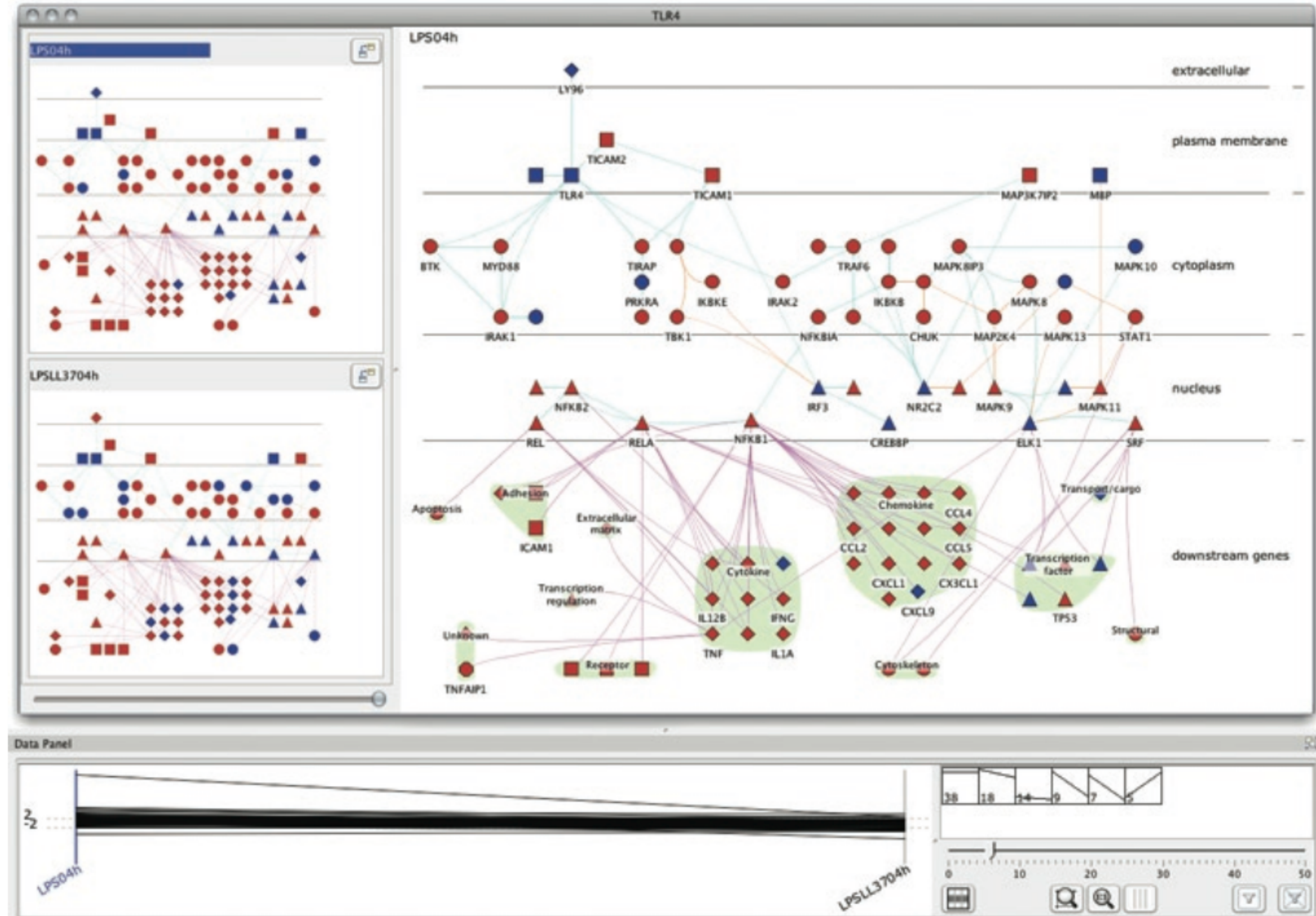
-> Limited in scalability



# Small Multiples

Cerebral [Barsky, 2008]

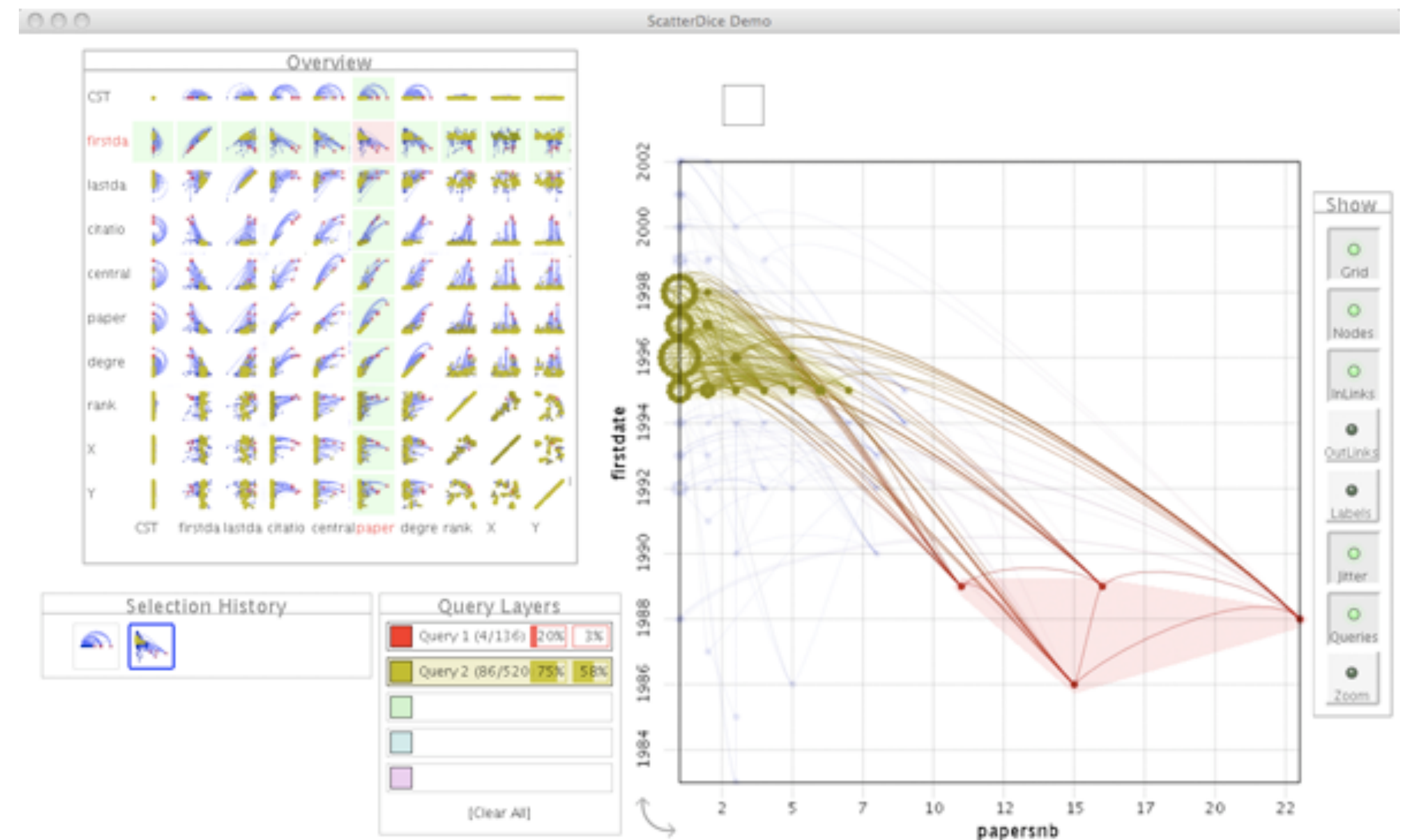
Each dimension in its own window



# Data-driven node positioning

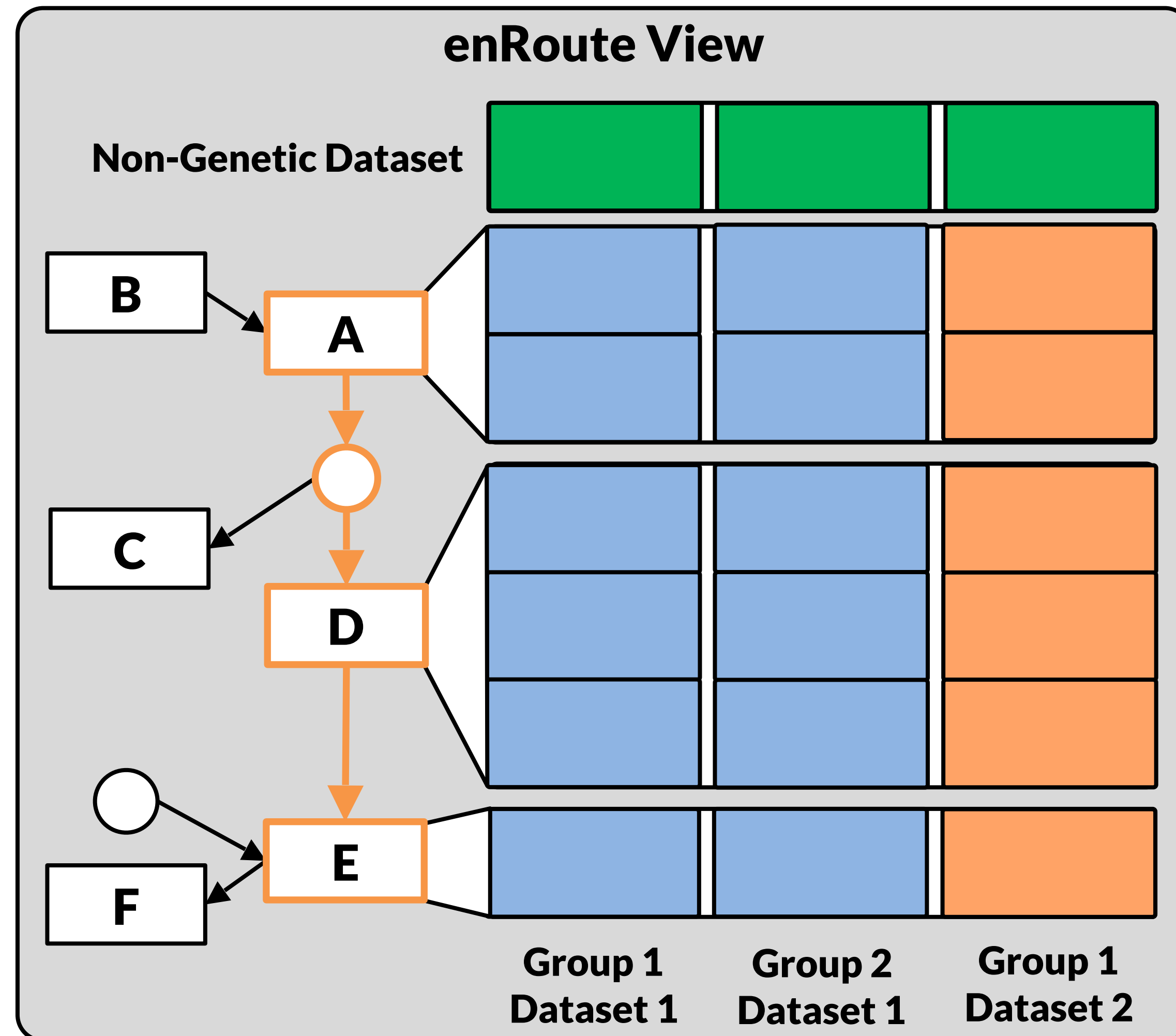
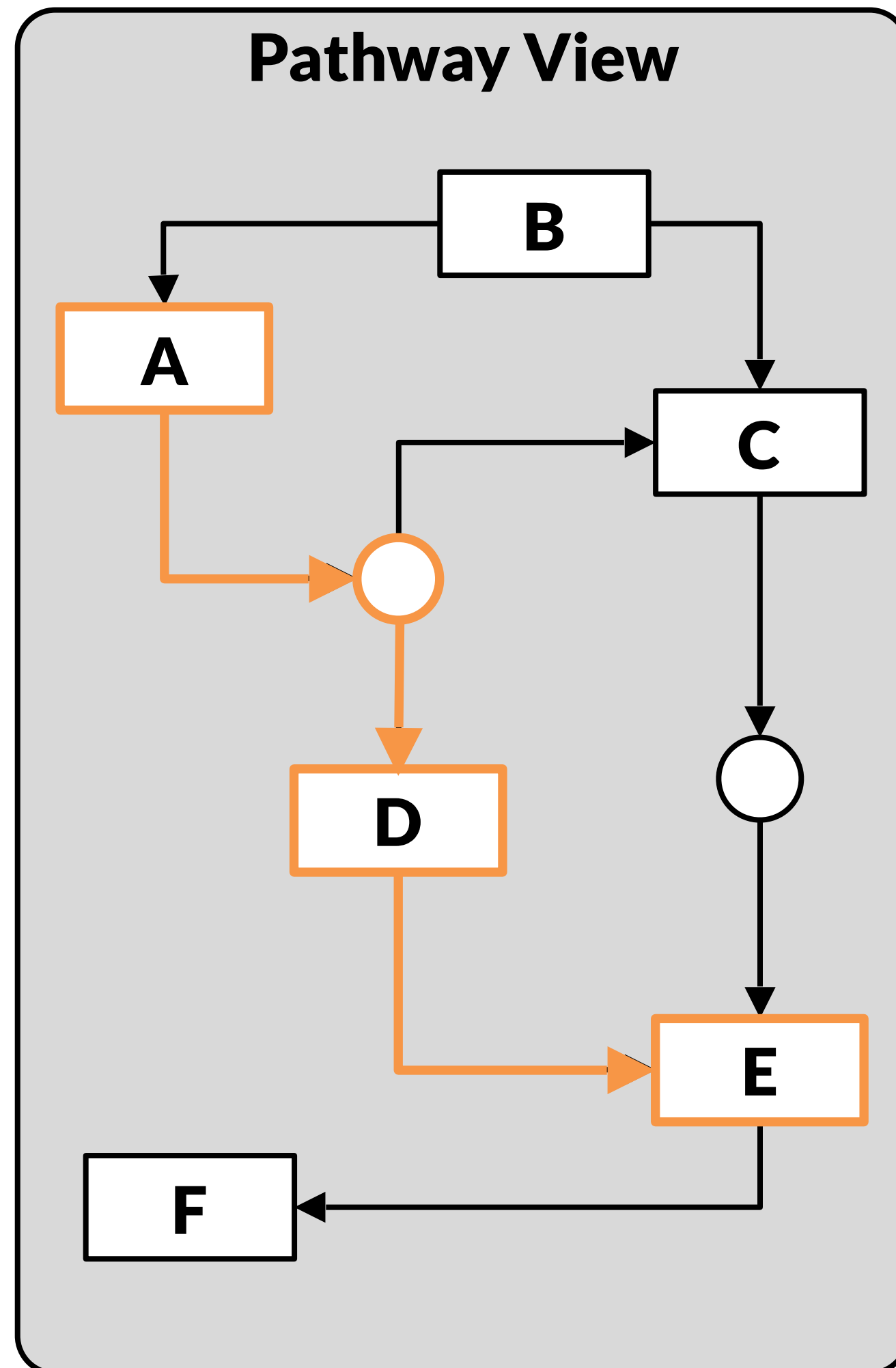
## GraphDice

Nodes are laid out according to attribute values



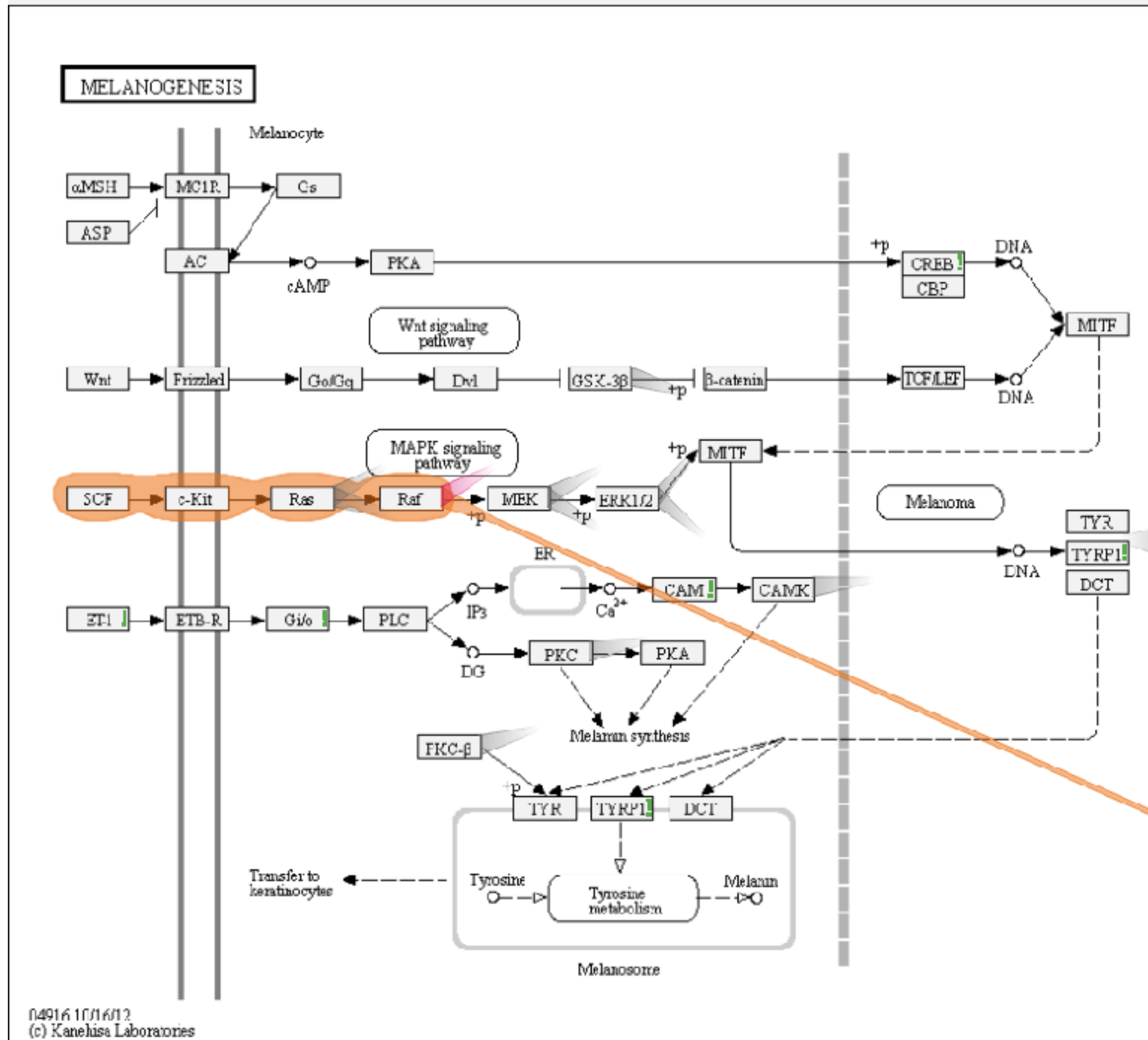
[Bezerianos et al, 2010]

# Path Extraction: enRoute

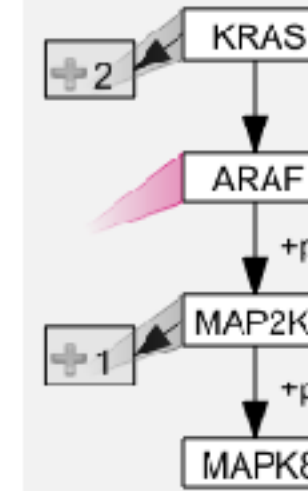


# enRoute

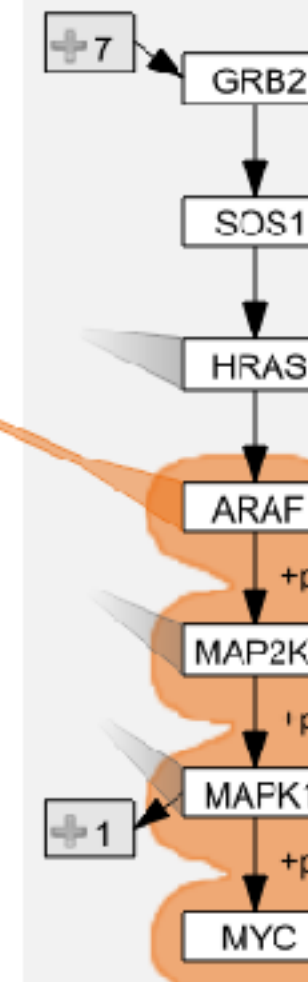
Melanogenesis



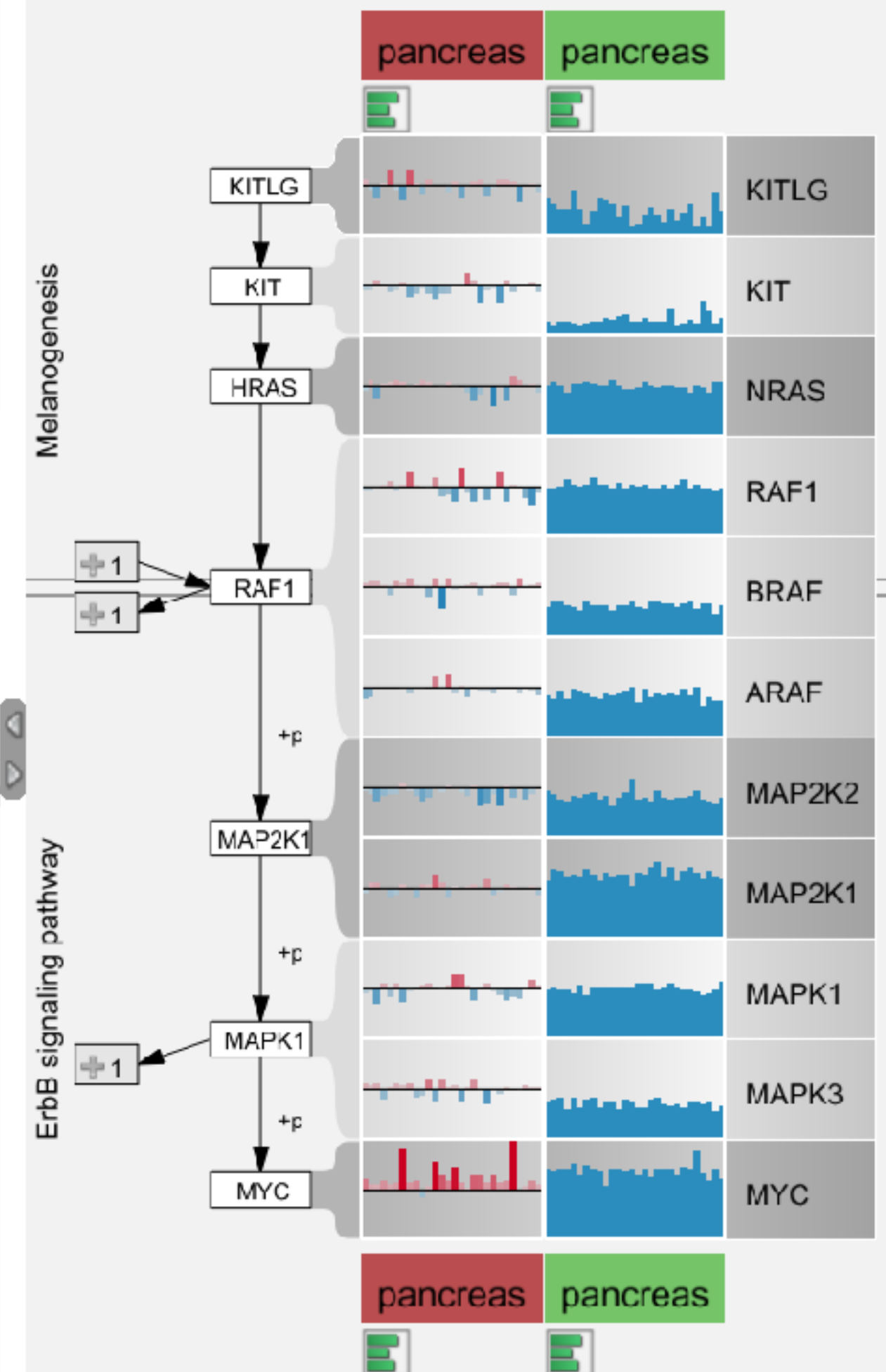
Pancreatic cancer



ErbB signaling pathway



Selected Path



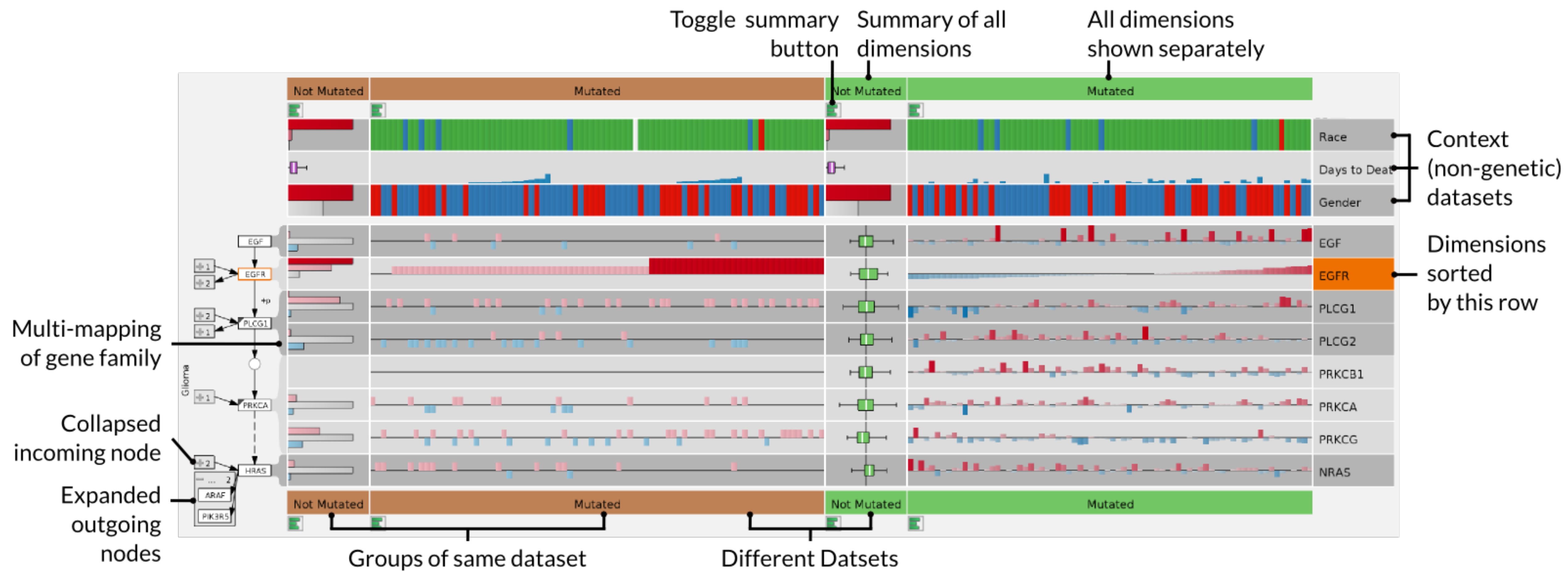
Pathways

- Pathway
- Filter:  
<None>
- 1 C donor
  - 2-Oxocarboxylic acid
  - ABC transporters
  - ABC-family proteins
  - ACE Inhibitor Pathwa
  - Acetylcholine Synthes
  - Acute myeloid leukem
  - Adherens junction
  - Adipocyte TarBase
  - Adipocytokine signali
  - Adipogenesis
  - Advanced glycosylatio
  - Aflatoxin B1 metaboli
  - African trypanosomias
  - AGE/RAGE pathway
  - AhR pathway
  - Alanine and aspartate
  - Alanine, aspartate an
  - Alcoholism
  - Aldosterone-regulated
  - Allograft rejection
  - Allograft rejection
  - Alpha 6 Beta 4 signal
  - alpha-Linolenic acid
  - Alzheimer's disease
  - Alzheimers Disease
  - amino acid conjugatio
  - amino acid conjugatio
  - Amino sugar and nucl
  - Aminoacyl-tRNA bios
  - Amoebiasis
  - Amphetamine addicti
  - AMPK signaling
  - Amyotrophic lateral sc
  - Androgen receptor si
  - Angiogenesis
  - Angiogenesis
  - angiogenesis overvie
  - Antigen processing an
  - APC/C-mediated degra
  - Apoptosis
  - Apoptosis
  - Apoptosis Meta Path
  - Apoptosis Modulation
  - Apoptosis Modulation
  - Apoptosis, anoikis an

Selected Path

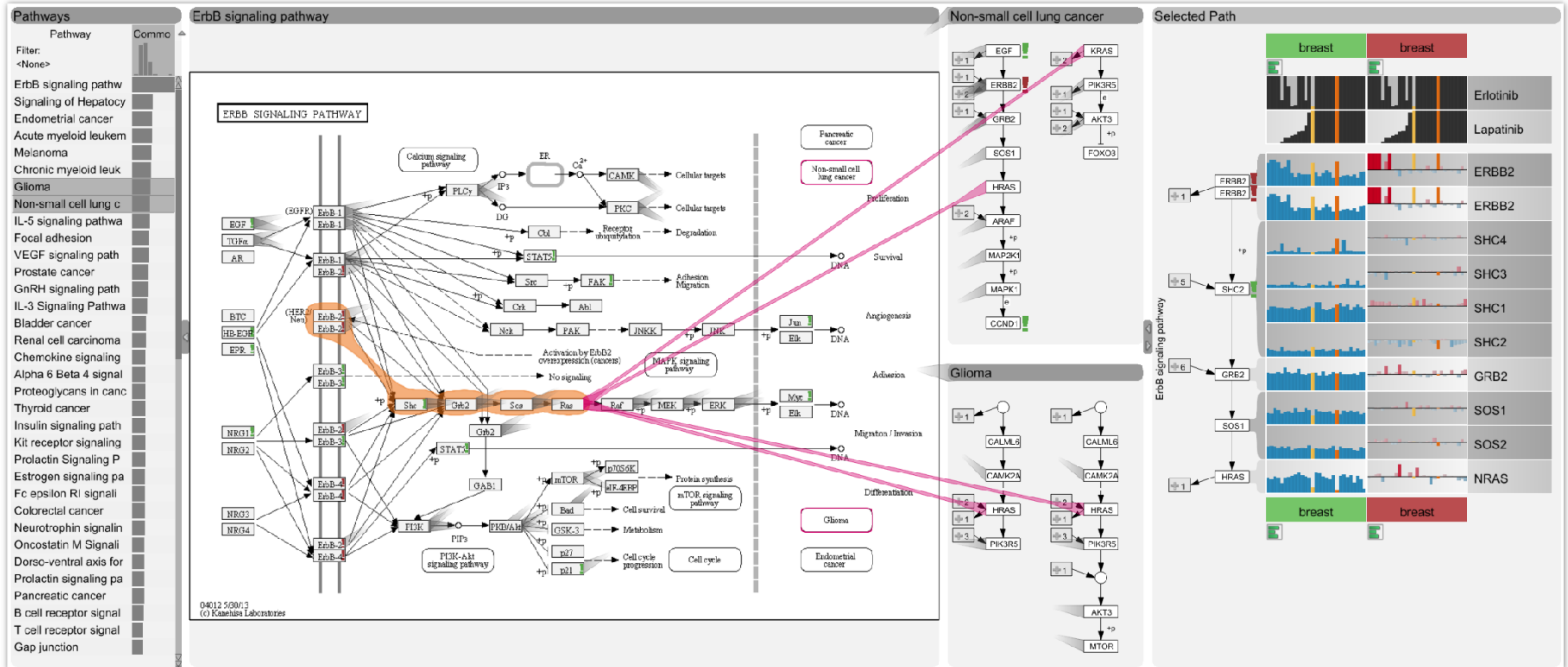
Area reserved for the details of the selected pathway, currently empty.

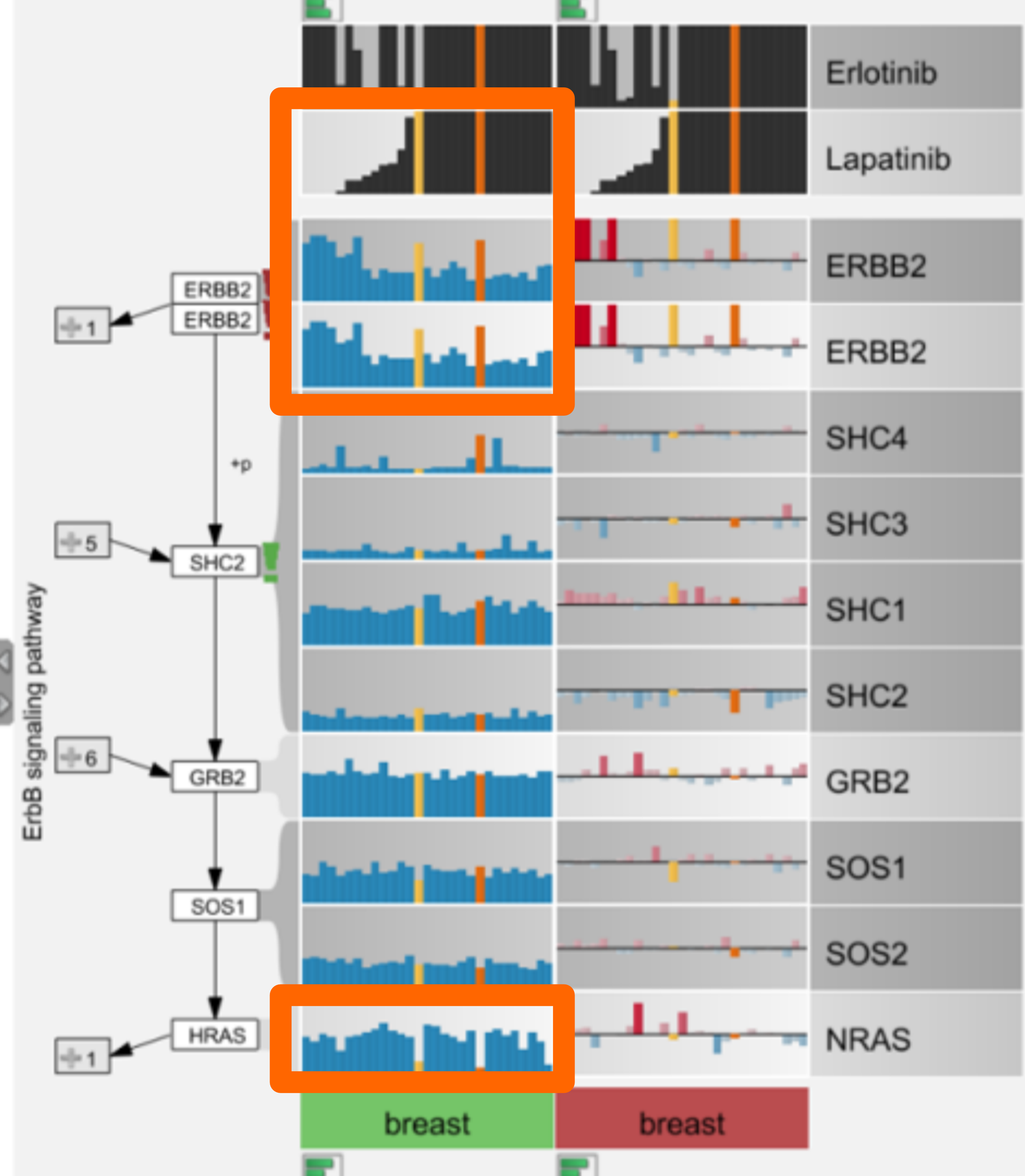
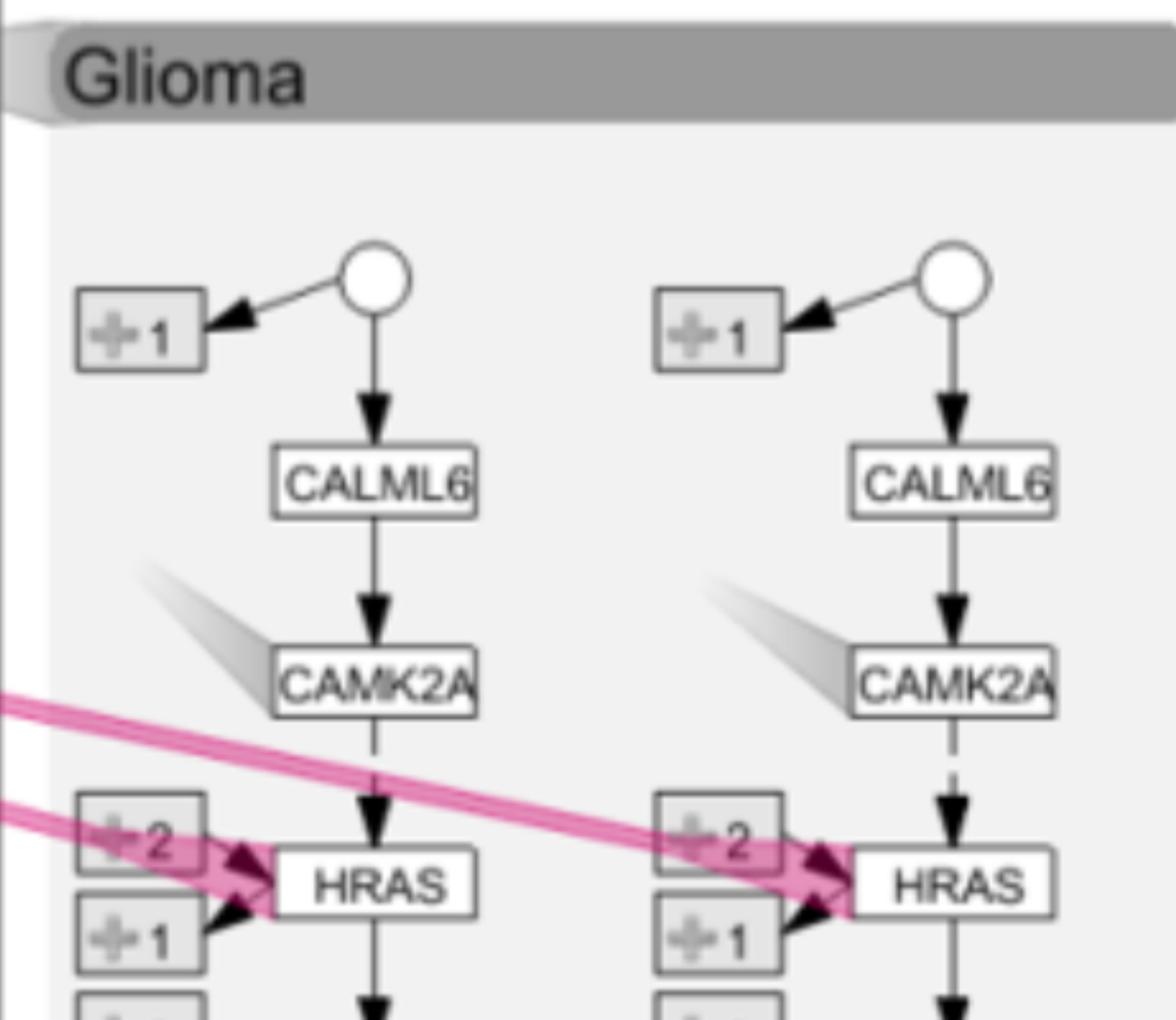
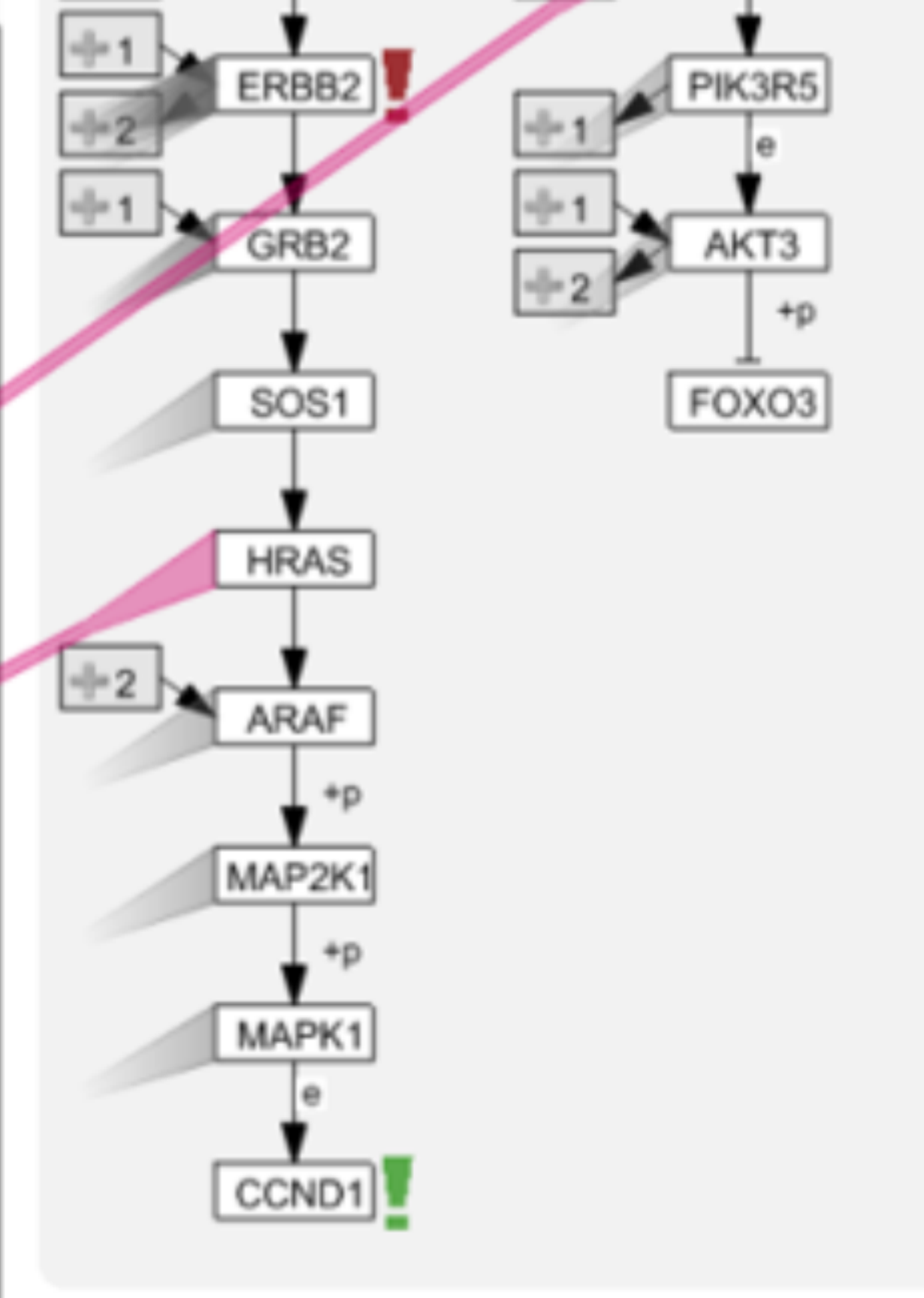






# Case Study: CCLE Data





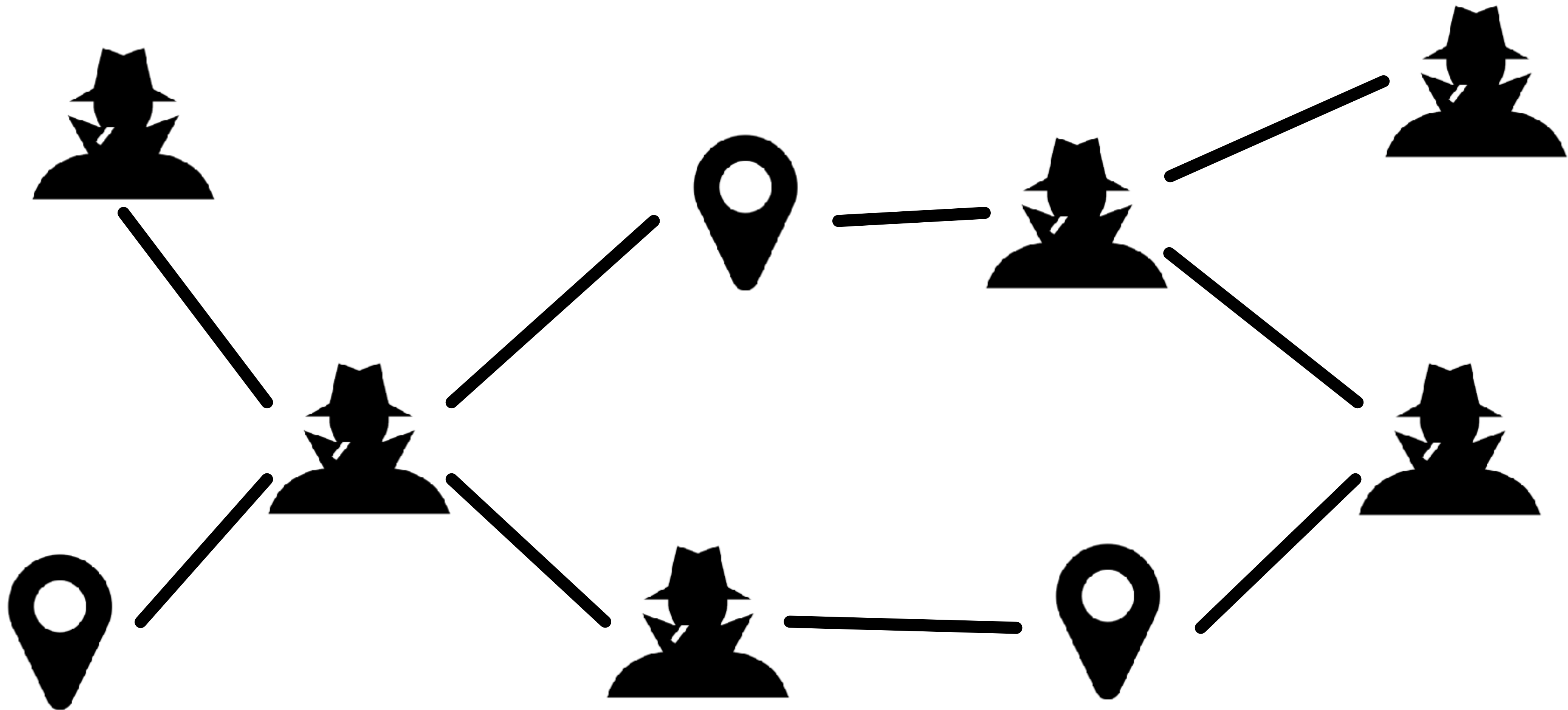
# Visual Analysis of Paths in Graphs

The screenshot displays the Pathfinder application interface. At the top, the search parameters are: Start: Hanspeter Pfister, End: Ben Shneiderman. The length of paths is set to 3, with a total of 105 paths found. The interface is divided into two main sections: Path List and Path Topology.

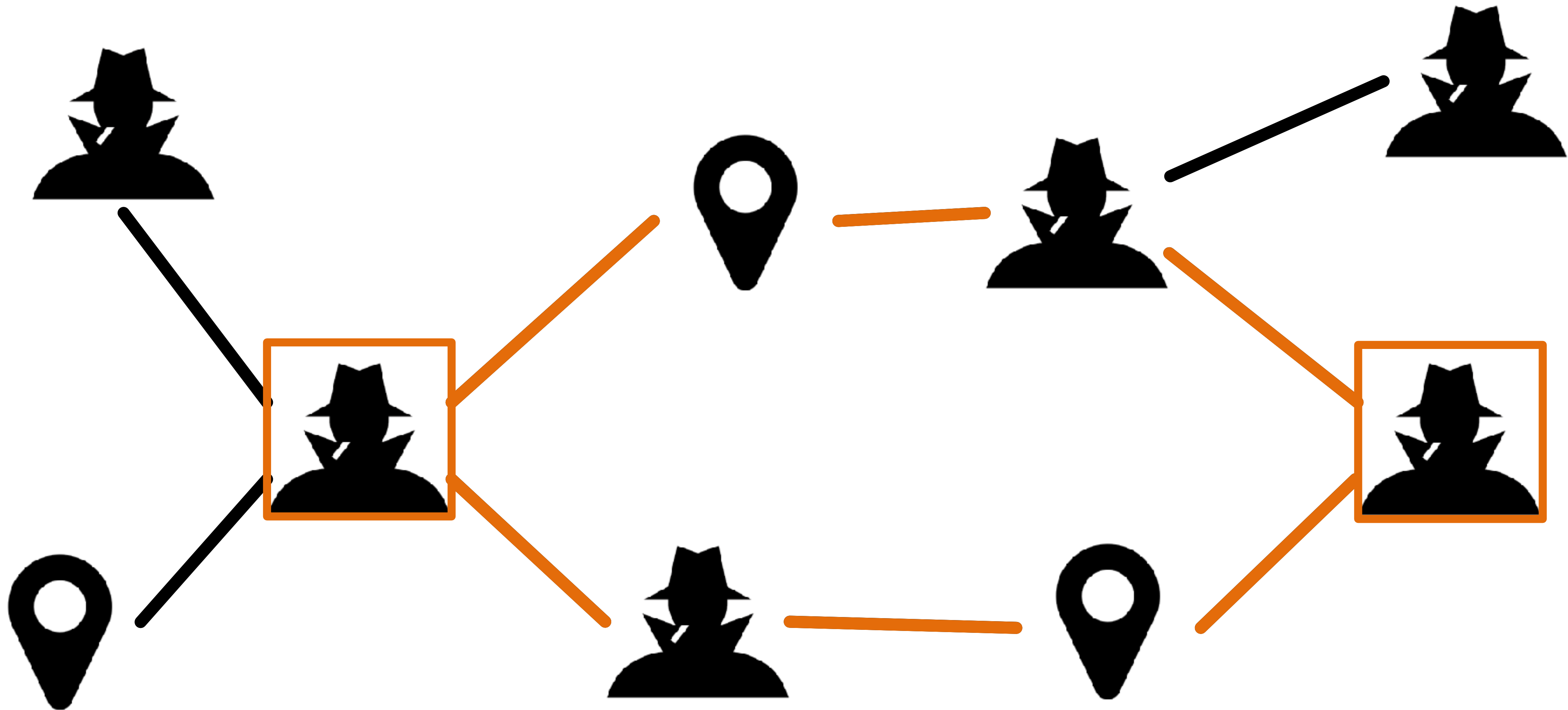
**Path List:** This section shows a list of paths of length 3. The selected path is highlighted in orange: Hanspeter Pfister - Krzysztof Z. Gajos - Desney S. Tan - Ben Shneiderman. Below the path names are various metrics represented by horizontal bars: chi\_publications, cited, degree, and tvcg\_publication.

**Path Topology:** This section shows a graph visualization of the selected path. The nodes are Hanspeter Pfister, Krzysztof Z. Gajos, Desney S. Tan, and Ben Shneiderman, connected in a sequence. The graph also shows other nodes connected to these, such as Frank van Ham, Adam Perer, Jean-Daniel Fekete, Catherine Plaisan, and Jennifer Golbeck.

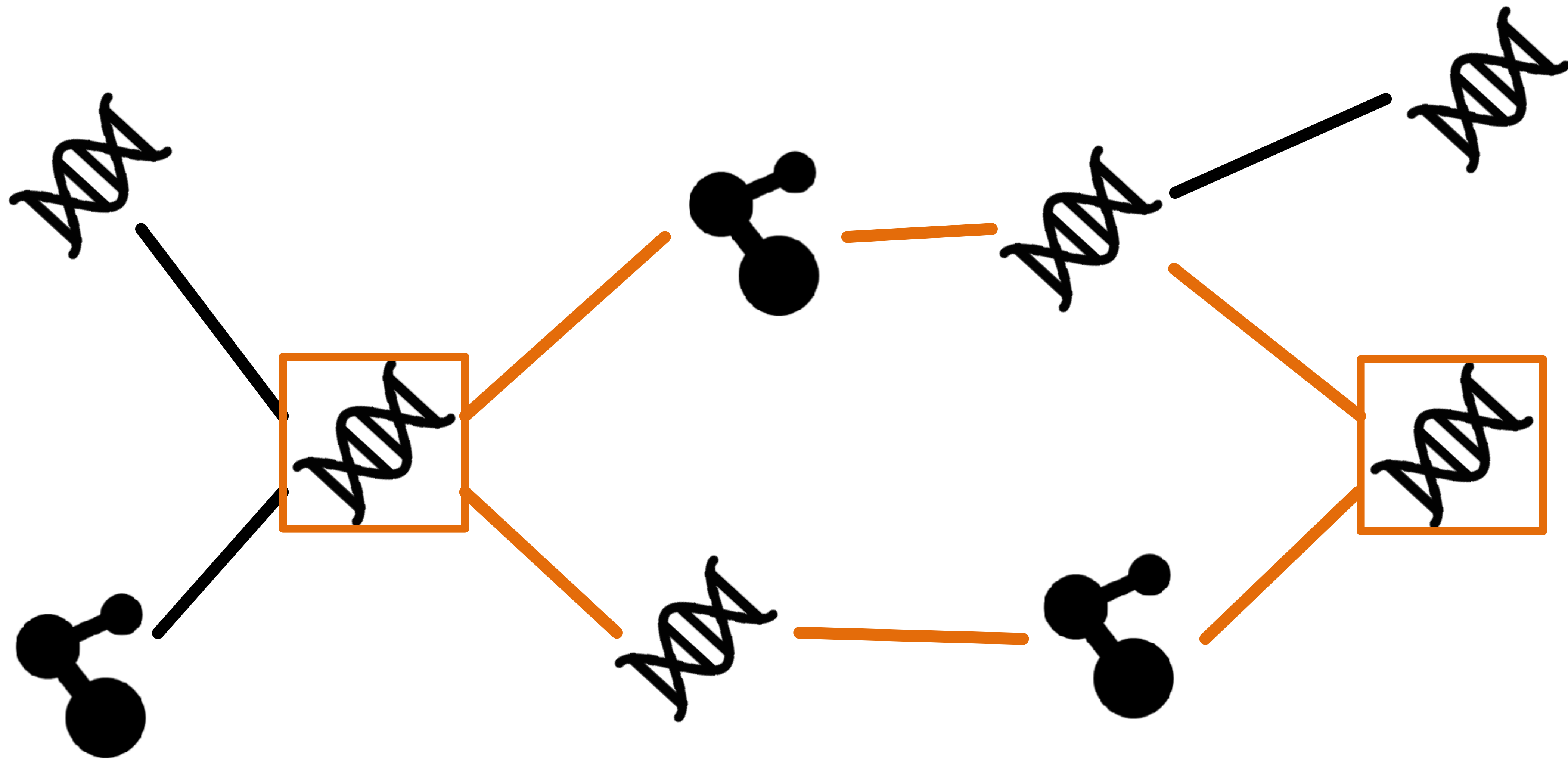
**Path Statistics:** This panel on the right provides summary statistics: Paths: 108/108, Edges: 196/196, Nodes: 95/95. It includes two horizontal bar charts: one for Author (95/95) and one for Sets (137/843). The Author chart shows Ben Shneiderman as the most frequent author. The Sets chart shows CHI (107/667) as the most frequent set.



**Intelligence Data:** How are two suspects connected?



**Intelligence Data:** How are two suspects connected?



**Biological Network:** How do two genes interact?

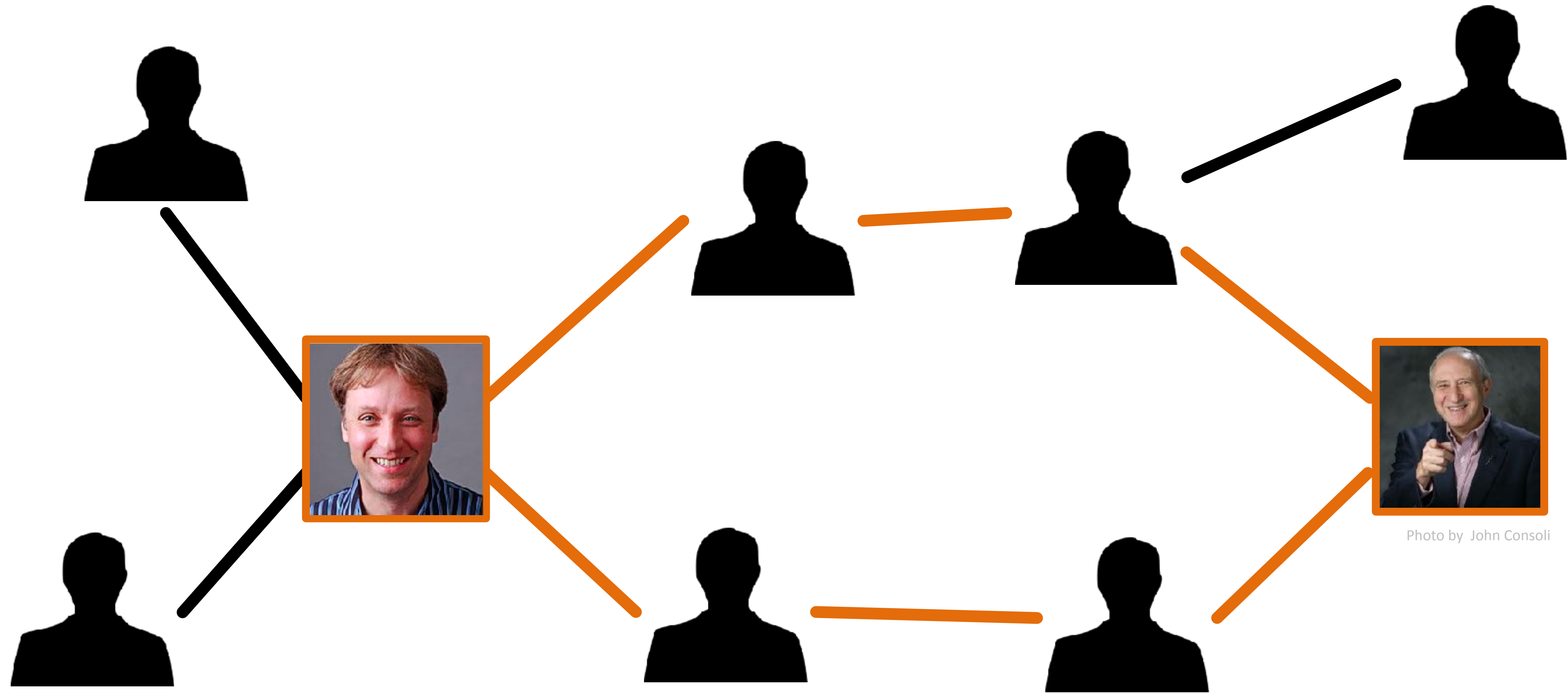
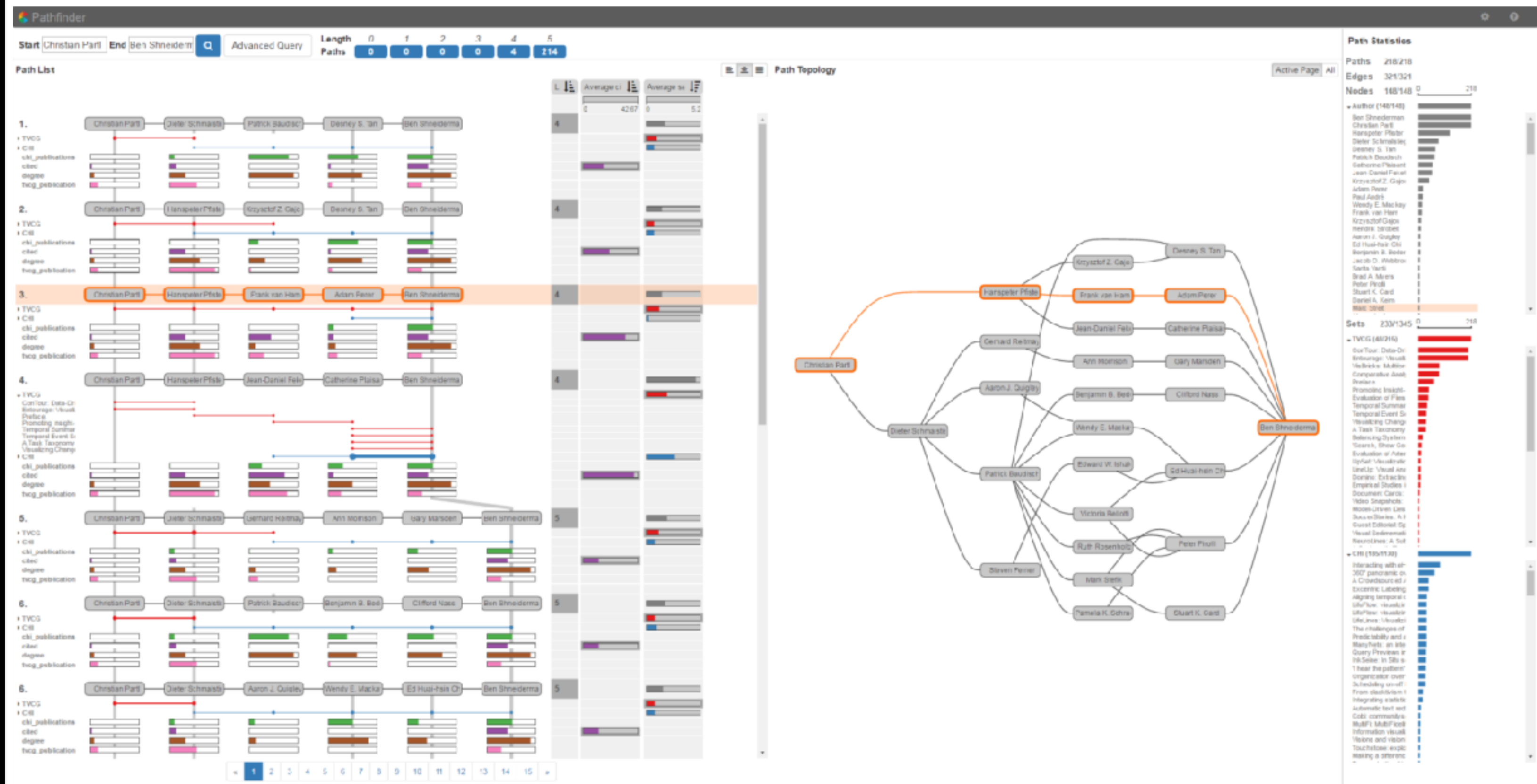


Photo by John Consoli

**Coauthor Network:** How is HP Pfister connected to Ben Shneiderman?

# Pathfinder

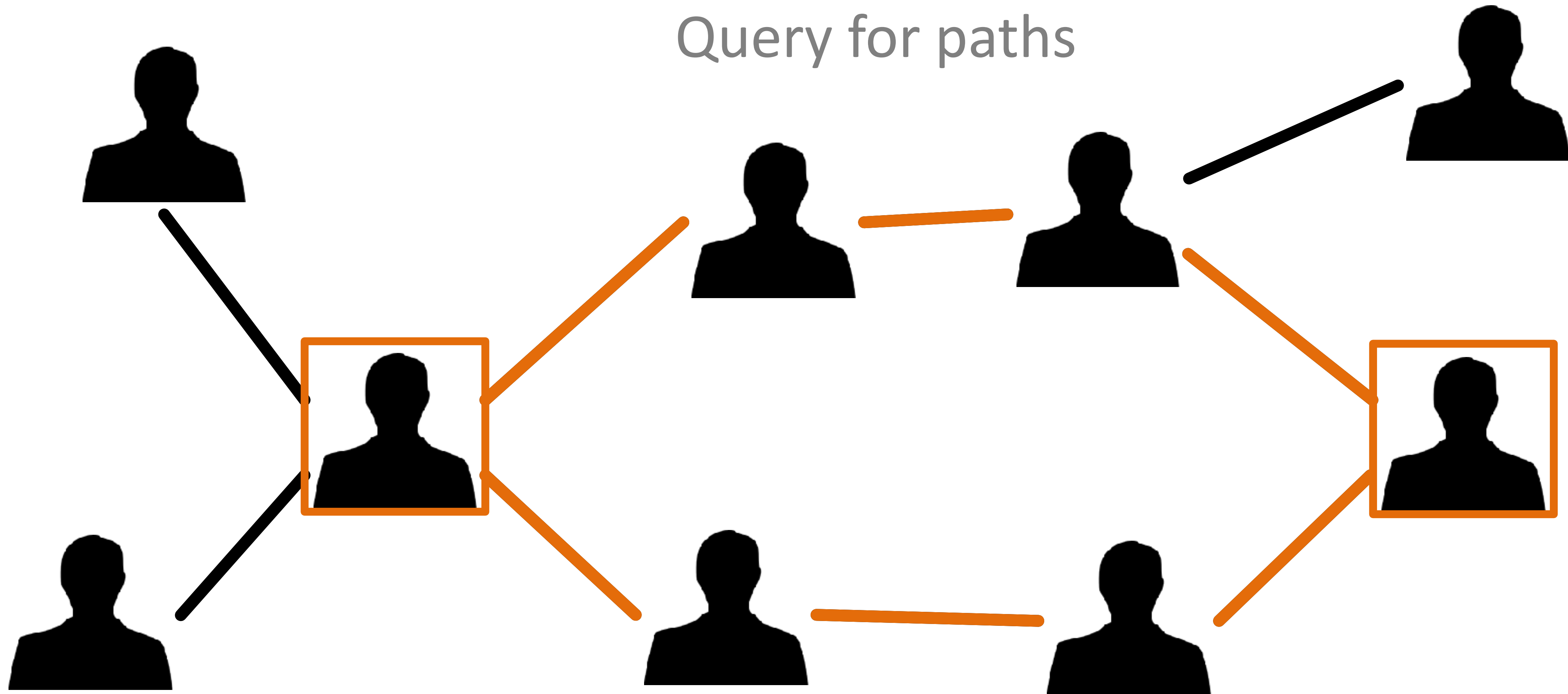


## Visual Analysis of Paths in Large Multivariate Graphs



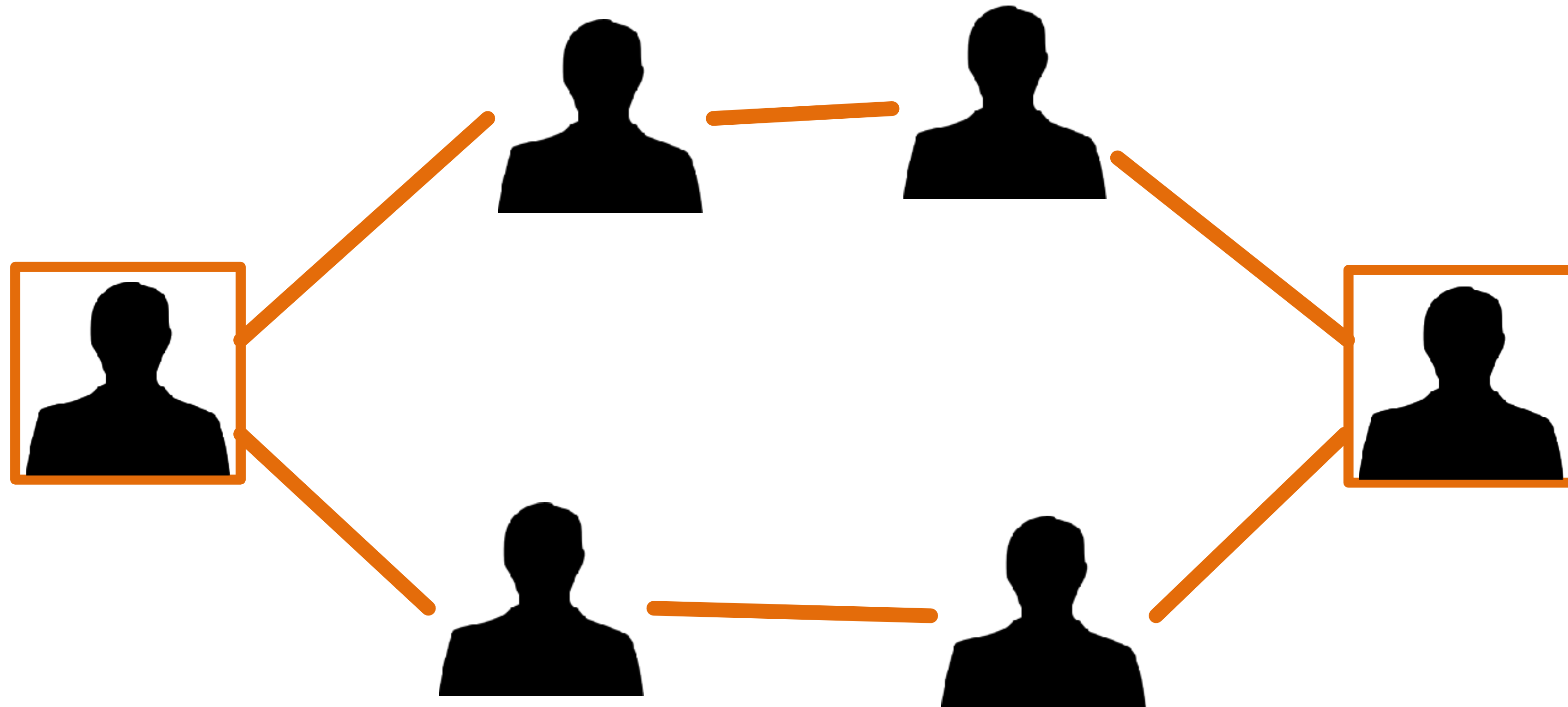
# Pathfinder Approach

Query for paths



# Pathfinder Approach

Shows more direct links diagram..

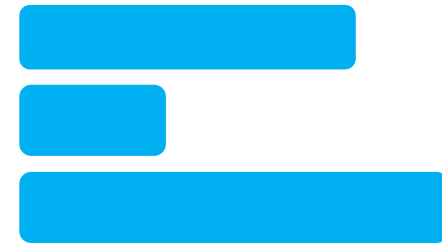


# Pathfinder Approach

Update ranking to identify important paths

Path Score

1.



2.

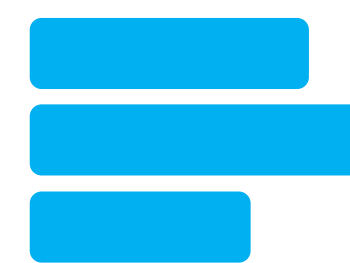
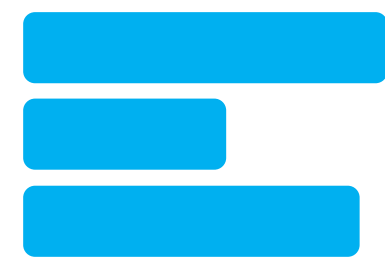
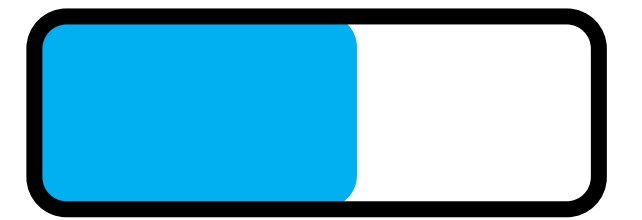


# Pathfinder Approach

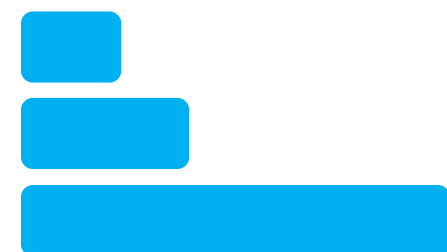
Update ranking to identify important paths

Path Score

1.



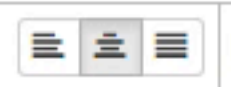
2.



Start  End

Path Statistics

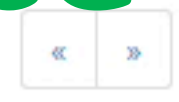
Path List



Path Topology

Active Page All

# Query Interface



# Path Representation

2.

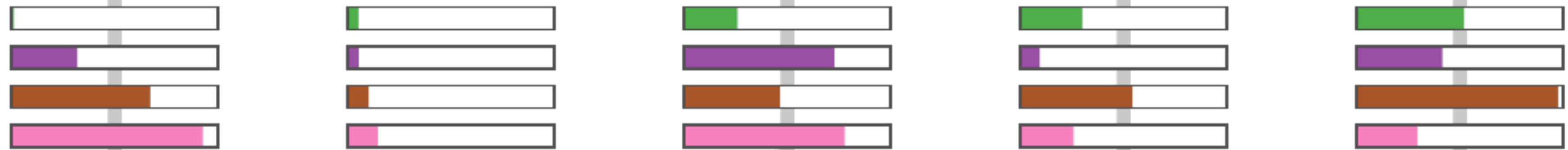


- ▼ CHI
  - A table!: improving
  - Excentric Labeling
  - LifeFlow: visualizir
  - Query Previews in
  - LifeLines: Visualiz
  - The challenges of
  - Organization over

Sets

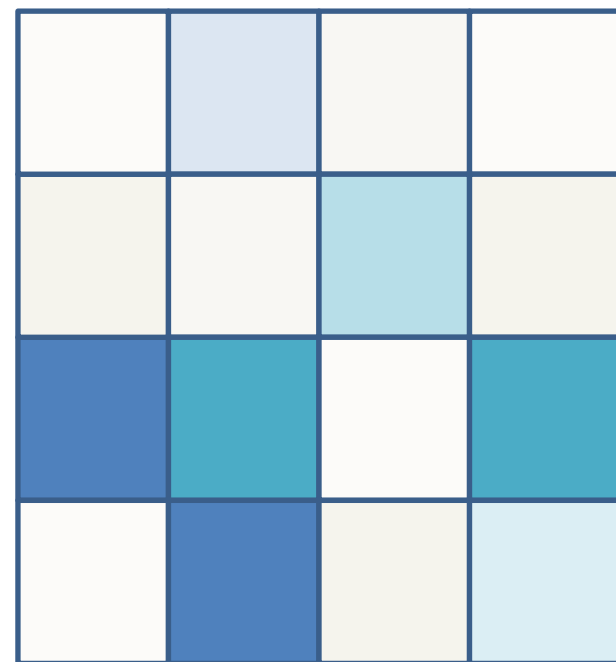
Numerical Attributes

- ▼ TVCG
  - UpSet: Visualizati
  - Visual Sedimentat
  - SoccerStories: A h
  - Promoting Insight-
  - Temporal Summar
  - Temporal Event S
  - A Task Taxonomy
  - Visualizing Chang
- chi\_publications
- cited
- degree
- tvcg\_publication





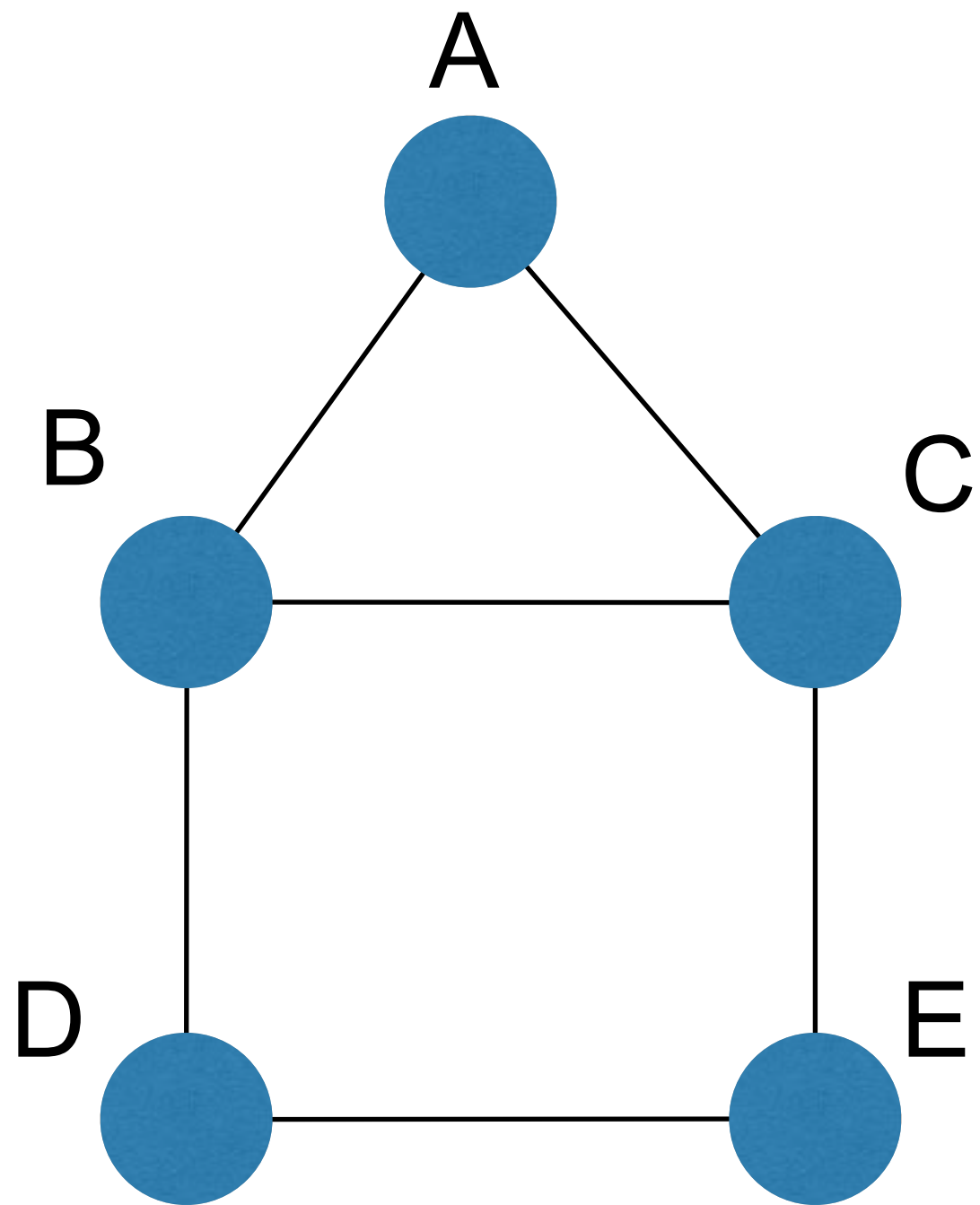
# Matrix Representations





# Matrix Representations

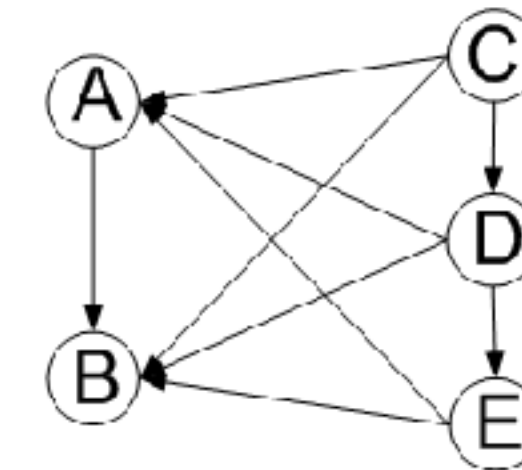
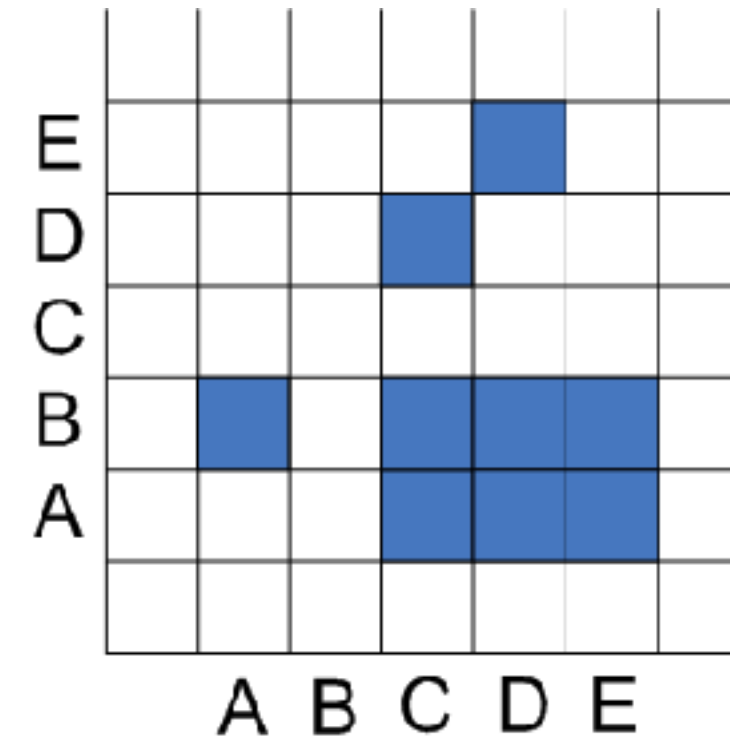
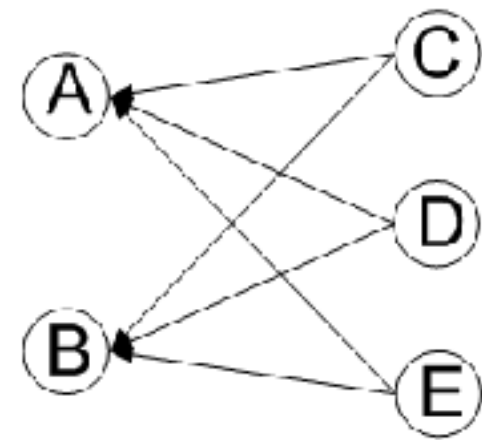
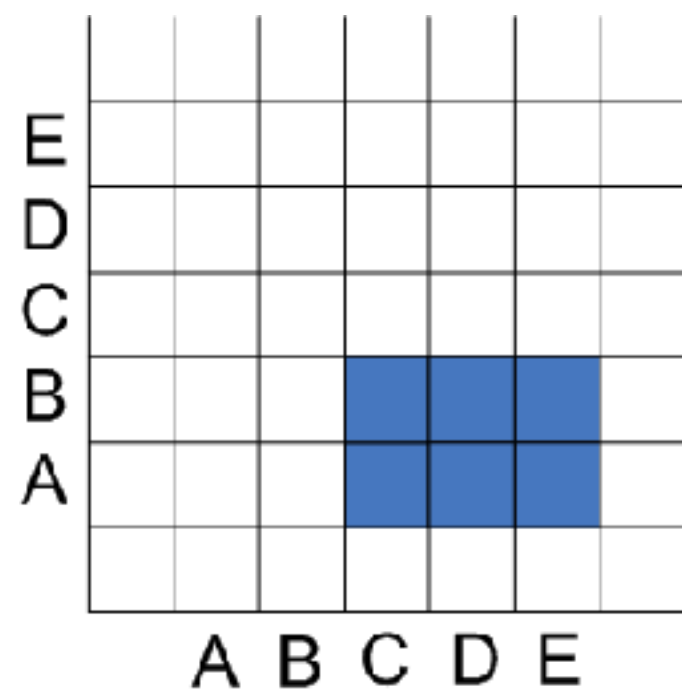
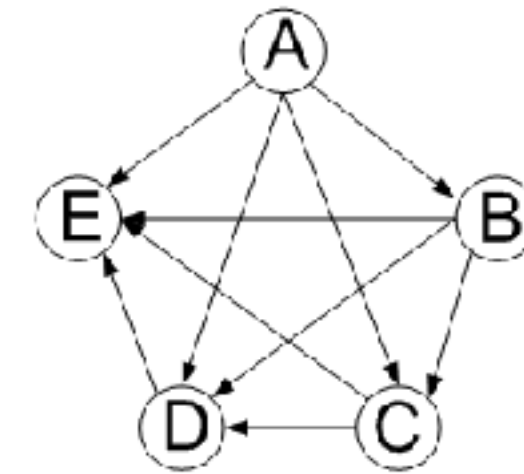
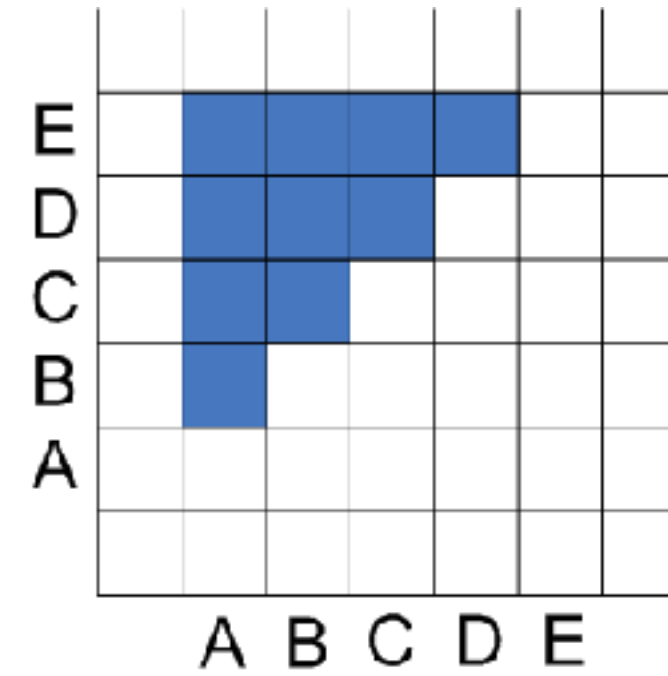
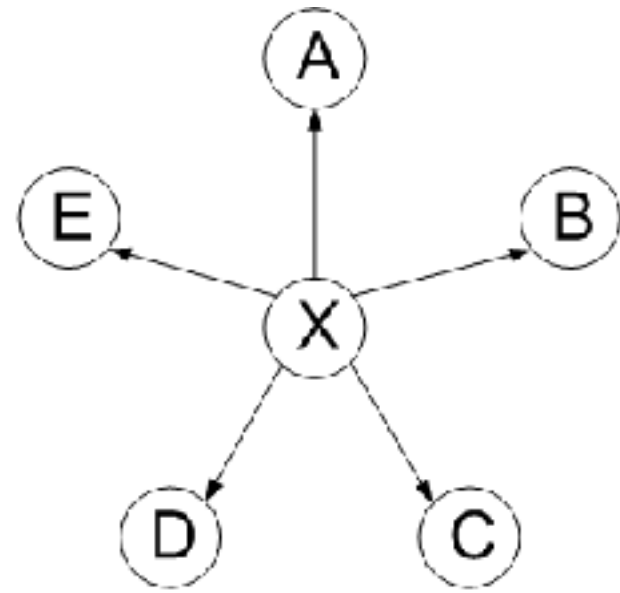
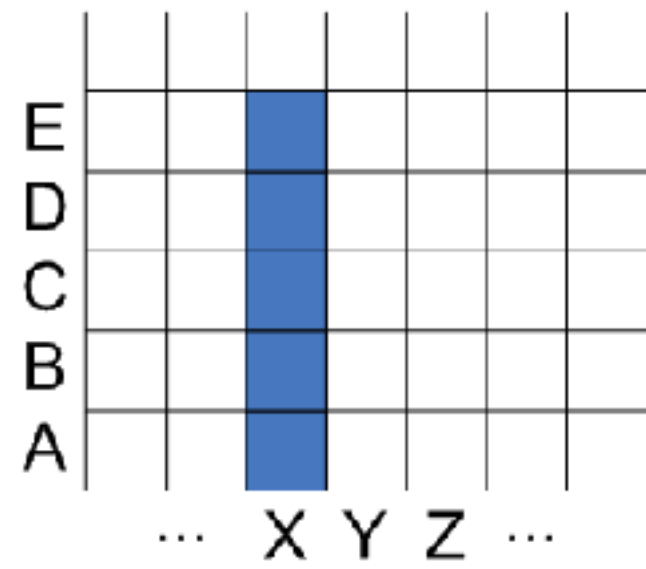
Instead of node link diagram, use adjacency matrix



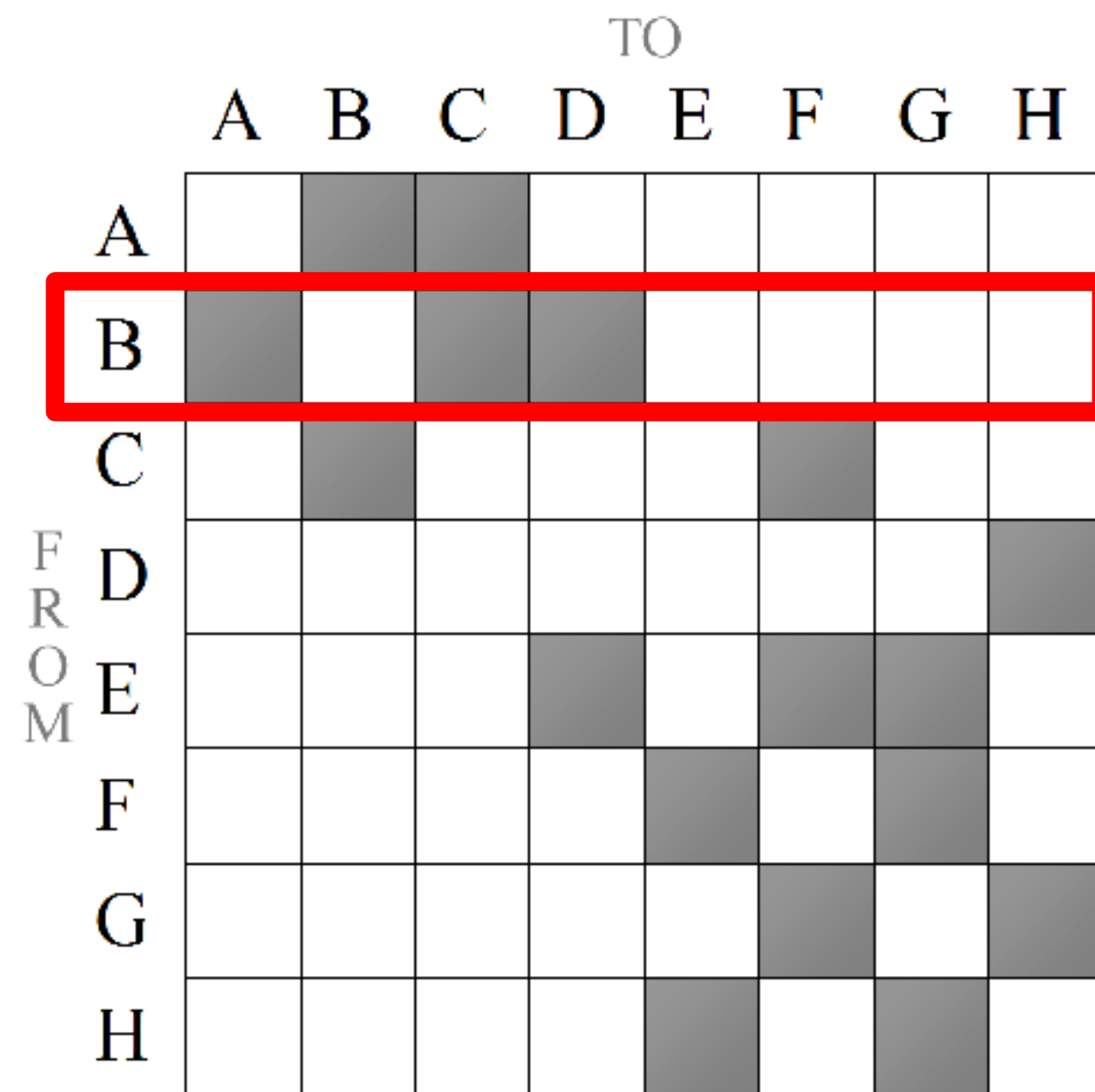
	A	B	C	D	E
A		■	■		
B	■		■	■	
C	■	■			■
D		■			■
E			■	■	

# Matrix Representations

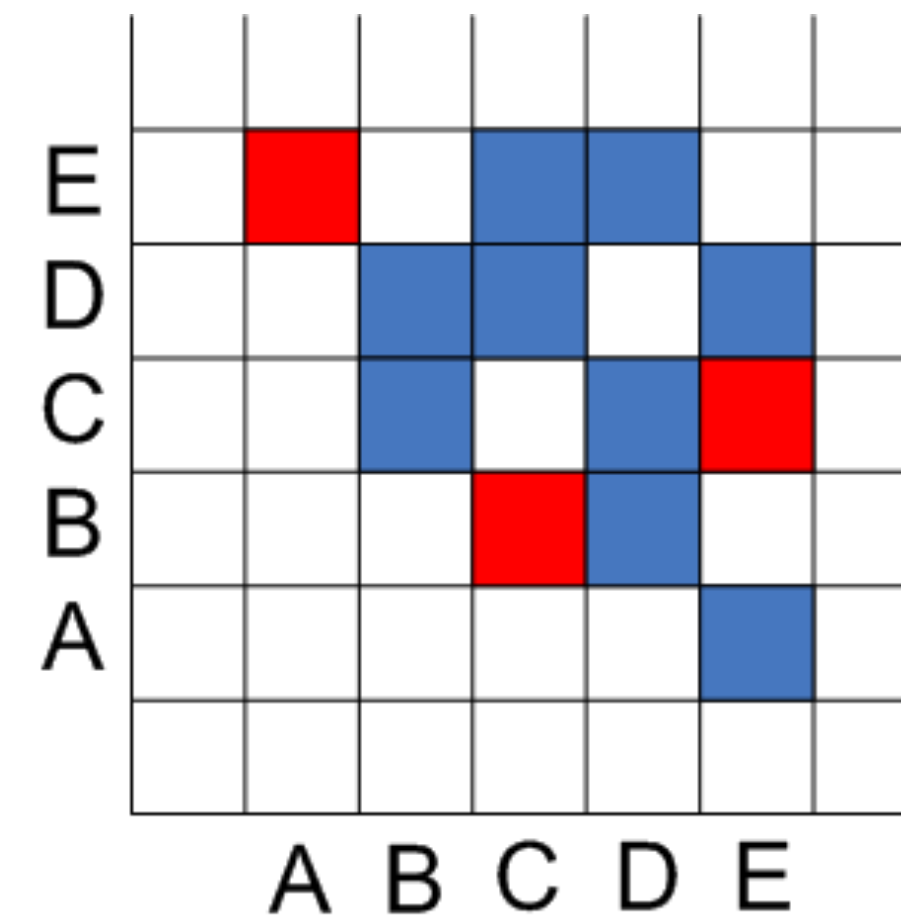
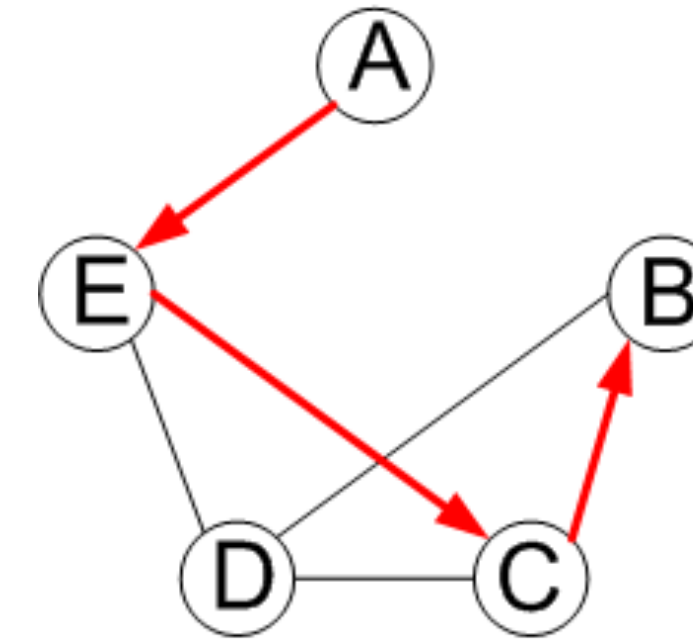
Examples:



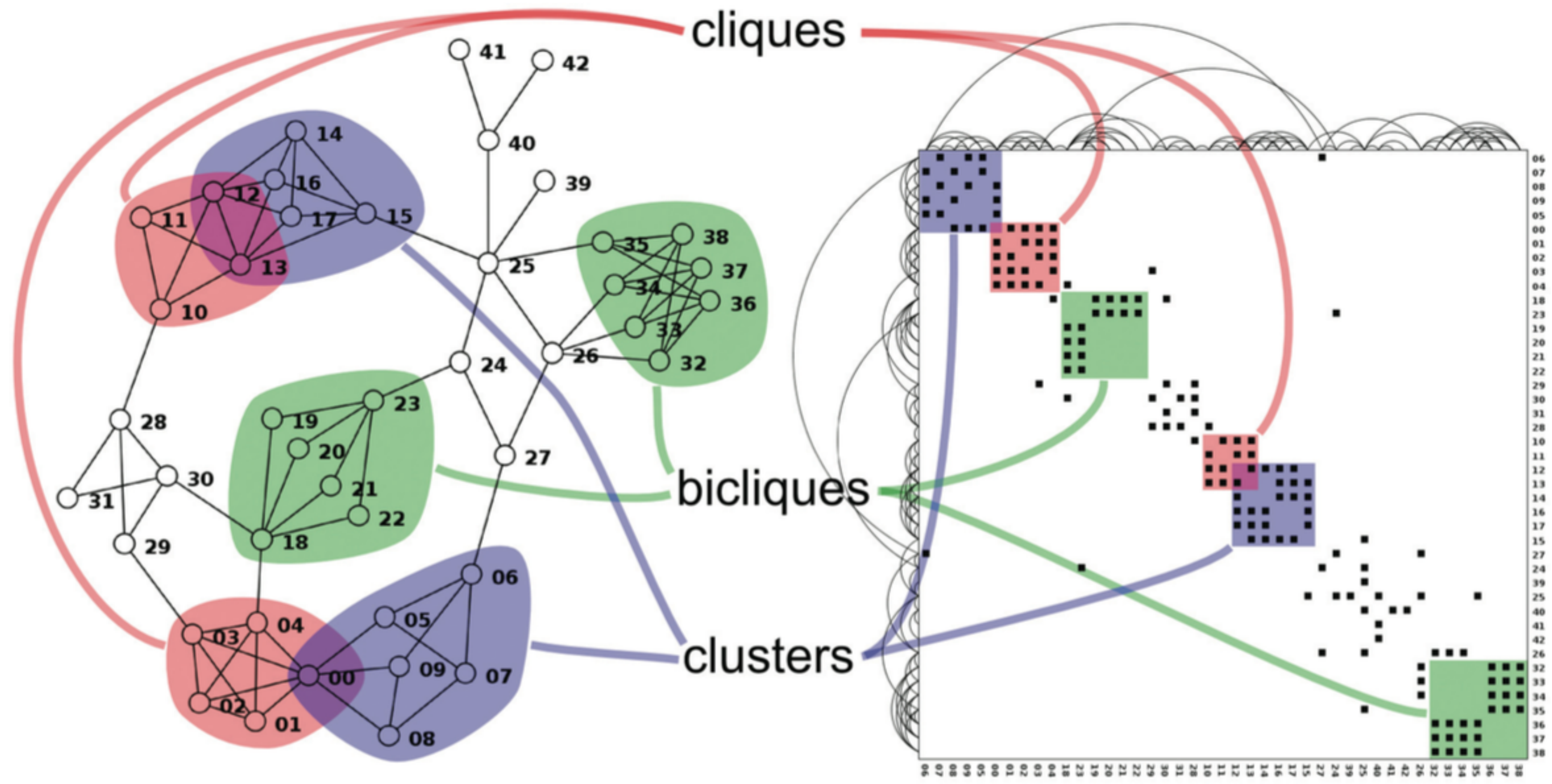
# Matrix Representations



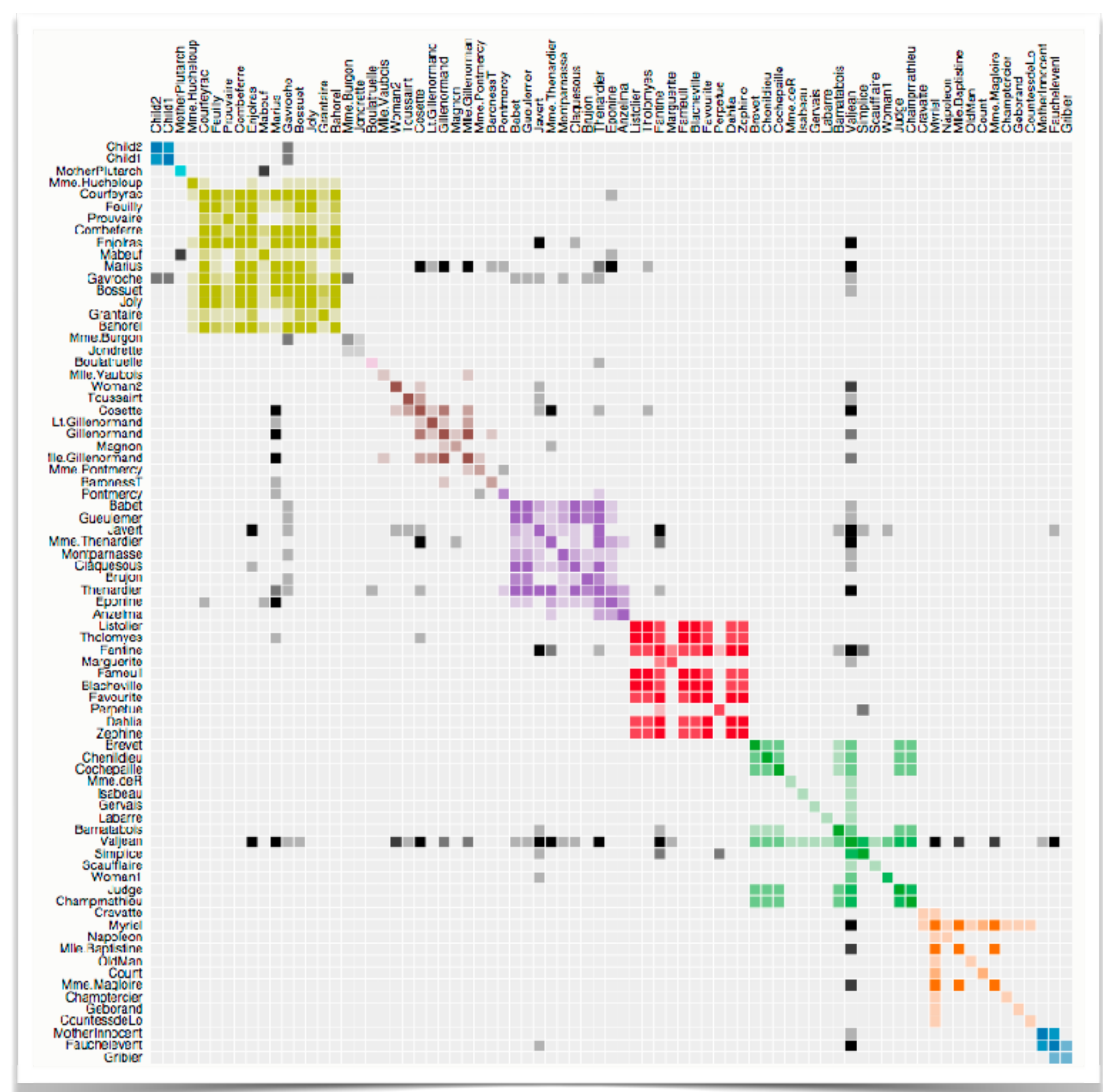
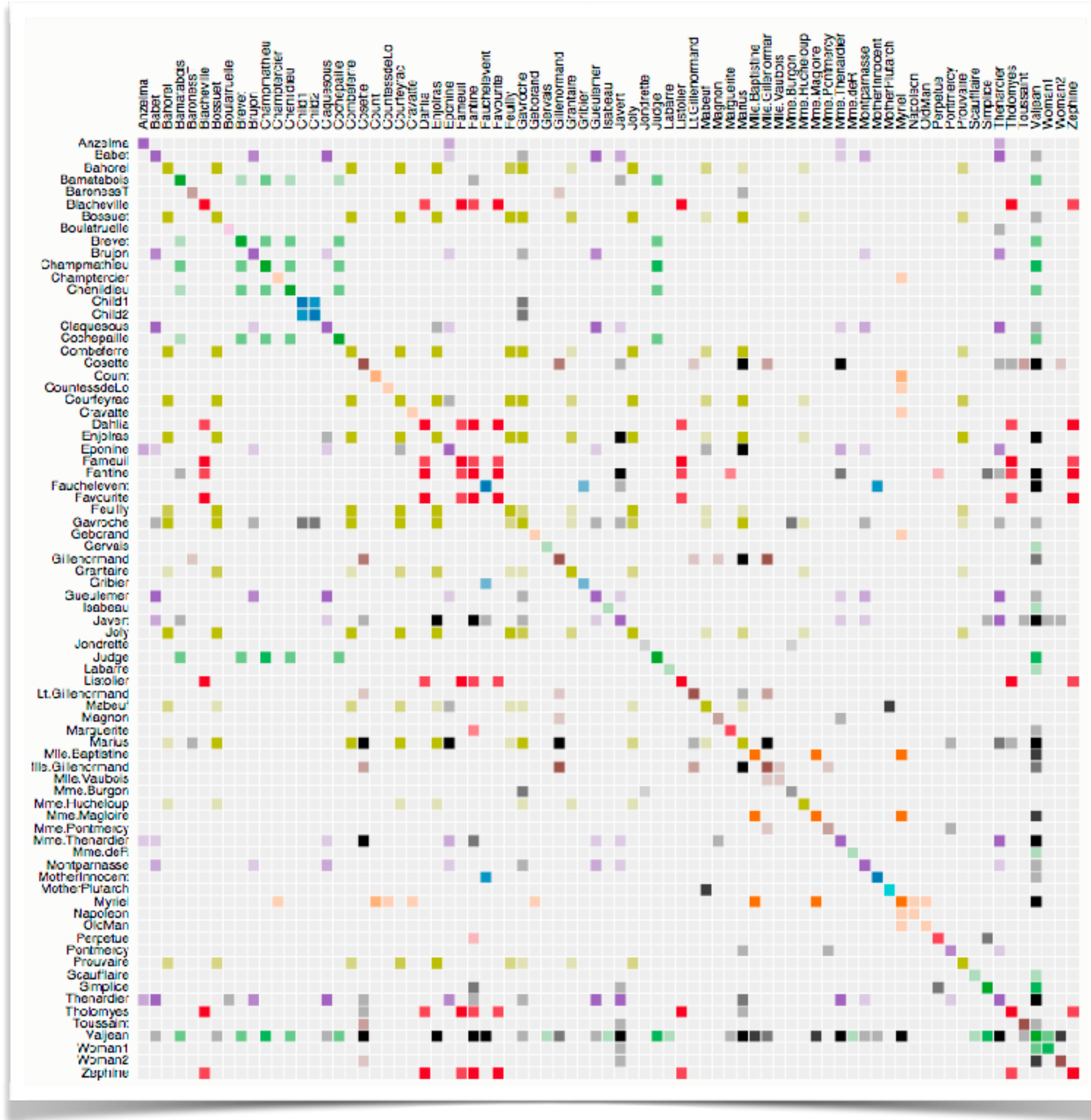
Well suited for  
neighborhood-related TBTs



Not suited for  
path-related TBTs



# Order Critical!



# Matrix Representations

## Pros:

can represent **all graph classes** except for hypergraphs

puts **focus on the edge set**, not so much on the node set

simple grid -> **no elaborate layout** or rendering needed

well suited for **ABT on edges** via coloring of the matrix cells

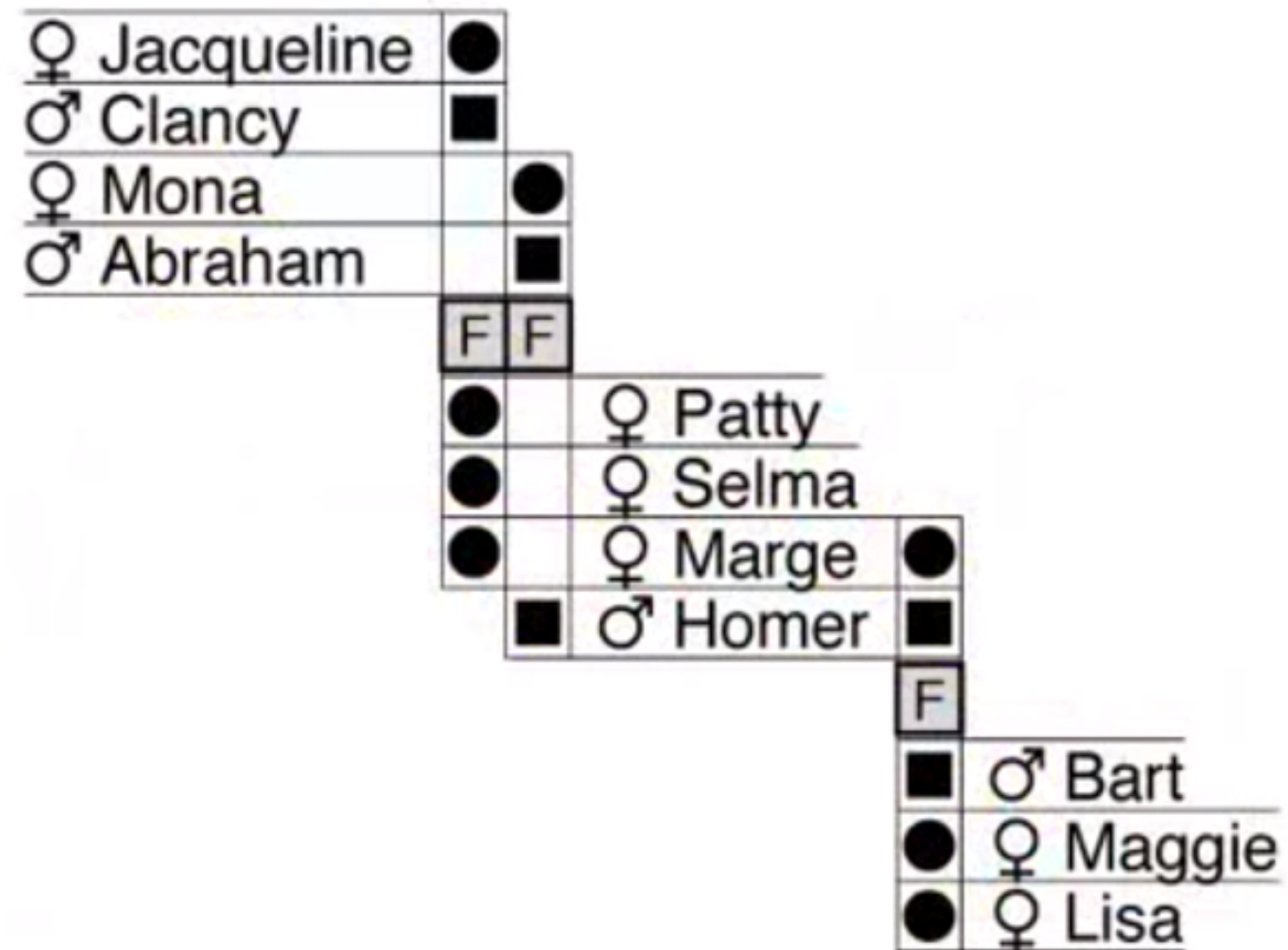
well suited for **neighborhood-related TBTs** via traversing rows/columns

## Cons:

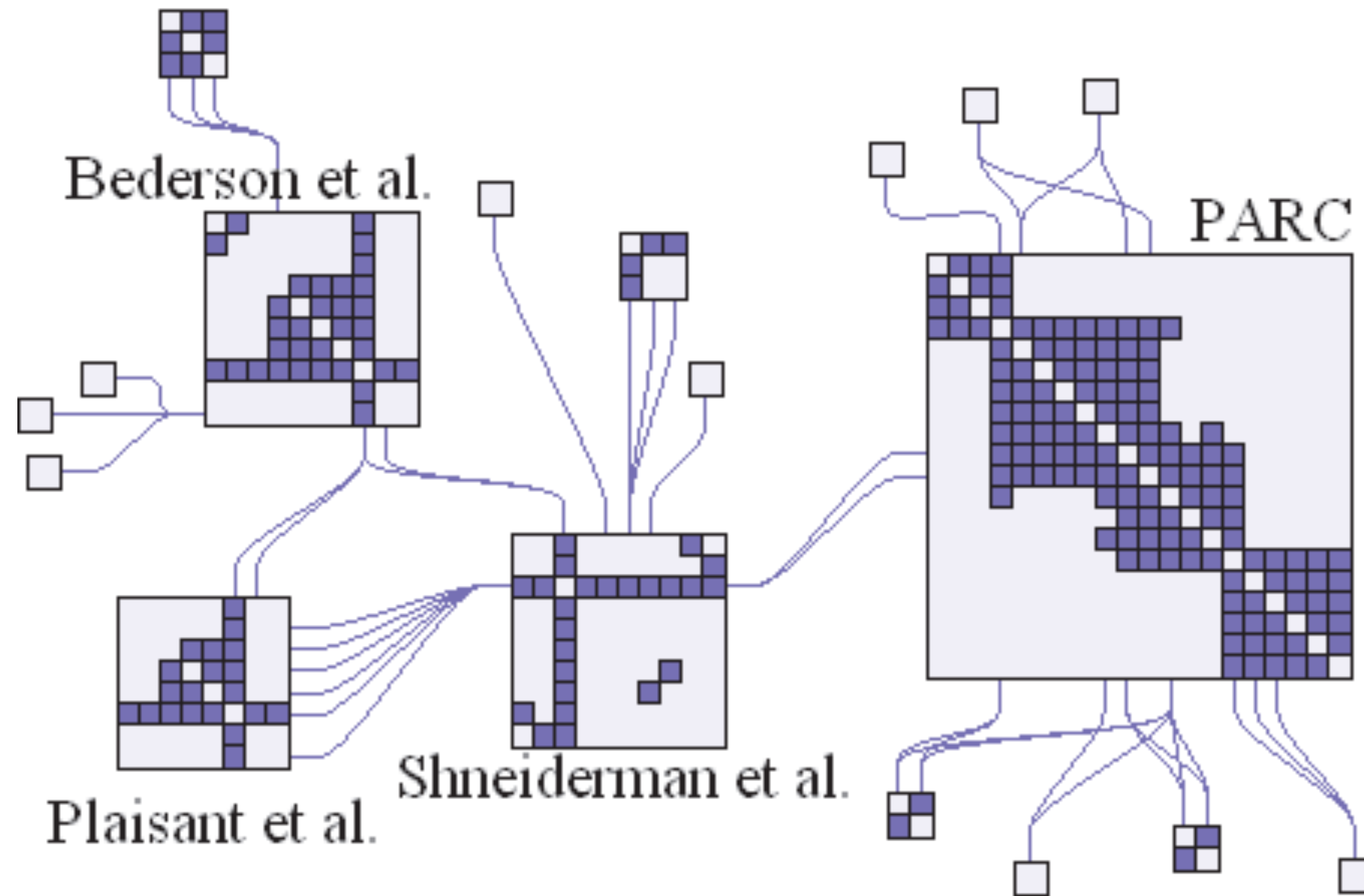
quadratic screen space requirement (any possible edge takes up space)

not suited for path-related TBTs

# Special Case: Genealogy



# Hybrid Explicit/Matrix

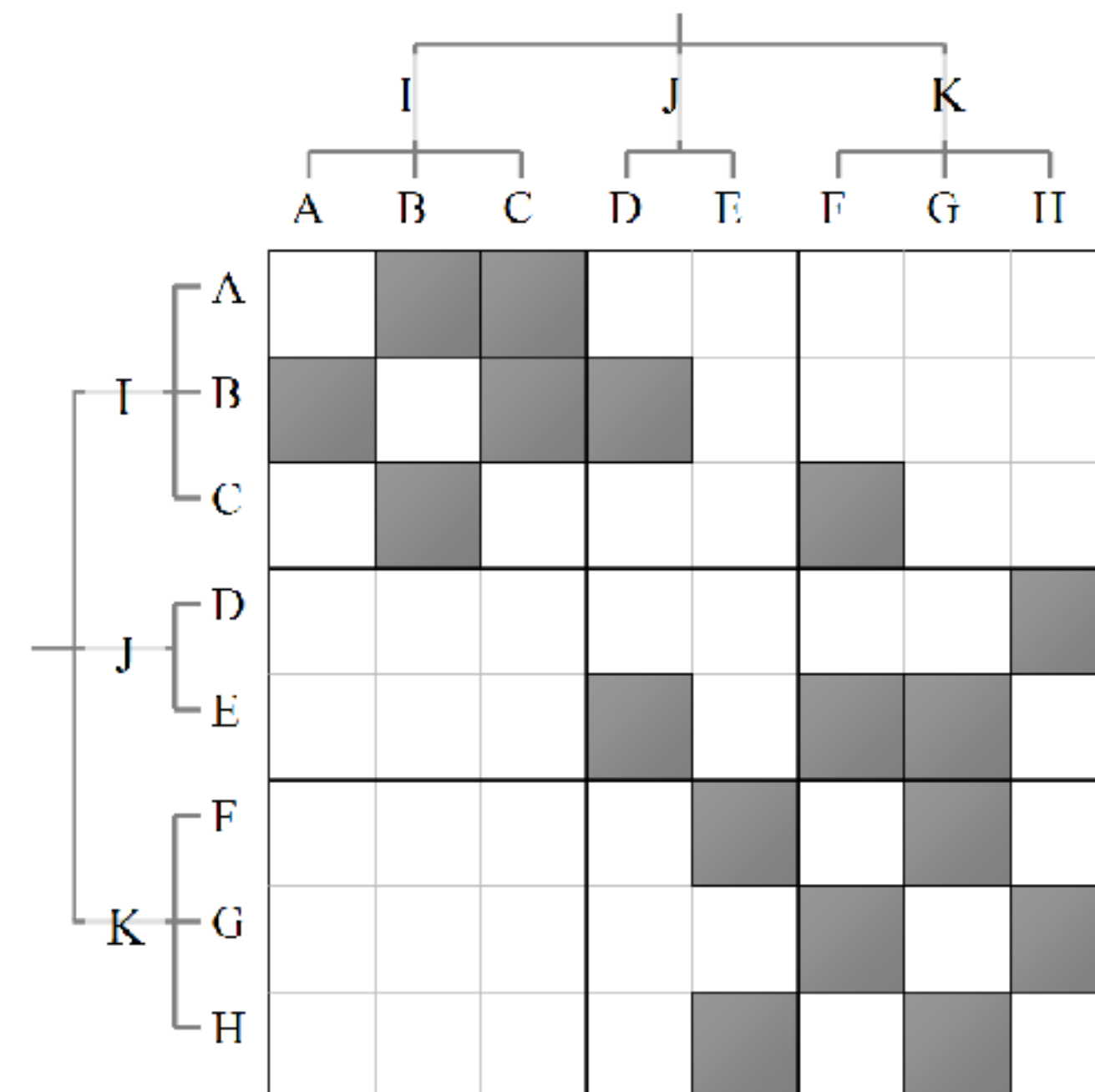
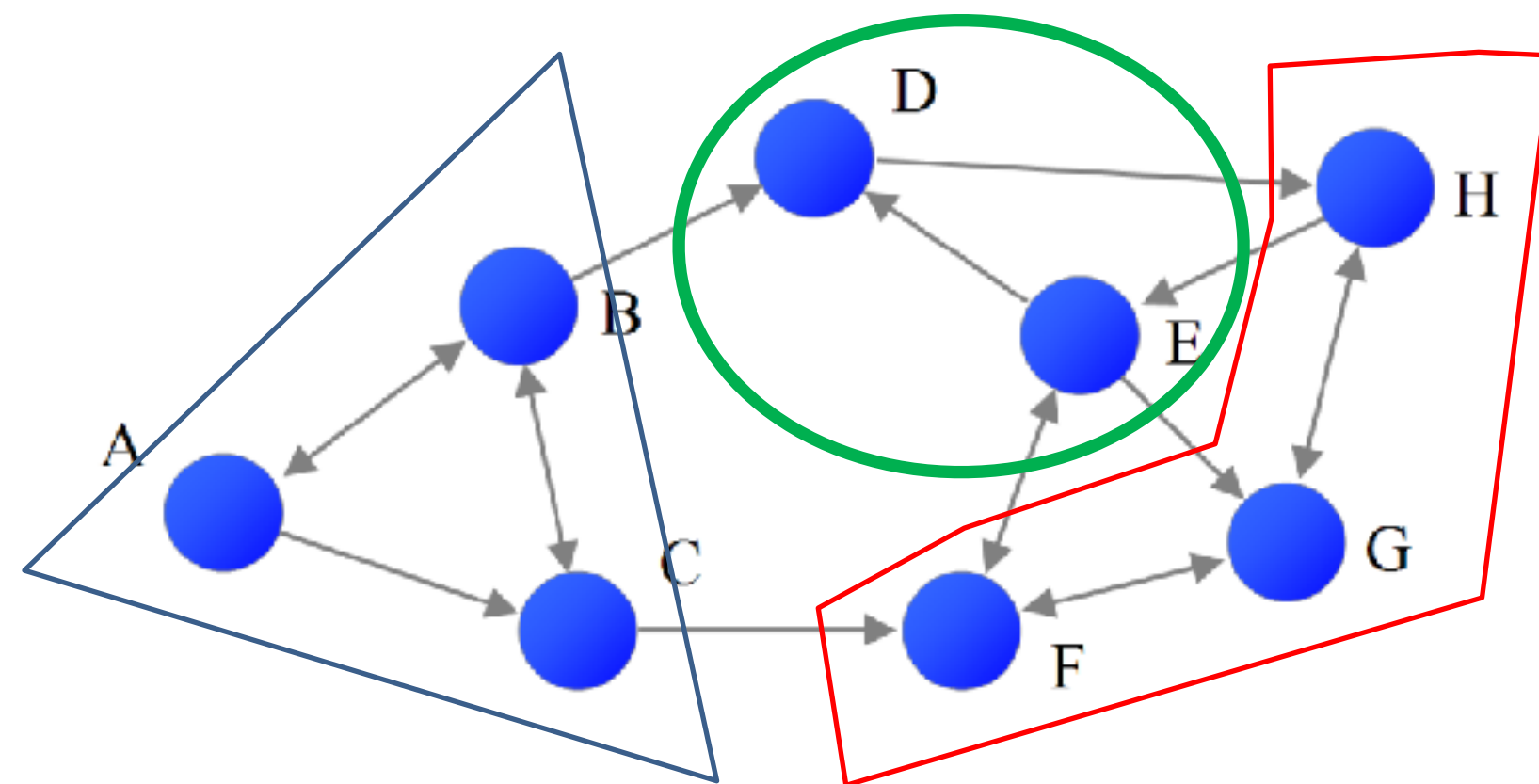




# Matrix Representations

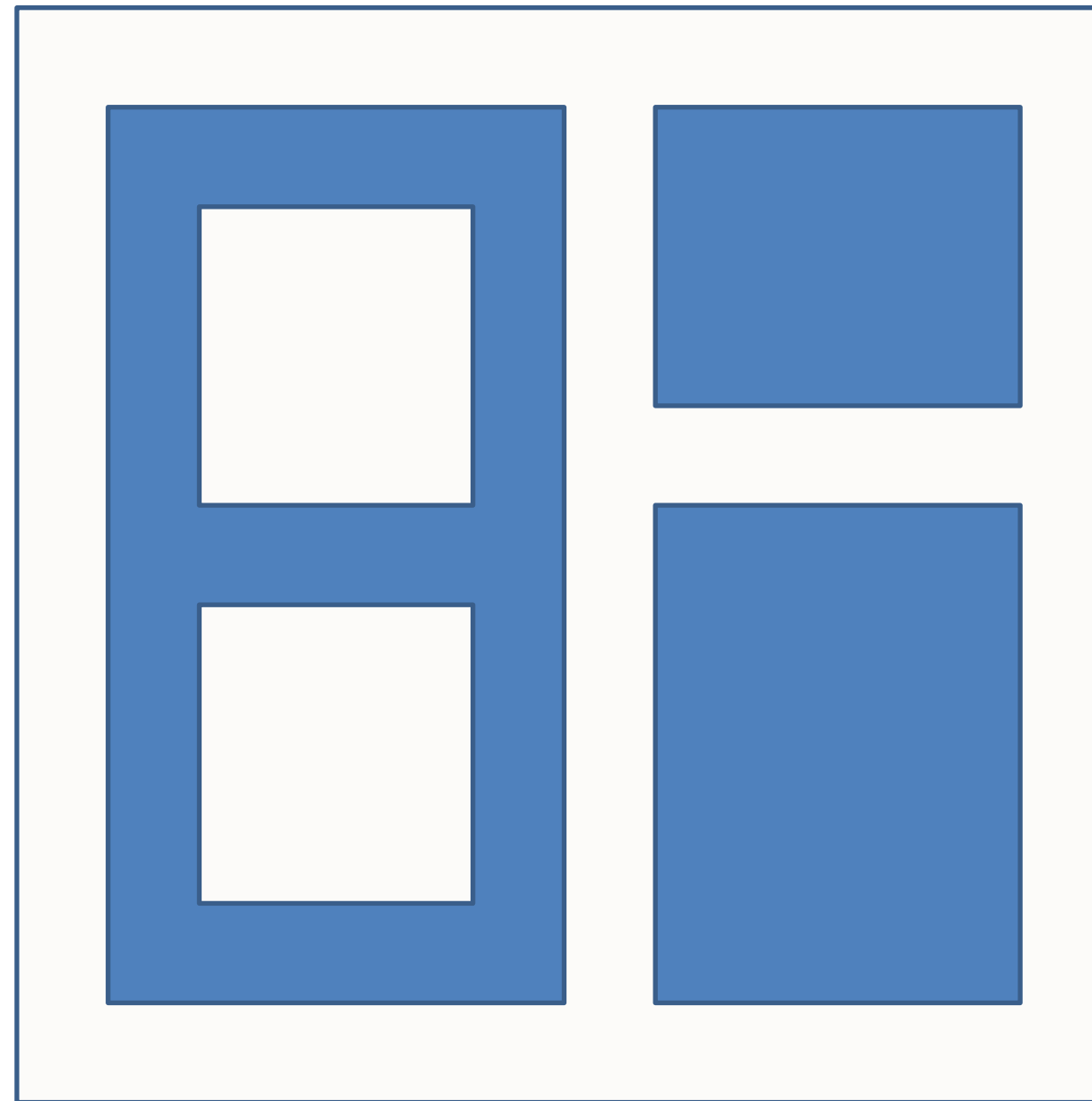
**Problem #1:** used screen real estate is quadratic in the number of nodes

**Solution approach:** hierarchization of the representation

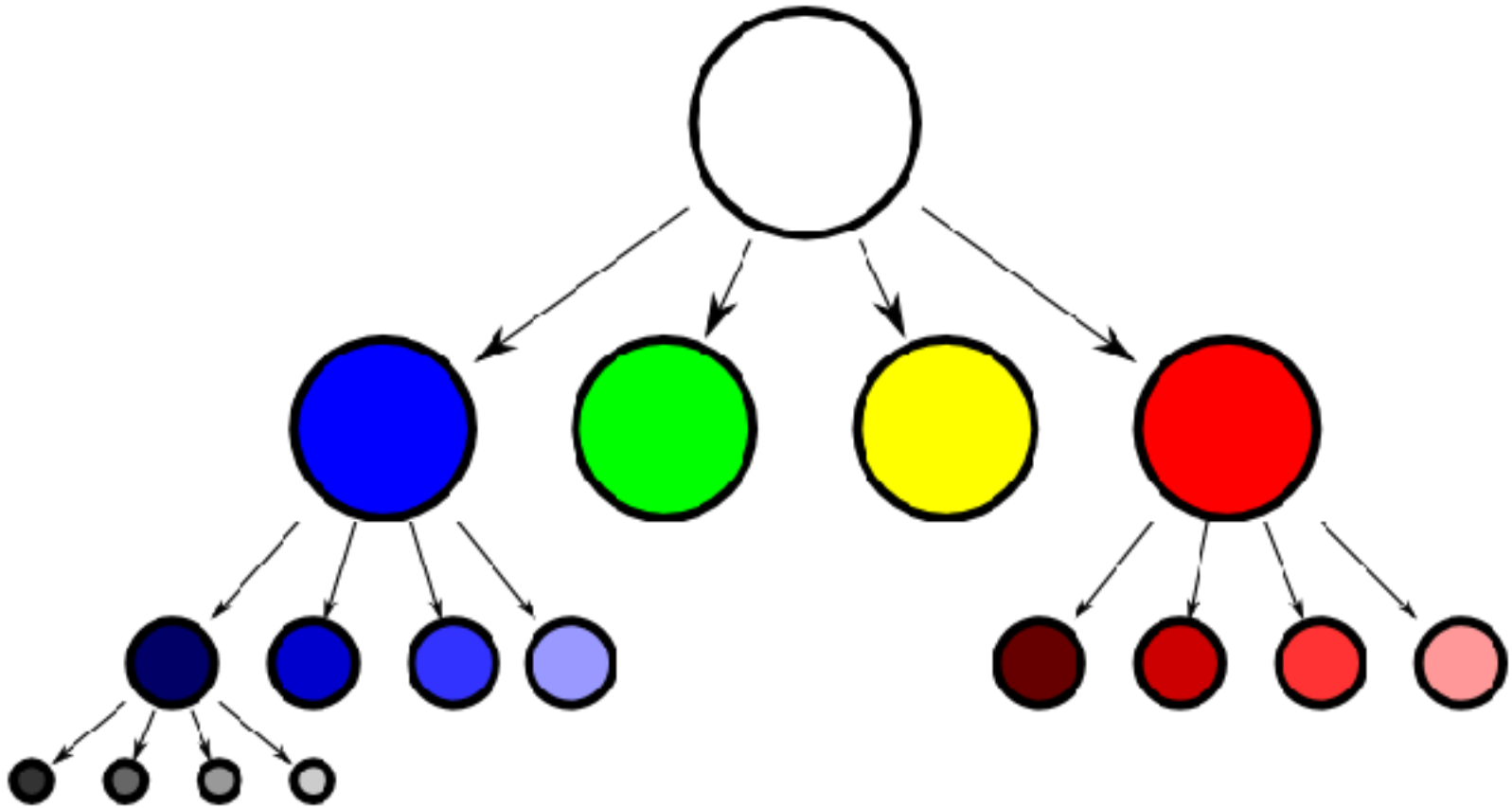
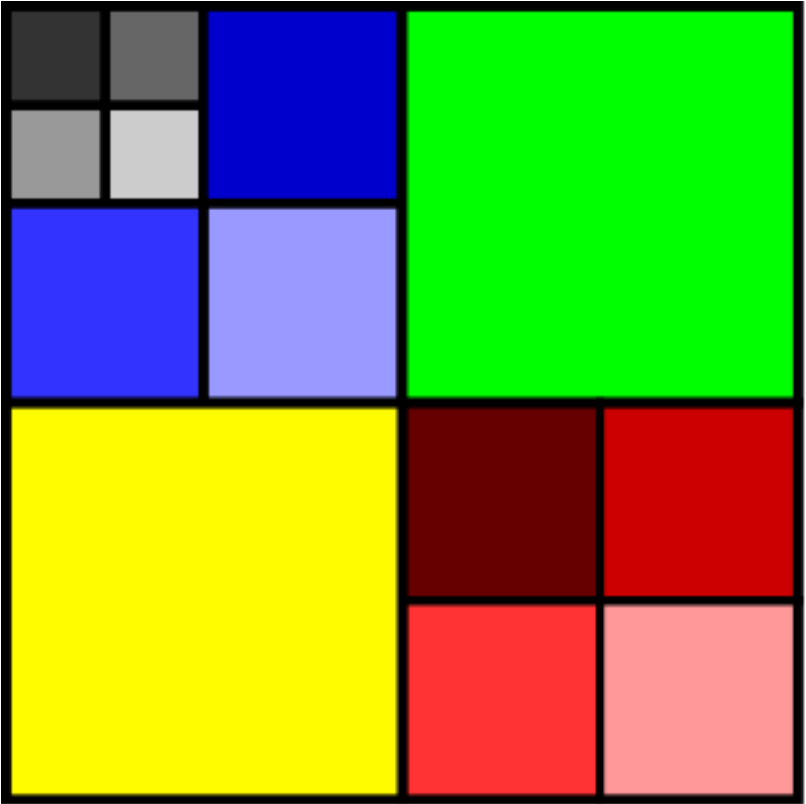
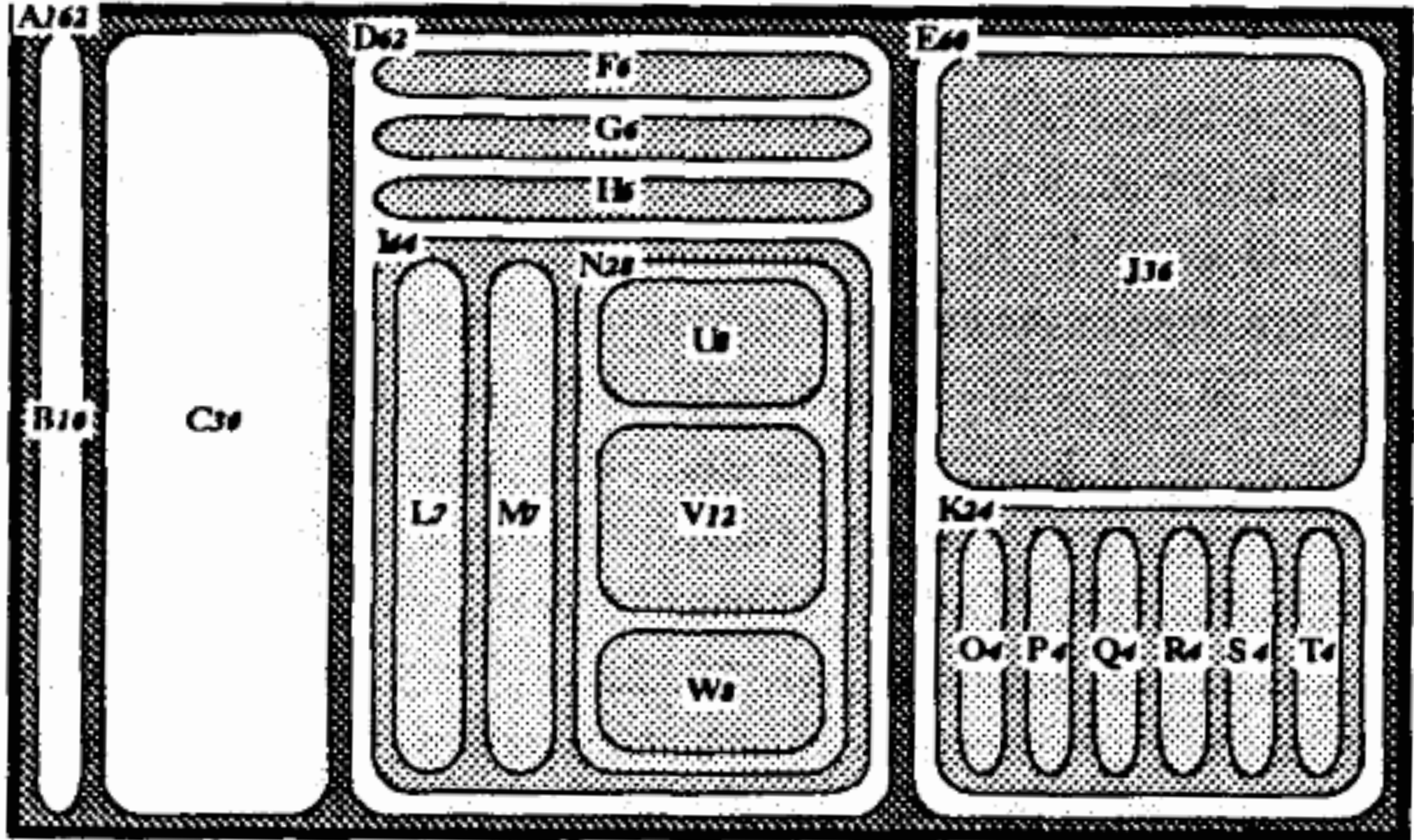
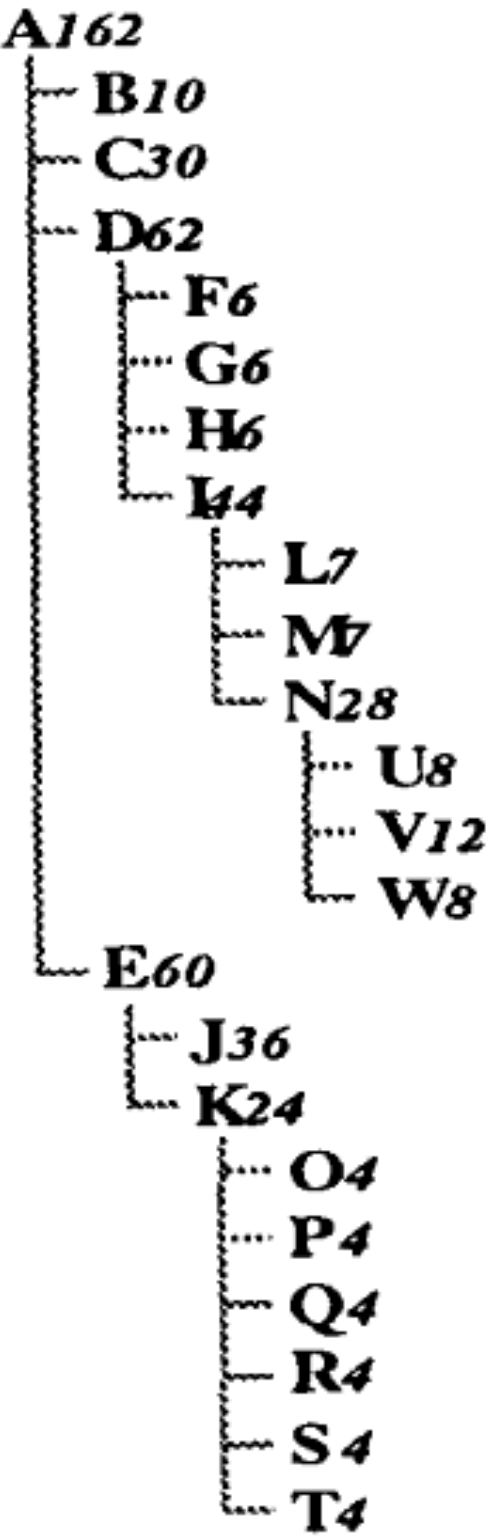


[van Ham et al. 2009]

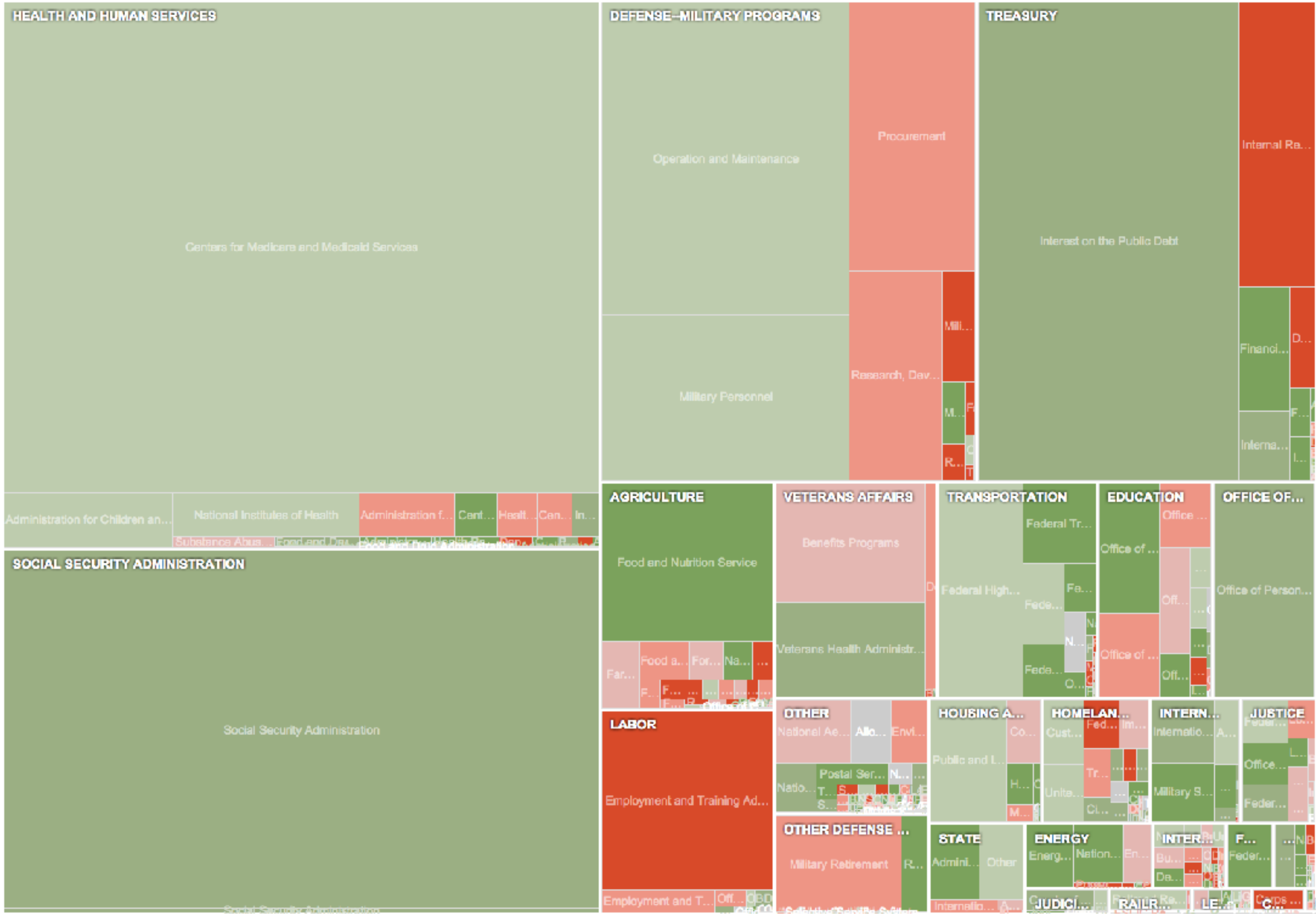
# Implicit Layouts for Trees



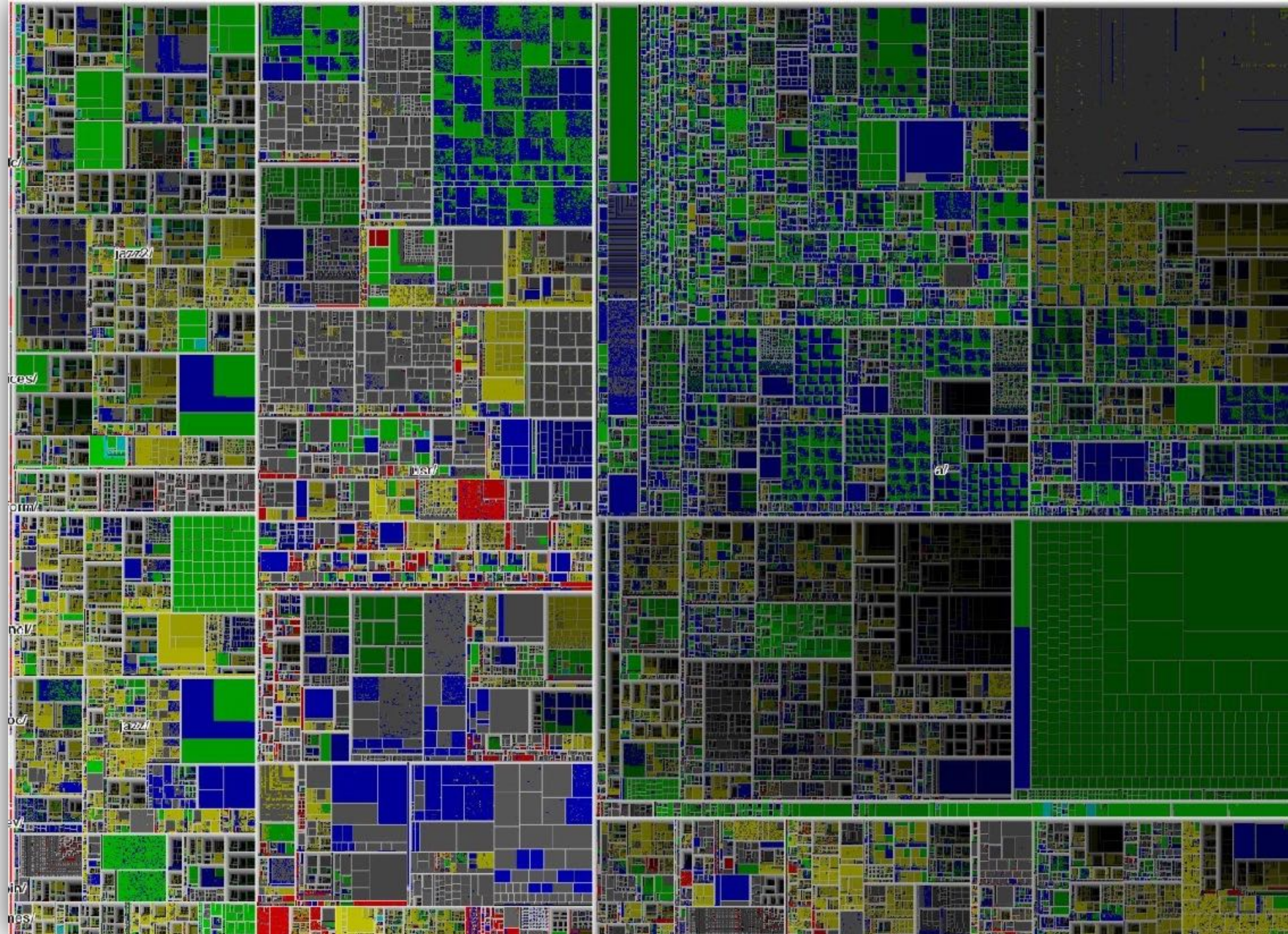
# Tree Maps



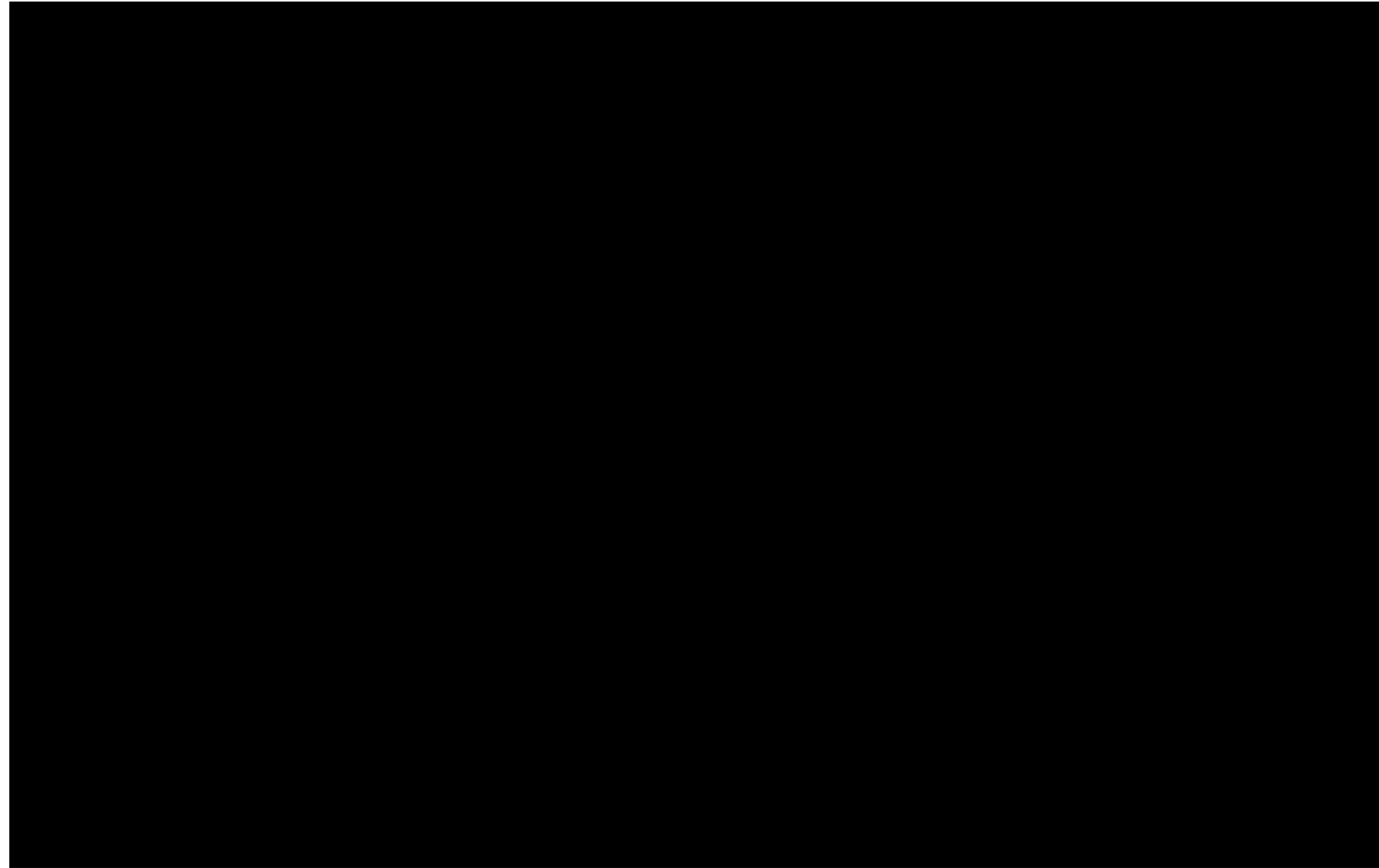
# Zoomable Treemap



# Example: Interactive TreeMap of a Million Items



# Sunburst: Radial Layout



[Sunburst by John Stasko, Implementation in Caleydo by Christian Partl]

# Implicit Representations


## Pros:

- space-efficient because of the lack of explicitly drawn edges: scale well up to very large graphs
- in most cases well suited for ABTs on the node set
- depending on the spatial encoding also useful for TBTs


## Cons:

- can only represent trees
- since the node positions are used to represent edges, they can no longer be freely arranged (e.g., to reflect geographical positions)
- useless to pursue any task on the edges
- spatial relations such as overlap or inclusion lead to occlusion

# Tree Visualization Reference

How to cite this site? [treevis.net - A Visual Bibliography of Tree Visualization 2.0 by Hans-Jörg Schulz](#)    v.21-OCT-2014

Check out other surveys! 

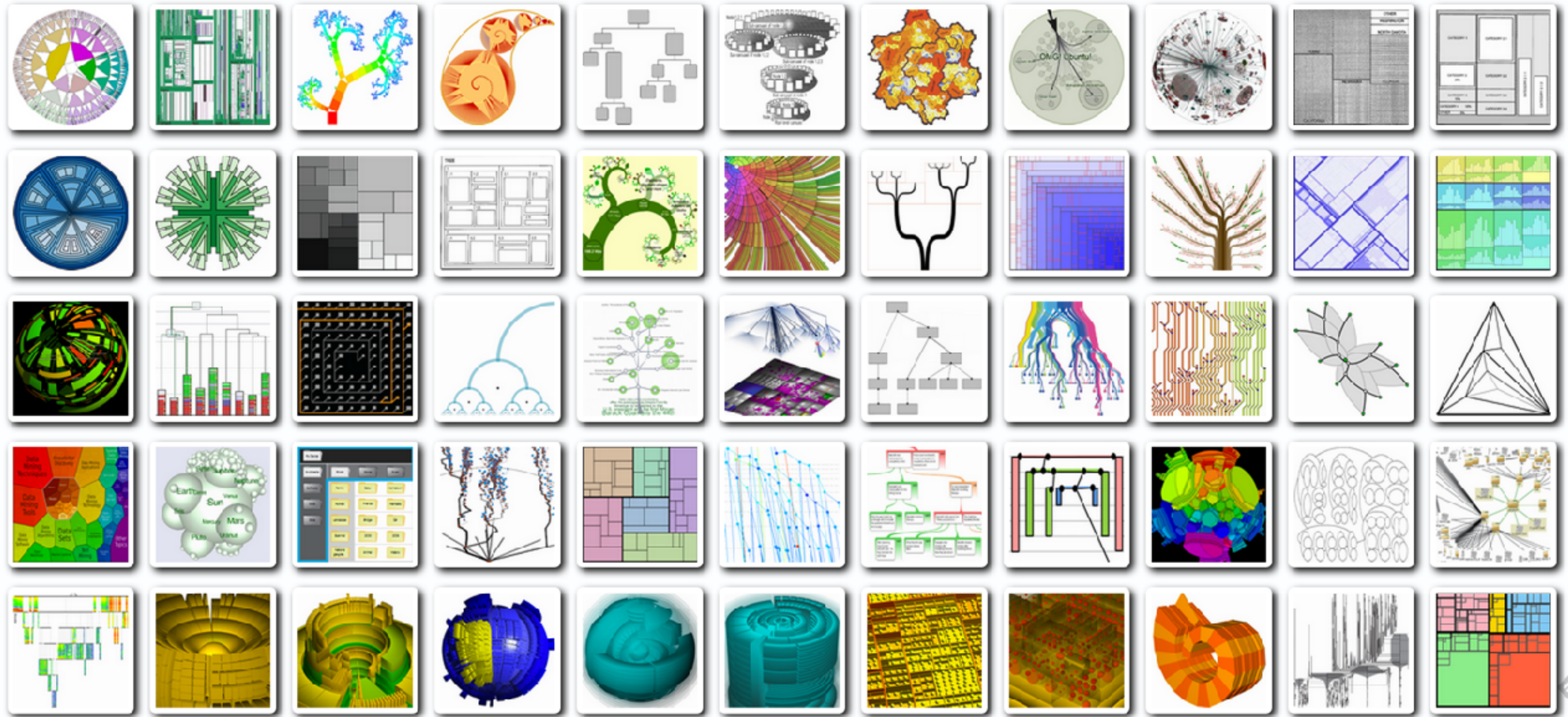
Dimensionality: All   

Representation: All   

Alignment: All   

Fulltext Search:  x

Techniques Shown: 277





# Visualizing Time Varying Graphs

Up to now: given graphs were **static**

**Extension:** given is a **sequence of graphs**

either the sequence is given in full (offline)  
or the sequence is streamed (online)

**Variants:**

*varying linkage:*

node set is fixed, only edges change over time

*varying attributes:*

graph structure is fixed, only attributes change

# Visualizing Time Varying Graphs

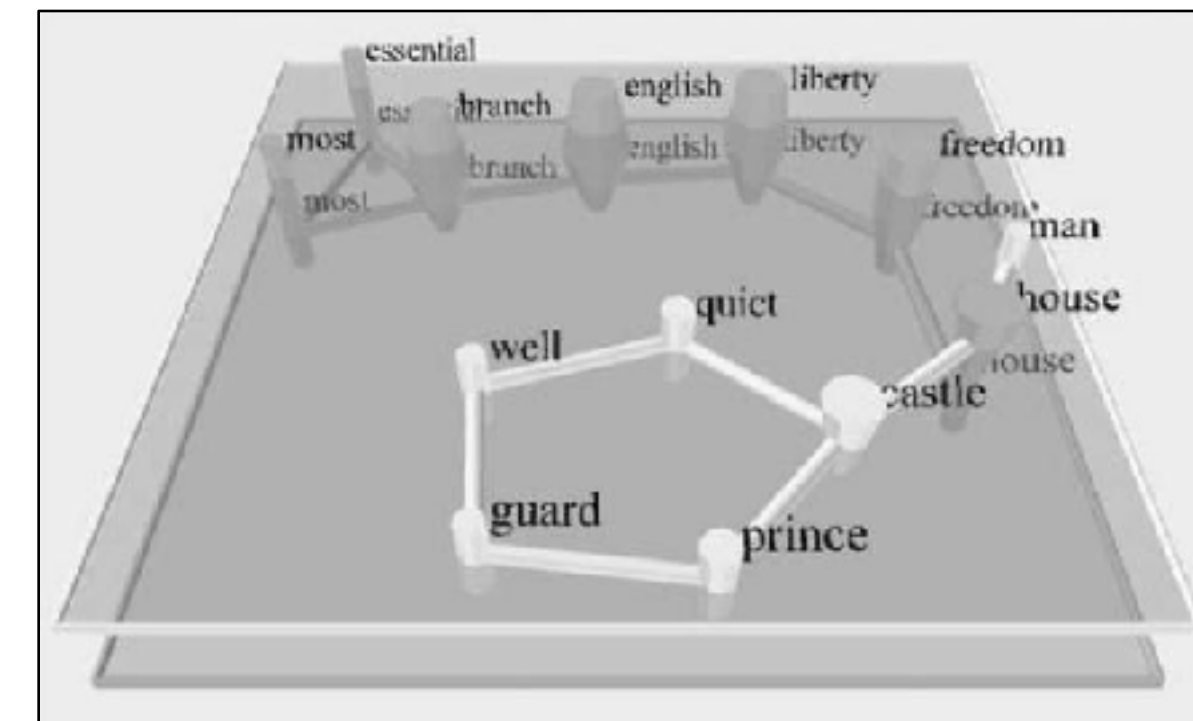
## Animation

Map time to time

## Layering

Layout graph in 2D and use 3<sup>rd</sup> dimension to show time

For small graphs with few time steps

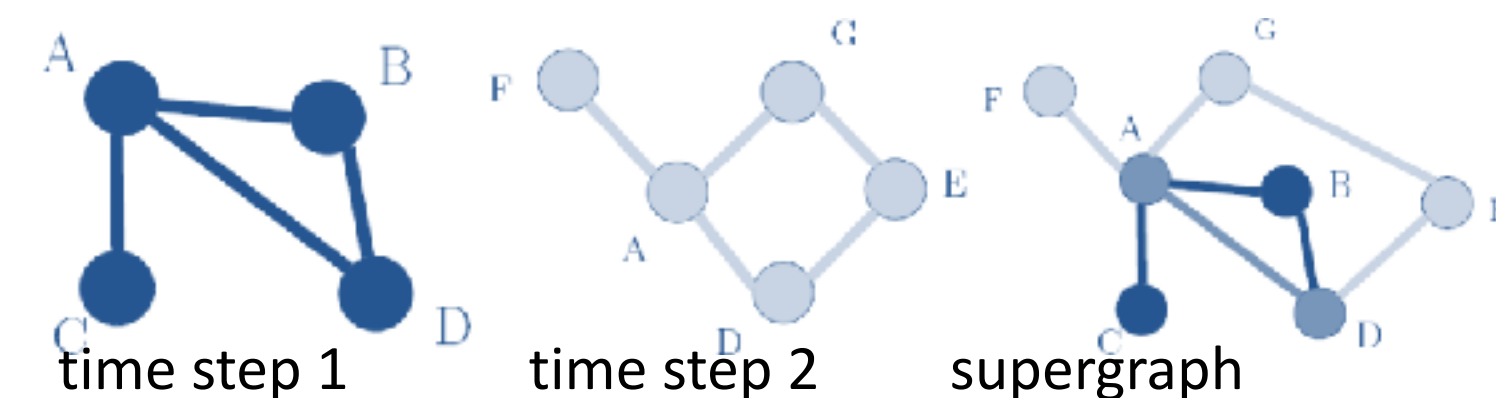


Brandes & Corman 2003

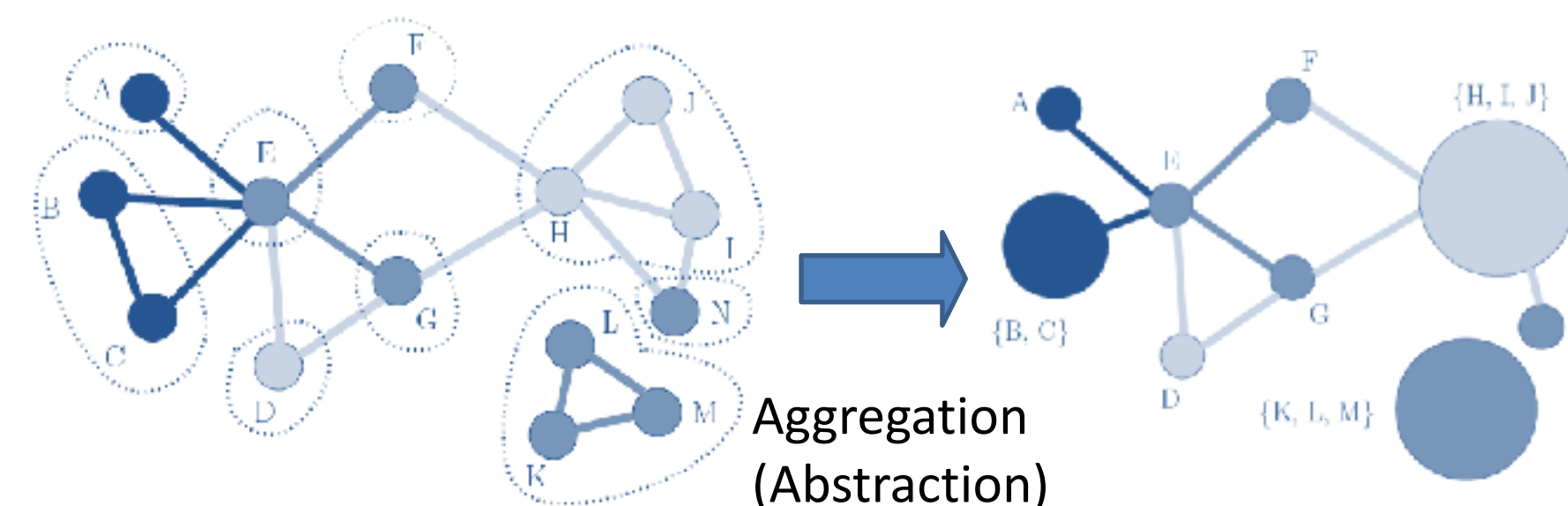
## Supergraph

Aggregate all time steps into a supergraph

Use colors etc. to represent time



## Aggregation



# Visualizing Edge Attributes

Most common ways to encode edge attributes

**Quantitative: Width**



**Ordinal: Saturation**



**Nominal: Style**



# Graph Interaction: Navigation

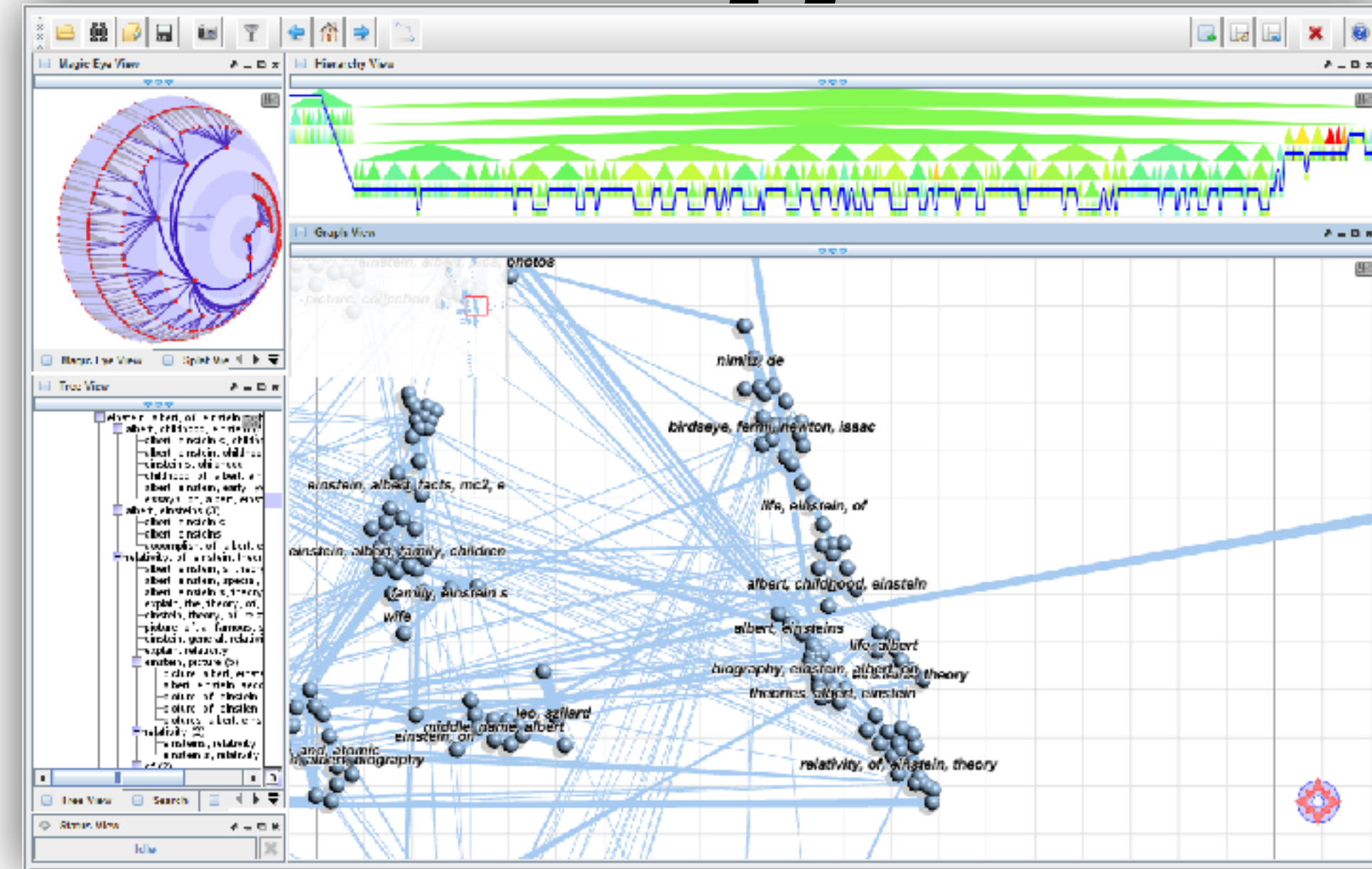
Standard techniques

e.g., overview+detail

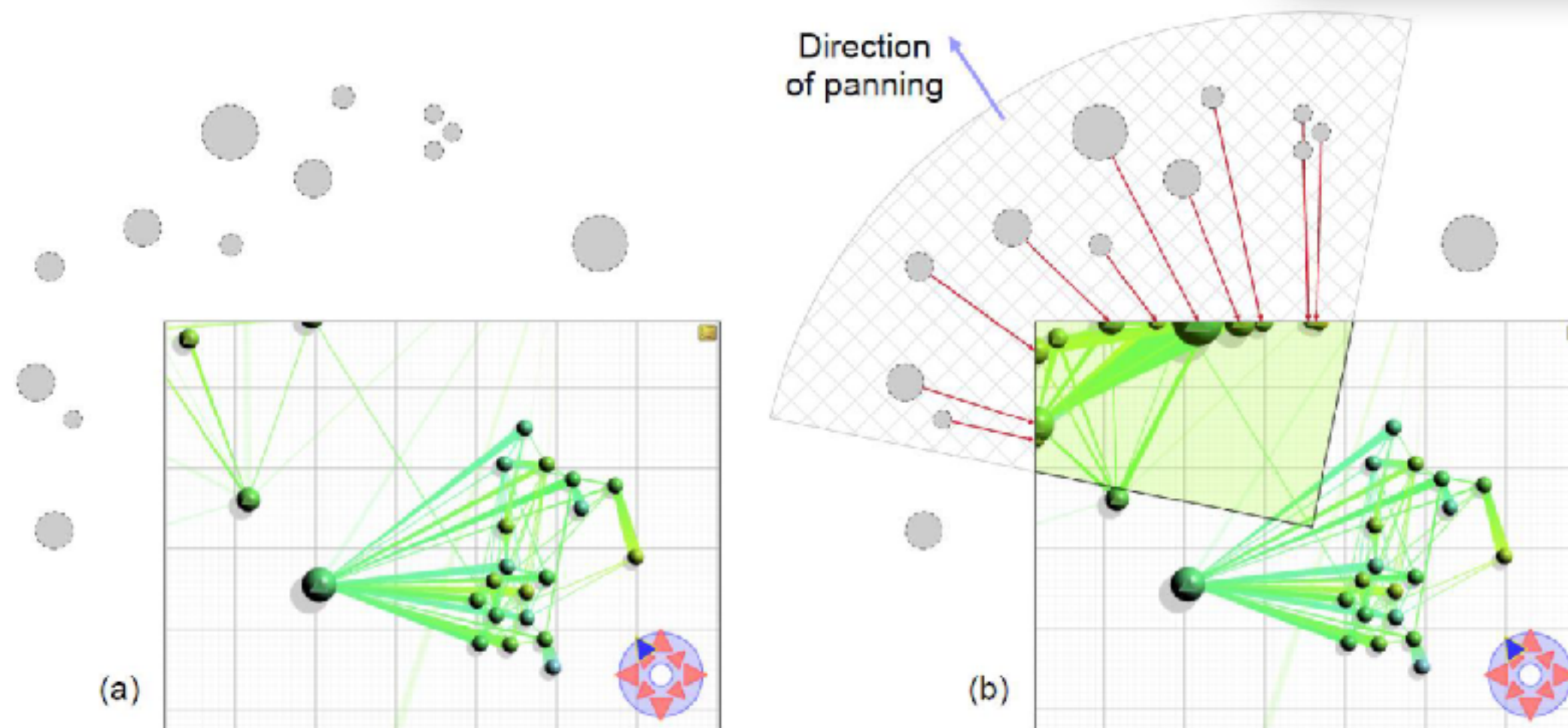
Edge-based traveling

Radar view for

foresighted panning



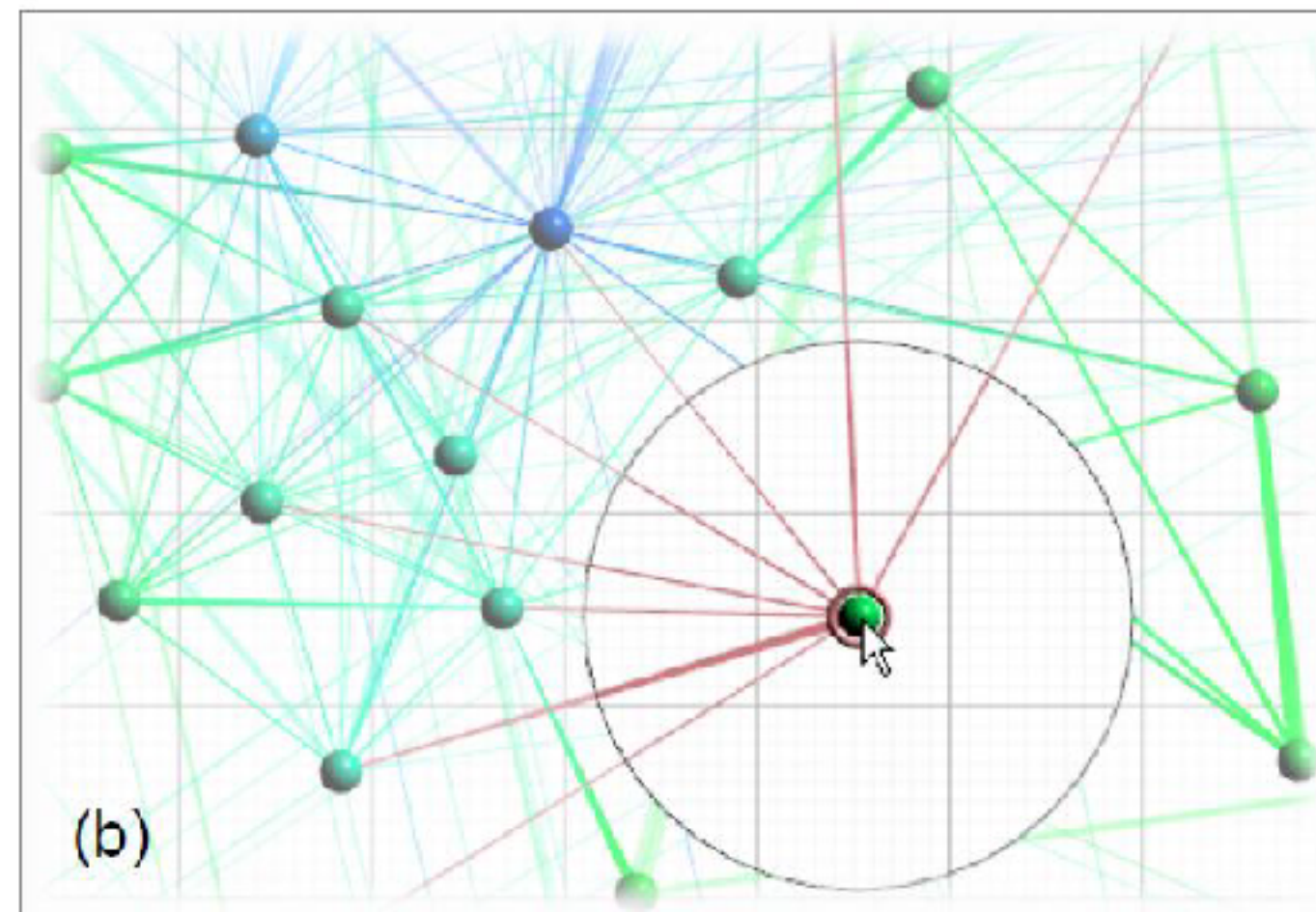
[Tominski et al. 2010]



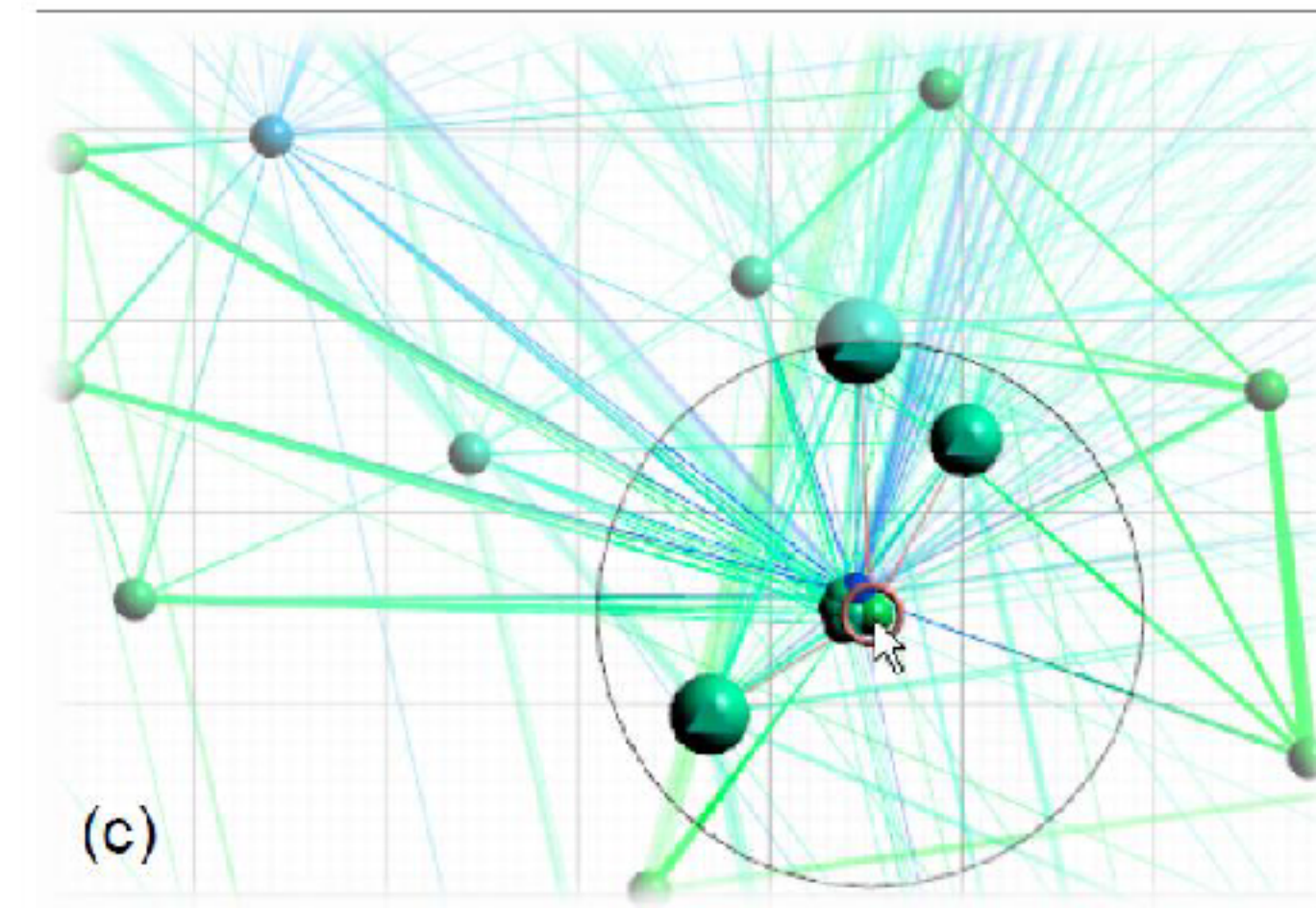
[Tominski et al. 2010]

# Graph Interaction: Manipulation

Details-on-demand: smart lenses (semantic lenses)



Local-Edge-Lens shows only edges incident to the nodes inside



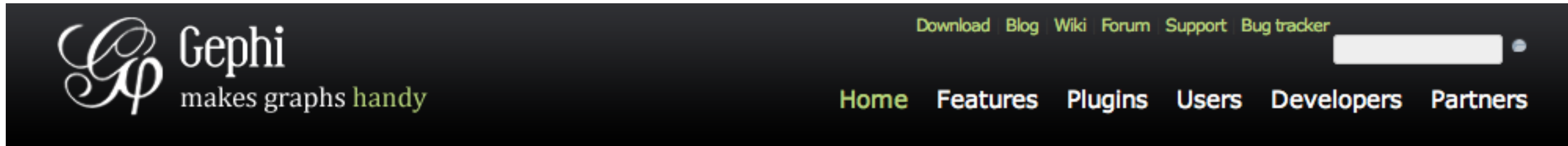
Bring-Neighbors-Lens gathers all neighbors of the center node

[Tominski et al. 2009]

# Graph Tools & Applications

# Gephi

<http://gephi.org>



## The Open Graph Viz Platform

Gephi is a visualization and exploration platform for all kinds of networks and complex systems, dynamic and hierarchical graphs.

Runs on Windows, Linux and Mac OS X. Gephi is open-source and free.

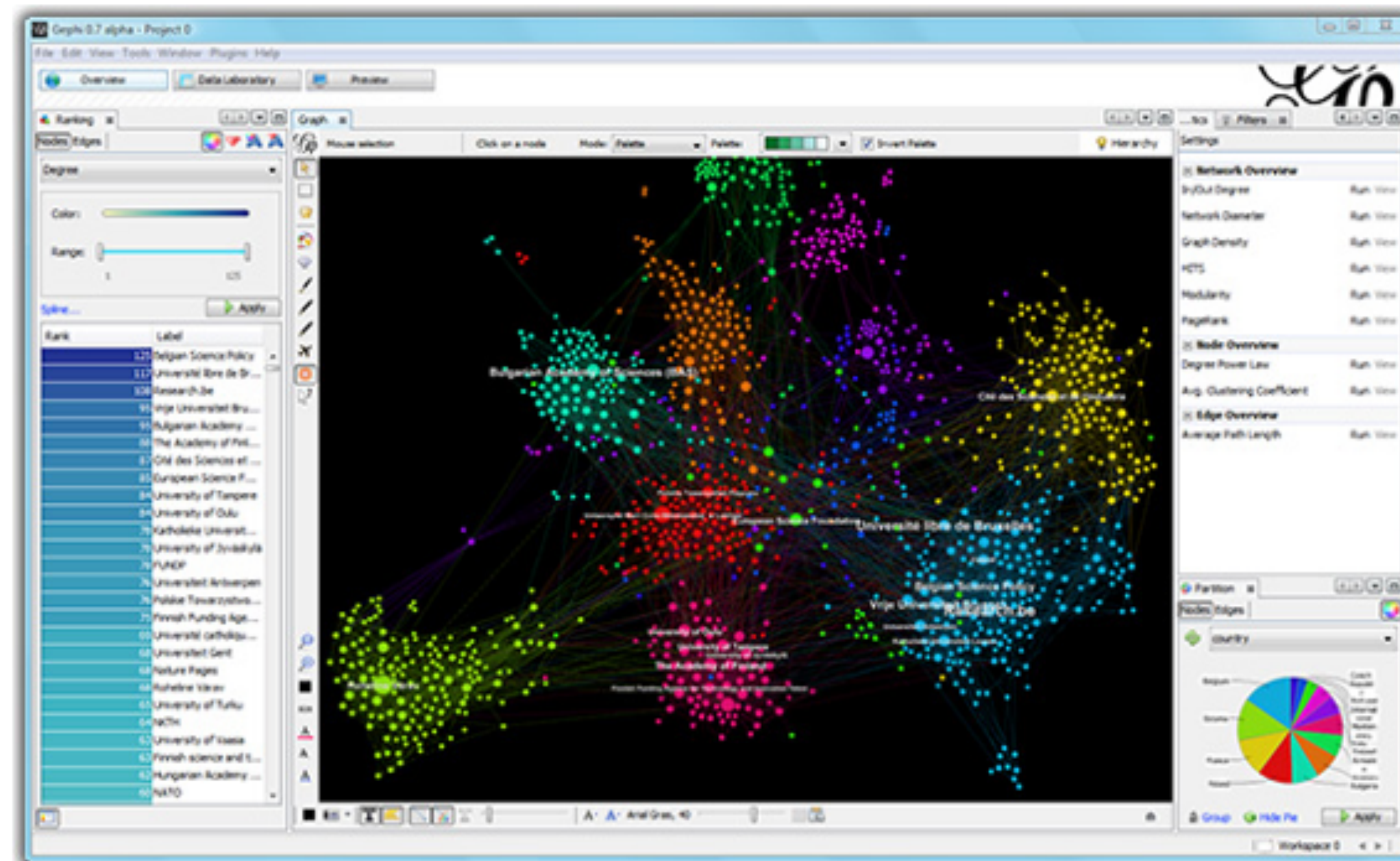
[Learn More on Gephi Platform »](#)



[Release Notes](#) | [System Requirements](#)

► [Features](#)  
► [Quick start](#)

► [Screenshots](#)  
► [Videos](#)



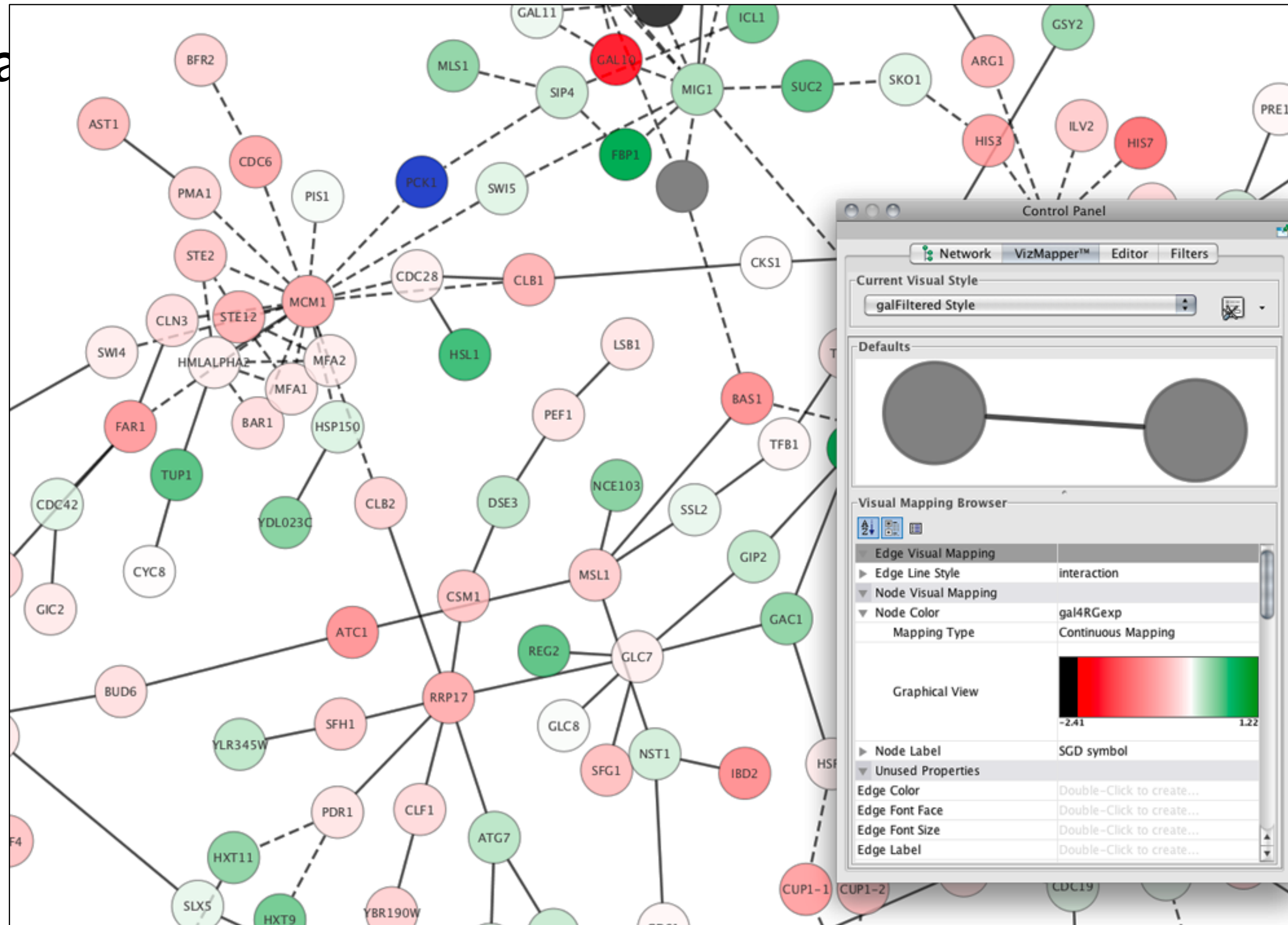
Gephi has been accepted again for Google Summer of Code! The program is the best way for students around the world to start contributing to an open-source project. Students, apply now for Gephi proposals. Come to the GSOC forum section and say Hi! to [this topic](#).

[Learn More »](#)

# Cytoscape

<http://www.cytoscape.org/>

Open source platform





# Cytoscape Web

<http://cytoscapeweb.cytoscape.org/>

**Cytoscape Web** Feature Showcase Demo

This is a separate demo application, built around the Cytoscape Web visualization. Because this showcase is complex, you may experience issues, such as slowdowns, on older or less efficient browsers.

Save file Open file Style Layout

Examples Visual style Filter Properties

Nodes Edges Reset filters

Filter such that every any filter is satisfied.

id Find a value to filter

label Find a value to filter

shape Find a value to filter

weight 0.03 0.45 0.5

The screenshot displays the Cytoscape Web interface. The main area shows a network diagram with nodes A01 through A09. Node A01 is a yellow circle, A02 is a grey triangle, A03 is a red octagon, A04 is a grey diamond, A05 is a grey parallelogram, A06 is a blue square, A07 is a green rectangle, A08 is a grey hexagon, and A09 is a grey pentagon. Edges connect these nodes, with some being solid blue and others dashed blue. A green dot is visible near node A02. The interface includes a top menu bar with 'Save file', 'Open file', 'Style', and 'Layout'. On the right, there are tabs for 'Examples', 'Visual style', 'Filter', and 'Properties'. Below these are 'Nodes' and 'Edges' tabs, and a 'Reset filters' button. A filter configuration panel is open, showing a filter rule: 'Filter such that every any filter is satisfied.' Below this are input fields for 'id', 'label', and 'shape', each with a 'Find a value to filter' placeholder. A 'weight' slider is also present, ranging from 0.03 to 0.5, with a current value of 0.45. At the bottom right, there are navigation icons for zooming and panning.

# NetworkX

<https://networkx.github.io/>

## NetworkX

[NetworkX Home](#) | [Documentation](#) | [Download](#) | [Developer \(Github\)](#)

### High-productivity software for complex networks

NetworkX is a Python language software package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.



#### [Documentation](#)

*all documentation*

#### [Examples](#)

*using the library*

#### [Reference](#)

*all functions and methods*

### Features

- Python language data structures for graphs, digraphs, and multigraphs.
- Nodes can be "anything" (e.g. text, images, XML records)
- Edges can hold arbitrary data (e.g. weights, time-series)
- Generators for classic graphs, random graphs, and synthetic networks
- Standard graph algorithms
- Network structure and analysis measures
- Open source [BSD license](#)
- Well tested: more than 1800 unit tests, >90% code coverage
- Additional benefits from Python: fast prototyping, easy to teach, multi-platform

#### Versions

#### Latest Release

1.8.1 - 4 August 2013  
[downloads](#) | [docs](#) | [pdf](#)

#### Development

1.9dev  
[github](#) | [docs](#) | [pdf](#)  
build passing  
coverage 83%

#### Contact

[Mailing list](#)  
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[Developer guide](#)

